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Investigation of Aperture Coupled Microstrip Antenna to Obtain a High Efficient Active Integrated Antenna by Using Class F and Inverse Class F Power Amplifiers

Lei Liu

PhD 2013
Investigation of Aperture Coupled Microstrip Antenna to Obtain a High Efficient Active Integrated Antenna by Using Class F and Inverse Class F Power Amplifiers

Lei Liu

A thesis submitted in partial fulfilment of the requirements of the University of Northumbria at Newcastle for the degree of Doctor of Philosophy

Research undertaken in the Faculty of Engineering and Environment

October 2013
Abstract

In wireless communications and radar systems, there are requirements for high efficiency, small size, low cost, and wide bandwidth of transmitter front-end usage for commercial and also military applications. Active integrated antenna (AIA) could satisfy almost all the requirements. The overall objective of the proposed research is to model, optimise, and design a compact and high efficient AIA using an aperture coupled microstrip antenna (ACMA) by integrating with a power amplifier (PA). Research on ACMA has been focused on the transmissions line (TL) model (TLM) and full wave electromagnetic (EM) model analysis. The full wave investigation is rigorous and elegant but because the dimension of the physical model and the value of the circuit elements are interdependent, the design of the antenna is still difficult. TLM analysis has lower accuracy but easier to analysis and optimise than full wave EM model analysis. To increase the accuracy, the challenge is the coupling ratios between feed/slot, and slot/patch where no unique solution at the moment exists. In this thesis, a novel and simplified method has been produced to investigate these ratios using Scattering (S) parameters. A dual frequency ACMA has been designed to verify these results. Research on the class F and inverse class F PAs is carried out by a novel and simplified load/pull method. A new design method of harmonic load matching network has been presented using lump elements and TLs. Both linear and nonlinear modelling has been investigated. High power added efficiency (PAE) and high gain which are up to 60% and 12dB have been obtained. Finally AIAs have been produced based on previous investigation on class F, inverse class F PAs and a broadband circular polarized ACMA design with 350 MHz bandwidth and 8.5 dB gain at 2 GHz.
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### Glossary of Symbols

- **a**: Incident power
- **b**: Reflected power
- **C**: Capacitance
- **E**: Source power
- **\( \varepsilon_r \)**: Relative permittivity
- **\( \varepsilon_{\text{reff}} \)**: Effective relative permittivity
- **f**: Frequency
- **f_0**: Fundamental frequency
- **G**: Conductance
- **\( G_p \)**: Power gain
- **H**: Height
- **h**: Height of substrate between feed and slot
- **I_{dc}**: DC current
- **I_{ds}**: Current flow over transistor
- **I_{Fun}**: Current at fundamental frequency
- **I_I**: Input current
- **i_{max}**: Peak current of transistor
- **i_p**: Peak current of active device
- **I_R**: Reflected current
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$k_0$</td>
<td>Wave propagation constant in air</td>
</tr>
<tr>
<td>$L$</td>
<td>Inductance</td>
</tr>
<tr>
<td>$L_c$</td>
<td>Length of conductor</td>
</tr>
<tr>
<td>$L_{eff}$</td>
<td>Effective length</td>
</tr>
<tr>
<td>$L_{os}$</td>
<td>Length of open circuit line</td>
</tr>
<tr>
<td>$L_p$</td>
<td>Length of patch</td>
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<tr>
<td>$L_s$</td>
<td>Length of slot</td>
</tr>
<tr>
<td>$L_{st}$</td>
<td>Length of stub</td>
</tr>
<tr>
<td>$n_f$</td>
<td>Turns ratio between feed and slot</td>
</tr>
<tr>
<td>$n_p$</td>
<td>Turns ratio between slot and patch</td>
</tr>
<tr>
<td>$P_a$</td>
<td>Power available</td>
</tr>
<tr>
<td>$P_{AC}$</td>
<td>AC power</td>
</tr>
<tr>
<td>$P_{DC}$</td>
<td>DC power</td>
</tr>
<tr>
<td>$P_{diss}$</td>
<td>Power dissipation</td>
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<tr>
<td>$P_{Fun}$</td>
<td>Power at fundamental frequency</td>
</tr>
<tr>
<td>$P_L$</td>
<td>Power obtained by the load</td>
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<tr>
<td>$P_{out}$</td>
<td>Power output</td>
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<tr>
<td>$R$</td>
<td>Resistance</td>
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<tr>
<td>$R_L$</td>
<td>Load resistance</td>
</tr>
<tr>
<td>$R_{on}$</td>
<td>Internal resistance of transistor</td>
</tr>
<tr>
<td>$R_s$</td>
<td>Surface resistance</td>
</tr>
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<td>Description</td>
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<tr>
<td>--------</td>
<td>-------------</td>
</tr>
<tr>
<td>$S_{11(22)}$</td>
<td>Reflection coefficient</td>
</tr>
<tr>
<td>$S_{21(12)}$</td>
<td>Transmission coefficient</td>
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<tr>
<td>$T$</td>
<td>Tallness</td>
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<td>$V_{DD}$</td>
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<td>Knee voltage</td>
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<tr>
<td>$v_{max}$</td>
<td>Peak voltage of active device</td>
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<td>$V_p$</td>
<td>Pinch off voltage</td>
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<td>Width of stub</td>
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<td>$Z_{0s}$</td>
<td>Characteristic impedance of slot</td>
</tr>
<tr>
<td>$Z_{2n}$</td>
<td>Impedance at even harmonic frequency</td>
</tr>
<tr>
<td>$Z_{2n+1}$</td>
<td>Impedance at odd harmonic frequency</td>
</tr>
<tr>
<td>Symbol</td>
<td>Definition</td>
</tr>
<tr>
<td>--------</td>
<td>---------------------------------------------------------------------------</td>
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<tr>
<td>$Z_{Fun}$</td>
<td>Impedance at fundamental frequency</td>
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</tr>
<tr>
<td>$Z_s$</td>
<td>Impedance of slot</td>
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<td>$\alpha$</td>
<td>Attenuation constant</td>
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</tr>
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<td>Phase constant</td>
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<td>Propagation constant</td>
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<td>$\delta$</td>
<td>Skin depth</td>
</tr>
<tr>
<td>$\Delta L$</td>
<td>Extended length of fringing field</td>
</tr>
<tr>
<td>$\Delta L_s$</td>
<td>Extended length of slot</td>
</tr>
<tr>
<td>$\eta$</td>
<td>Power converted efficiency</td>
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<td>$\eta_A$</td>
<td>Average efficiency</td>
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<td>$\theta_s$</td>
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</tr>
<tr>
<td>$\lambda$</td>
<td>Wavelength</td>
</tr>
<tr>
<td>$\lambda_p$</td>
<td>Wavelength of patch</td>
</tr>
<tr>
<td>$\lambda_s$</td>
<td>Wavelength of slot</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Absolute magnetic permeability of the conductor</td>
</tr>
</tbody>
</table>
\( \rho \) Bulk resistivity

\( \omega \) Angular frequency

\( f(\theta, \phi) \) Magnitude of field
## Glossary of Acronyms

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Definition</th>
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<tbody>
<tr>
<td>AC</td>
<td>Alternating Current</td>
</tr>
<tr>
<td>ACMA</td>
<td>Aperture coupled microstrip antenna</td>
</tr>
<tr>
<td>ADS</td>
<td>Advanced Design System</td>
</tr>
<tr>
<td>AIA</td>
<td>Active Integrated Antenna</td>
</tr>
<tr>
<td>AlGaAs</td>
<td>Aluminium Gallium Arsenide</td>
</tr>
<tr>
<td>AM</td>
<td>Amplitude Modulation</td>
</tr>
<tr>
<td>AR</td>
<td>Axial Ratio</td>
</tr>
<tr>
<td>CST</td>
<td>Computer Simulation Technology</td>
</tr>
<tr>
<td>dB</td>
<td>Decibel</td>
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<td>DC</td>
<td>Direct Current</td>
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<tr>
<td>EM</td>
<td>Electromagnetic</td>
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<tr>
<td>GA</td>
<td>Genetic Algorithm</td>
</tr>
<tr>
<td>GaN</td>
<td>Gallium Nitride</td>
</tr>
<tr>
<td>Ge</td>
<td>Germanium</td>
</tr>
<tr>
<td>GHz</td>
<td>Gigahertz</td>
</tr>
<tr>
<td>GPS</td>
<td>Global Positioning Satellite</td>
</tr>
<tr>
<td>HB</td>
<td>Harmonic balance</td>
</tr>
<tr>
<td>HBT</td>
<td>Heterojunction Bipolar Transistor</td>
</tr>
<tr>
<td>HEMT</td>
<td>High Electron Mobility Transistor</td>
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<tr>
<td>Abbreviation</td>
<td>Description</td>
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<td>--------------</td>
<td>---------------------------------------</td>
</tr>
<tr>
<td>HF</td>
<td>High frequency</td>
</tr>
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<td>HFET</td>
<td>Heterojunction Field Effect Transistor</td>
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<tr>
<td>InGaAs</td>
<td>Indium Gallium Arsenide</td>
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<td>InP</td>
<td>Indium Phosphide</td>
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<td>LF</td>
<td>Low frequency</td>
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<td>Megahertz</td>
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<td>ML</td>
<td>Microstrip Line</td>
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<tr>
<td>mW</td>
<td>Milliwatt</td>
</tr>
<tr>
<td>PA</td>
<td>Power Amplifier</td>
</tr>
<tr>
<td>PAE</td>
<td>Power Added Efficiency</td>
</tr>
<tr>
<td>PCB</td>
<td>Printed Circuit Board</td>
</tr>
<tr>
<td>pHEMT</td>
<td>pseudomorphic High Electron Mobility Transistor</td>
</tr>
<tr>
<td>RF identification</td>
<td>RFID</td>
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<td>RF</td>
<td>Radio Frequency</td>
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<td>SiC</td>
<td>Silicon Carbide</td>
</tr>
<tr>
<td>SL</td>
<td>Slot line</td>
</tr>
<tr>
<td>TE</td>
<td>Telegrapher's Equation</td>
</tr>
<tr>
<td>TL</td>
<td>Transmission Line</td>
</tr>
<tr>
<td>TLM</td>
<td>Transmission Line Model</td>
</tr>
<tr>
<td>UHF</td>
<td>Ultra high frequency</td>
</tr>
<tr>
<td>VHF</td>
<td>Very high frequency</td>
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October, 2013
Declaration

I declare that the work contained in this thesis has not been submitted for any other award and that it is all my own work.

Lei Liu

October 2013
Chapter 1 Introduction and Overview

1.1 Introduction

In wireless communications and radar systems, there are requirements for high efficiency, small size, low cost, and wide bandwidth transmitter at the front-end usage for commercial and also military applications. AIA [1, 2] could satisfy almost all the requirements, which could be regarded as an active microwave circuit by replacing the output and input ports using wireless components instead of a conventional interface [3]. In order to reduce the power consumption at the transmitter and receiver, it is important to reduce the power dissipation or improve the power conversion efficiency from DC to the AC signal for the PA. To reduce the size, the radiation element could be directly integrated with the active device with matching networks or alternatively for additional size reduction, the radiation element could be used as the optimum load for the PA section. The cost of AIA could be reduced by using different integration methods, transistors, or suitable materials for different applications [4]. A wide bandwidth is quite essential when designing AIA for radio frequency (RF) wireless technologies with multimedia capabilities. AIA applications have been extended to the area of quasi-optical power combiners in the past ten years [2, 5-7]. In this thesis, analysis of TLM of the ACMAs is carried out to obtain a broad band and a high gain as the radiation element, as well as an optimum load for the PA. The thesis shows comprehensive investigation of PAs with the aim of improving the efficiency, gain and increasing the bandwidth by means of using the switch mode active device and novel designed harmonic matching networks.

As the radiation element, the traditional microstrip based patch antennas offer small size, low cost, ease of integration at the cost of a narrow bandwidth, poor gain, and limited
applications. In order to overcome these problems, the ACMA [8, 9] was proposed and utilized to obtain a wide bandwidth and high gain. Due to its separate feed and radiation element structure, it is easy to use different feed methods [10-12], substrates and many patch shapes [13, 14] in order to obtain the optimum performance. The circular polarized antenna and arrays [15-22] were introduced to increase the gain for satellite communication applications. The EM simulation method for the antenna design is accurate and rigorous. However, the dimension of physical model and parameters of circuit elements are interdependent and the antenna design is still difficult. Hence, the simplified TLM analysis is used for investigation and design which is relatively straightforward for further optimization using the genetic algorithms (GAs) [23-25], stochastic algorithms [26, 27], and conjugate gradients [28, 29], etc. The key problem in circuit modelling is the two turns ratios between feed/slot $n_f$ and slot/patch $n_p$, which are reported in numerous research publications, however with no single approach or technique. In this thesis a simplified theoretical method for analysing the turn ratios by means of S parameter is presented. To verify the mathematical theory, simulation is carried out and the results are compared with the measured data. Equations are derived by means of curve fitting methods for $n_f$ and fringing field using the large gap between slot/patch with the air substrate. A broadband dual frequency linear polarized ACMA is subsequently designed to verify the obtained results.

In order to achieve high power conversion efficiency for DC-to-AC signal, switching model class F and inverse class F PAs are used, where the active device is driven by a large input signal to ensure that the active device functions as a switch. The power dissipation from the active device is due to the internal resistance of transistor which causes the overlap of flowed voltage and current. In order to overcome this problem, the harmonic load matching networks are proposed in order to shape the voltage and current
waveforms by the lumped elements and the TLM. The ideal linear switch models are developed for the simulation purpose and mathematical expressions are derived for the output power, optimum load impedance, and efficiency in order to investigate the system performance. For non-linear simulation, based on Statz model, a simplified load/source pull method is proposed for the harmonic source and the load matching network in order to obtain maximum PAE as well as the gain. The thesis outlines detailed comparison of class F and inverse class F PAs with lossless TL, and microstrip line (ML) model. Source and load matching network designs and also harmonics effects have been presented.

For the AIA design, a broadband circular polarized ACMA is designed at 2 GHz to integrate with the class F and inverse class F PAs. Simulation methods are also adopted to predict the PAE and gain by replacing the load of PAs with an antenna. Based on these results, two practical AIAs using class F PA and inverse class F PAs are designed, fabricated and tested. In the advanced AIA design, the harmonic load matching network of PA can be eliminated and directly integrated with the antenna as the harmonic load. In this case, the antenna acts both as the radiating element and the optimum load. However, the design procedure is rather complex, which could lead to a more compact module.

1.2 Motivations and Objectives of the Research

Based on the defence and space applications, the demand for both the microstrip antennas and AIAs have increased with emphasis on the performance rather than the cost. However, for commercial civilian applications such as global positioning satellite (GPS), cellular phone, RF identification systems (RFID), personal communication systems, automatic toll collection, wide area computer networks, and RF energy harvesting systems, the reduction of cost has the priority by comparing with high-quality performance. In order to have the
best of two worlds (i.e. performance and reduced costs) broadband, high gain, dual
frequency, or circularly polarized microstrip antennas are the way forward. Adopting the
circuit design method can lead to reduced simulation time and utilising GA or other
optimization methods could assist in more accurate. Research based on either the cavity
method [14] or the full wave EM analyses [9] are rigorous but complex and with
conflicting results. Hence, TLM analysis has been carried out which is simple structured
but low accuracy. To improve this, the challenges of TLM focus on the turns ratio between
feed/slot, and slot/patch. The PA is the most costly element in RF circuits [30]. To
minimize the cost, and enhance the efficiency and gain, research has been mainly focused
on the power dissipation analysis of transistor, harmonics control and also the low cost
material used by MLs. To obtain maximize the PAE and the gain, the switch model class F
and inverse class F PAs are investigated and compared using a novel design for harmonic
load matching networks. The objectives of this research are summarized as follows:

- To develop a novel and simplified topology for calculating, simulating, and
  measuring $n_f$ and $n_p$ using the $S_{21}$ and $S_{11}$ parameters.
- To verify the turns ratio produced by designing an ACMA using the TLM.
- To produce a simplified design procedure to produce an ACMA using the TLM.
- To develop a logical and novel method to design harmonic load matching networks
  of class F and inverse class F PAs using the lump elements and TLM.
- To predict the power converted efficiency, PAE and gain using linear and nonlinear
  models of transistor for the class F and inverse class F PAs.
- To produce AIAs based on the designed classes F and inverse class F PAs
  integrated with the circular polarized antenna.
1.3 Contributions of Research

- A simplified and novel method has been developed to produce the turns ratio between feed and slot using $S_{21}$ and $S_{11}$ parameters which has been verified by simulation and practically measurement, see Chapter 3. Additionally an expression is derived for this turns ratio in terms of the slot length and height of the substrate using the curve fitting method.

- A dual frequency broad band aperture coupled antenna has been designed using the TLM to approve the validity of turns ratio between the feed and slot produced by means of simulation and practical measurement, which is presented in Chapter 3.

- A novel and simplified design approach has been developed by using the TLM for the design of an ACMA, which is shown in Chapter 3.

- Novel topologies have been developed to produce harmonic load matching networks using the lumped element and the TLM to satisfy the conditions of class F PA and inverse class F PAs with accurate numerical calculation and also simulation validation by ADS software, which is presented in Chapter 4.

- Power converted efficiency investigation has been systematically carried out by simulation using the linear model of transistor under the conditions of varying internal loss of the active device, infinity harmonics of the load matching network, up to third harmonics matching network using the ideal TL and the lossy ML, which is shown in Chapter 4.

- Novel load/source pull methods have been developed based on the new harmonic load matching network design methods. Performances of the PAE and gain have been compared by means of simulation using ADS software for the nonlinear model class F and inverse class F PAs, which is presented in Chapter 5.
1.4 Outline of Thesis

This thesis presents a simplified method of investigation into ACMA by using circuit and TLMs, which focus on the turns ratio analysis. Also the performance of class F and inverse class F PAs are investigated by linear and non linear models.

Chapter 2 reviews the primary and secondary parameters of the TL theory, which is based on Maxwell’s equations indicating that the TLs are equivalent to the lumped circuit of a resistor, inductor, conductor and capacitor. The characteristic impedance is indicated by the ratio of voltage to current when signal is applied to an infinite long line. The propagation constant is expressed by the attenuation constant and the propagation constant. The ML is one type of electrical TL, which is fabricated in printed circuit board (PCB). For practical usage, the ML is easy to be used as an integrated circuit design. However, power will be dissipated due to the loss factors, which are the conductor and dielectric losses. To minimize this problem, low loss materials are normally chosen for the design but at a high cost. Equations are derived for the reflection and transmission coefficients in terms of source, load impedance and also the voltage and current, which are utilized for further analysis. Microstrip patch antennas are introduced with different patch shapes and feed methods. In this work the ACMA is selected for the further analysis due to its characteristics of flexible structure, wide bandwidth and high gain.

Chapter 3 investigates the TL model of a rectangular patch ACMA. By comparing with the full wave EM model, which is more accurate but difficult to analyse requiring complex equations, the TLM can be easily analysed using circuits to save simulation and also optimization time. The key challenge of the circuit model is the coupling ratios between feed/slot, and slot/patch, which has been investigated by number of researchers using
different rigorous methods. However, there are non-unique and simple solutions for the TLM analysis. This work outlines a simplified method to calculate, simulate and also measure the turns ratio using the S parameters for different substrates. Equations are derived in terms of the height of substrates and the length of slot. Based on these results, a wide bandwidth dual frequency dual polarized ACMA is designed to verify the theoretical analysis.

In Chapter 4, the PA histories and theories are reviewed. The PAs are analysed for the class A to class F and the inverse class F. In this thesis, class F and inverse F PAs are selected for analysis due to their high performance and low profile. The active device ideally works as a switch to minimize the voltage and current overlap and also the power dissipation from transistor. Hence, an ideal switch connected with a resistor is used to model the active device. The harmonic load matching networks are designed for both PAs to shape the voltage and current waveforms using the lump elements model and also the TLM. A novel and logical method is also proposed to design the harmonic load matching network with accurate calculations.

In Chapter 5, loss investigation is carried out for the shunt stub of harmonic matching networks using S parameters. A circuit model is proposed to indicate the power dissipation in terms of the resistor and transmission length. To investigate the nonlinear model, the transistor is modelled by Statz model based on the data sheet from ATF 33143. Based on the designed harmonic matching networks, the performance of class F PA and inverse class F PA are investigated and compared in terms of a range of input power levels and frequencies. The source harmonic terminations are also analysed by the second and third harmonic controls and comparisons are carried out for both PAs.
Chapter 6 presents the concepts of AIA, which can integrate circuit functions such as filter, mixer, and power amplifier, thus saving the space and reducing the power dissipation. A broadband circular polarized ACMA is designed, which is based on the analysis in Chapter 3, to replace the load of PA. The comparison is carried out using class F and inverse F PAs based on Chapter 5 with simulation and also practical measurement.

Chapter 7 concludes the work that has been done. A further design method of AIA to obtain a smaller size and a higher efficiency is presented. An ACMA can be used as the optimum harmonic load of active device by eliminating the matching network to improve the efficiency. GA is introduced to optimise the bandwidth of antenna, enhance the efficiency and the gain of AIA.

The issues, effects, solutions, and original contributions are listed in the road map in Fig. 1.1.
Fig. 1.1 Summary of the issues, effects, current solutions and original contributions in AIA research.
1.5 List of Publications

Journals


Conferences


Chapter 2 Review of Transmission Line and Microstrip

Antenna Theory

2.1 Introduction

This chapter introduces the concept of TL, which is a material medium that forms a patch for transmitting energy from one place to another. Each elementary element of TL can be represented by a series resistance connect with an inductance; parallel connect with a leakage conductance and a capacitance. These four parameters are called primary constants. The secondary constants - characteristic impedance and propagation constant are constrained by these primary constants and will be used in the ML analysis. A ML is an electrical TL with metal and ground printed on two sides of dielectric substrate. A ML can be used in integrated circuits and combine multi-functional elements using PCB technology. When a signal propagates along the TL, there will be power reflected back and power that goes through which can be analysed by a two port network. Electrical properties of networks can be expressed by scattering parameters (S parameters) such as gain, return loss, voltage standing wave ratio, reflection coefficient, etc[9]. In antenna design field, the power reflected back can be represented by $S_{11}$ which is called input port voltage reflection coefficient. For a two port network as used in designing of a power amplifier, the forward voltage gain can be indicated by $S_{21}$. At the end of this chapter, this author introduces the characteristics of microstrip patch antenna which consist of radiation element, substrate, and also ground plane. Different shapes of radiation elements are introduced with the performance of bandwidth and gain. Five feed methods are also
presented which are used to connect the antennas with integrated circuits or other RF components.

2.2 Review of TL Theory

In an electronic system, the delivery of power requires the connection of two wires between the source and the load. At low frequencies, power is considered to be delivered to the load through the wire. In the microwave frequency region, power is considered to be propagating in electric and magnetic fields that are guided through a channel. Any physical structure that guides an electromagnetic wave is known as the TL [9, 14]. TLs are normally in the forms of two wire lines, coaxial cable, wave guide and planar TL, with the latter being widely adopted in this thesis. Planar TLs mainly include strip line, ML, slot line, fin line, coplanar waveguide and coplanar slot line [31, 32]. In the following section primary and secondary parameters of TLs will be discussed.

2.2.1 Primary Constants

The relationship of voltage and current on an electrical TL as a function of the distance and time was described by the Telegrapher's Equations (TEs) [33] developed by Oliver Heaviside who created the transmission model based on Maxwell’s equations [34, 35]. This model represents the TL as an infinite series of two-port elementary components, each representing an infinitesimally short segment of the TL, with the equivalent elementary section shown in Fig. 2.1 [36-38].
where,

\( R \) (unit: \( \Omega \)): Resistance per unit length, which is due to finite resistivity of conductors.

\( G \) (unit: S): Leakage conductance per unit length, which is due to losses in an imperfect insulator.

\( C \) (unit: F): Capacitance per unit length, which is due to the potential difference between conductors generating the electric field.

\( L \) (unit: H): Inductance per unit length, which is due to the magnetic field generated by the AC current.

2.2.2 Secondary TL Parameters

When the signal is applied to an infinitely long line, the ratio of voltage to current implied on any distance from the source is defined as the line characteristic impedance \( Z_0 \). When the wave reaches the end of the line, in general, there will be a reflected wave that travels back along the line in the opposite direction towards the source. Based on the TEs, using the TLM, the characteristic impedance could be represented by [14]:

![Fig. 2.1 Elementary components of a TL.](image-url)
\[ Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} \]

\[ , \quad (2.1) \]

where \( \omega \) is the angular frequency.

The main properties of transmission lines are:

1. Independent of the length of the line,
2. Independent of the termination of the line,
3. Not the impedance that a line itself possesses,
4. Determined only by the parameters of the line per unit length.

At high frequencies or low losses \( R \ll \omega L, G \ll \omega C \), \( Z_0 \) can be approximated from the binomial expansion:

\[ Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} \]

\[ = \frac{L}{C} \left( 1 + \frac{1}{2} \left( \frac{R}{j\omega L} - \frac{G}{j\omega C} \right) \right) \]

\[ = \frac{L}{C} \quad \text{Lossless (} R= G = 0 \text{).} \quad (2.2) \]

The propagation constant \( \gamma \) of an electromagnetic wave is a measure of the change undergone by the amplitude of the wave as it propagates in a given direction. The quantity being measured can be the voltage or current in a circuit or a field vector such as the electric field strength or the flux density. The propagation constant itself measures change per metre but is otherwise dimensionless. The relationship between the propagation constant and the primary constant is given by (2.3):
The propagation constant is a complex quantity, which is given by \( \gamma = \alpha + j \beta \), where \( \alpha \) is the attenuation constant and \( \beta \) is the phase constant.

The propagation constant is separated into two components that have very different effects on signals. The real part of the propagation constant is the attenuation constant, which causes the signal amplitude to decrease along the TL. The natural unit of the attenuation constant is Nepers/meter, but is often converted into dB/meter in microwave engineering.

The phase constant determines the sinusoidal amplitude/phase of the signal along a TL. In a lossless TL, the wave propagates as a perfect sine wave. For a TLM, the propagation constant can be determined from the primary line coefficients as given by [14]:

\[
\gamma = \sqrt{(R + j\omega L) * (G + j\omega C)}.
\]  

(2.3)

Hence,

\[
\alpha = \frac{R}{2} \sqrt{\frac{C}{L}} + \frac{G}{2} \sqrt{\frac{L}{C}} = \alpha_c + \alpha_d,
\]  

(2.5)

where

\[
\alpha_c = \frac{R}{2} \sqrt{\frac{C}{L}} \quad \text{(Conductor loss),}
\]  

(2.6)

\[
\alpha_d = \frac{G}{2} \sqrt{\frac{L}{C}} \quad \text{(Dielectric loss),}
\]  

(2.7)

\[
\beta = \omega \sqrt{LC}.
\]  

(2.8)

For a lossless TL, \( \alpha = 0, \gamma = j \beta \).
2.3 Review of the ML Theory

ML is a type of electrical TL and is used to convey microwave-frequency signals. It consists of a conducting strip separated from a ground plane by a dielectric layer known as the substrate. Microwave components such as antennas, couplers, filters, power dividers etc. can be formed from ML with the entire device fabricated as a pattern of metallization on the substrate [9, 14]. ML is much less expensive than the traditional waveguide technology, as well as being far lighter and more compact. By comparing with other TLs like wave guide, the drawbacks of the MLs are the generally lower power handling capacity and higher losses. Also, unlike waveguide, microstrip is not enclosed, and is therefore susceptible to the cross-talk and un-intentional radiation [39, 40].

The geometry of ML is shown in Fig. 2.2.

Fig. 2.2 Geometry of TL.

$W$ and $L_c$ are the width and length of the conductor, $T$ is the conductor thickness, $H$ and $\varepsilon_r$ are the height, and dielectric constant of the substrate.
2.3.1 Effective Relative Permittivity

The effective relative permittivity ($\varepsilon_{reff}$) is the effective dielectric constant between the constant of air and the relative dielectric constant of the substrate. In a copper conductor, the electric current generates the electric and magnetic fields. The propagation of the electrical field is in and around the ML, which is produced in the substrate and air. The effective dielectric constant is defined as the function of relative permittivity and the ratio of $W/H$, as given in (2.9), and (2.10) [9]:

$$\varepsilon_{reff} = \frac{\varepsilon_r + 1}{2} + \left[ \frac{\varepsilon_r - 1}{2} \right] \left[ (1 + \frac{12H}{W})^{-\frac{1}{2}} + 0.04(1 - \frac{W}{H})^2 \right] \quad (W/H \leq 1), \quad (2.9)$$

$$\varepsilon_{reff} = \frac{\varepsilon_r + 1}{2} + \left[ \frac{\varepsilon_r - 1}{2} \right] \left[ (1 + \frac{12H}{W})^{-\frac{1}{2}} \right] \quad (W/H > 1). \quad (2.10)$$

2.3.2 Characteristic Impedance

For a ML, $Z_0$ is a function of the relative permittivity and $W/H$ ratio, which can be represented by [9]:

$$Z_0 = \frac{60}{\varepsilon_{reff}^2} \ln \left( \frac{8H}{W} + \frac{0.25W}{H} \right) \quad (W/H \leq 1), \quad (2.11)$$

$$Z_0 = \frac{120\pi}{W} \frac{\varepsilon_{reff}^2}{\frac{W}{H} + 1.393 + 0.667 \ln \left( \frac{W}{H} + 1.444 \right)} \quad (W/H > 1). \quad (2.12)$$

In addition $W/H$ is defined in terms of $Z_0$ and $\varepsilon_r$ as:

$$\frac{W}{H} = \frac{8e^A}{\varepsilon_r e^{2A} - 2} \quad (W/H \leq 2), \quad (2.13)$$
\[
\frac{W}{H} = \frac{2}{\pi} \left\{ B - 1 - \ln(2B - 1) + \frac{\varepsilon_{r}^{-1}}{2\varepsilon_{r}} \left[ \ln(B - 1) + 0.39 - \frac{0.61}{\varepsilon_{r}} \right] \right\} \quad (W/H = 2), \tag{2.14}
\]

where
\[
A = \frac{Z_{0}}{60} \left( \frac{\varepsilon_{r}+1}{2} \right)^{1/2} + \frac{\varepsilon_{r}^{-1}}{\varepsilon_{r}+1} (0.233 + 0.11 / \varepsilon_{r}) \quad \text{and} \quad B = \frac{377 \pi}{2Z_{0}\sqrt{\varepsilon_{r}}}, \tag{2.15}
\]

\[
\lambda_{g} = \frac{c}{f\sqrt{\varepsilon_{reff}}} \quad \text{and} \quad \theta = \beta L = \frac{2\pi L}{\lambda_{g}}, \tag{2.16}
\]

where \( \lambda_{g} \) is the wave length in substrate.

### 2.3.3 Loss Investigation of a ML

Due to the characteristics of the MLs, the loss cannot be ignored particularly when an ordinary low cost PCB FR4 substrate is used. The loss tangent of PCB FR4 is 0.025 which is higher than that of Duroid 5870 (0.0025) at microwave frequency range. The rest of this section will analyse the loss of MLs that can equally be applied to other materials in future designs especially using PCB FR4 substrate.

The major losses due to the MLs are (i) conductor loss \( \alpha_{c} \), (ii) dielectric loss \( \alpha_{d} \), and (iii) radiation loss \( \alpha_{r} \).

**Conductor loss** - The resistance of any conductor is not zero. So when current is passed through the wire, the energy is lost in the form of heat. At high frequencies, the conductor losses are generally due to the skin effect. When a DC voltage (or current) is applied the distribution of electron movement is fairly uniform. When AC is applied, the flux density at the centre of the wire is greater than at the outer edge, thus the reactance is also greater. The current reduces with inversing the resistance. In other words, when AC is applied the current will flow faster on the outer edge of the conductor than through the centre [42]. For a ML, the surface resistance \( R_{s} \) is given by [43]:

\[
\lambda_{g} = \frac{c}{f\sqrt{\varepsilon_{reff}}} \quad \text{and} \quad \theta = \beta L = \frac{2\pi L}{\lambda_{g}}, \tag{2.16}
\]
where $\rho$ is the bulk resistivity and $\delta$ is the skin depth defined by:

$$\delta = \frac{\rho}{\sqrt{\mu \pi f} \text{cm}},$$

(2.18) where $\mu$ is the absolute magnetic permeability of the conductor, and $f$ is the working frequency.

The conductor loss is therefore defined as:

$$\alpha_c = 8.86 * \frac{R_c}{Z_0} W.$$  

(2.19)

(ii) Dielectric loss - Different dielectric substrate material creates a different power loss at microwave frequencies. The loss in the dielectric is due to a high resistance and the movement of the dielectric molecules in the substrate. The movement of molecules in the dielectric substrate will contribute losses in the form of heat. The dielectric loss is defined by:

$$\alpha_d = 27.3 * q * \varepsilon_r * \frac{\tan \delta}{\varepsilon_{ref} \varepsilon_g},$$

(2.20) where $q = \frac{\varepsilon_{ref} - 1}{\varepsilon_r - 1}.$

(iii) Radiation loss – The energy radiated is called radiation loss which depends on dielectric material conductor spacing and length of TL. If separation between conductors in
a metallic TL is appreciable fraction of wavelength, the electrostatic and electromagnetic fields that surround the conductor cause the line to transfer energy to nearby conductive material. Radiation losses can stem from numerous factors, including the type of dielectric material, its thickness, the shapes of TL structures in a microstrip circuit and also frequency. Radiation loss can significantly impact performance, resulting in increased insertion loss, changes in signal phase, and shifts in resonant frequency in certain microstrip circuits, such as filters and couplers. The shape of TL discontinuities could influence the amount of radiation loss with sharper edges on junctions cause higher radiation loss [9]. Substrate with low dielectric constants has often been used in microwave designs due to the low cost and versatility. However, less of the conducted EM energy is concentrated in the substrate and metal conductor which lead to higher radiation effects. The thickness of PCB material also impact the amount of radiation loss at higher frequency that it can be reduced by using thinner dielectric substrate for lower dielectric constant material and also higher dielectric constant material as well [9], [13].

Finally, the total loss is given by:

\[ \alpha_t = \alpha_c + \alpha_d + \alpha_r \]  

(2.21)

2.3.4 Review of S Parameters

This section introduces the basic concept of S parameters and the derivation of equations for unequal source and load impedance. This will be used in the rest of this thesis for patch antenna and power amplifier design and analysis. S parameters describe the input-output relationship between terminals in an electrical system and always a function of the frequency. For instance, for a two port network, \( S_{mn} \) represents the power transferred from
Port $n$ to Port $m$. A block diagram of a two port system with the unequal source and load impedance is depicted in Fig. 2.3:

\
E_1, R_{o1} (E_2, R_{o2}) is the source (load) power and its internal resistance. V_1, I_1 (V_2, I_2) are the voltage and current across the source (load). V_{i1}, I_{i1} (V_{i2}, I_{i2}) are the input voltage and current flow into the two port network from the source (load) port, and the V_{r1}, I_{r1} (V_{r2}, I_{r2}) are the reflected voltage and current from the two port network. If considering an incident power wave $a_1 (a_2)$ from source port (load port), it will lead to the reflected waves which exciting at both source port $b_1$ and load port $b_2$. The source (load) port is represented by port 1 (port 2) in the rest of this chapter.

\[ S_{11} = \frac{b_1}{a_1} \bigg|_{a_2=0} \] represents the reflection coefficient at port 1 with port 2 terminated with a matched load.

\[ S_{21} = \frac{b_2}{a_1} \bigg|_{a_2=0} \] represents the transmission coefficient from port 1 to port 2 with port 2 terminated with a matched load.

The S parameters are defined as:
\[
S_{11} = \frac{b_{11}}{a_1} |_{a_2=0} = \frac{i_{R1}\sqrt{R_{01}}}{i_{11}\sqrt{R_{01}}} = \frac{i_{R1}}{i_{11}} |_{i_{12}=0} = \frac{V_{R1}}{V_{11}}. \tag{2.22}
\]

So

\[
S_{11} = \frac{Z_{in1}-R_{01}}{Z_{in1}+R_{01}}, \tag{2.23}
\]

similarly

\[
S_{22} = \frac{b_{22}}{a_2} |_{a_1=0} = \frac{Z_{in2}-R_{02}}{Z_{in2}+R_{02}}, \tag{2.24}
\]

where \(Z_{in1}\), and \(Z_{in2}\) are the input impedance flowing into the two port network when \(E_1\), and \(E_2 = 0\).

\[
S_{21} = \frac{b_{21}}{a_1} |_{a_2=0} = \frac{i_{R2}\sqrt{R_{02}}}{i_{11}\sqrt{R_{01}}} |_{i_{12} = 0}. \tag{2.25}
\]

As \(I_2 = I_{12} - I_{R2}\) and \(I_{12} = 0\), \(I_2 = -I_{R2}\).

So

\[
S_{21} = \frac{-I_{2}\sqrt{R_{02}}}{\sqrt{R_{01}}E_1} = \frac{-2I_{2}\sqrt{R_{01}}\sqrt{R_{02}}}{E_1}. \tag{2.26}
\]

\[
S_{12} = \frac{-2I_{1}\sqrt{R_{01}}\sqrt{R_{02}}}{E_2}. \tag{2.27}
\]
2.4 Characteristics of Microstrip Patch Antennas

Microstrip patch antennas are the most common form of printed antennas. They are popular for their low profile, geometry, low cost and easy to integrate with RF circuit functions. A microstrip device in the simplest form is a layered structure with two parallel conductors separated by a dielectric substrate. The lower conductor acts as a ground plane. The device becomes a radiating microstrip antenna when the upper conductor is a patch with a length that is an appreciable fraction of a wavelength, approximately half a wavelength [9]. The width of the patch controls the total input impedance which will be reduced with the increasing width [13]. The width further controls the radiation pattern, which is widely used in telecommunication field. The microstrip patch antenna can be designed as the radiation element and also as the optimum load of an active device which make the whole circuit compact. As in airplane and space industry requirement, patch antennas could be designed to be operated in harsh environment [44]. The following section will present the effects of different shapes of radiation elements and feed methods on the performance of microstrip antennas.

2.4.1 Radiation Elements

There are different conductor shapes proposed and investigated for a microstrip patch antenna. The schematics of these radiation elements are shown in Fig. 2.4 [45].
Fig. 2.4 The schematic of patch shapes.

The rectangular and square patches in Fig. 2.4(a) and Fig. 2.4(b) are mostly used, which can be easily to be modelled and analysed [46-48]. The square patch also could be used to obtain a circular polarized radiation antenna [49, 50]. The circular and elliptical patches (Figs. 2.4(c) and (d) [11, 51-53]) are slightly smaller than the corresponding rectangular patch with lower gain and bandwidth. The triangular and dish patches, Figs. 2.4(e) and (f), are smaller than corresponding rectangular and circular patch antennas with lower bandwidth and gain [45, 54]. Dual polarized radiation patterns can be produced using these geometries but with lower bandwidth and gain [54, 55]. Due to the lack of symmetry of the structure, higher cross polarization can be generated [45, 56]. An annular patch is demonstrated in Fig. 2.4(g) which has the smallest conductor shape but decreased bandwidth, gain, and also the symmetry issue as circular geometry patch [45]. Exciting the lowest order model and obtain a superior impedance bandwidth are not a simple process. Thus, the noncontact excitation form is normally used [57, 58]. Other shapes of microstrip
patches are well investigated as H, E shapes [59-62] due to their low profiles and a compact configuration. However, the bandwidths of such antennas are not wide enough for some applications including radar and broadband communications [63-65]. To compensate these drawbacks, new structures will be introduced in the following sections.

2.4.2 Different Feed Methods of Microstrip Patch Antenna

A feed line via direct or indirect contact is used to excite the antenna. Here six typical feed methods are presented, which are edge fed, inset fed, probe fed, coupled fed, proximity coupled, and aperture coupled. The first three types are classified as direct contact and the rest are defined as indirect contact.

(i) Edge fed

![Fig. 2.5 Schematic of edge fed microstrip patch antenna.](image)

The edge fed technique is one of the original feed methods for the microstrip patch antenna where a ML is in direct contact with patch as shown in Fig. 2.5. The width and length of patch is \( W_p \) and \( L_p \), respectively. The input impedance can be easily matched by changing
the width and length of the feed using a quarter wave matching or other matching techniques [66, 67]. It is simple to fabricate this type of antenna because the feed and patch are in the same layer. Planar arrays could also be developed with higher gains [21, 68]. Transmission line models can be utilized to model the edge fed microstrip patch antenna, which will be covered in Chapter 3. Using large and thick substrate with a low value of dielectric constant could increase the bandwidth. However the surface wave efficiency will be reduced when using thick substrate with a high dielectric constant material [45, 54]. In addition, modelling of the performance of this type of antenna is not straightforward. The bandwidth and the gain of the microstrip patch antenna with this method are relatively narrow and low [14, 69].

(ii) **Inset fed**

![Fig. 2.6 Schematic of an inset fed microstrip patch antenna.](image)

At the edge of the normal edge fed microstrip patch antenna, the input impedance is high. The impedance could be reduced by modifying the feed, where the current is low at the
ends of a half-wave patch and increasing in magnitude toward the centre. Also the voltage will decrease in the same amount when the feed moves to the centre of the patch. Hence the input impedance could be reduced if the feed line is closer to the centre of the patch with impedance matching achieved by changing the position of feed line [70-72]. The advantage and drawbacks of this method are similar to the edge fed antenna.

(iii) **Probe fed**

The probe fed method for a microstrip patch antenna was proposed in 1970s, where a probe extends from the feed port at the ground plane and is connected to the patch as shown in Fig. 2.7.

![Fig. 2.7 Schematic of probe fed microstrip patch antenna.](image)

The pin of the feeding probe is usually a coaxial line so it also called the coaxial feed. The position of the feed controls the input impedance [73-75], which has small value at the centre position and large value at the edge. The key advantage of this feed method is the independent optimization of each layer. This is due to the feed network being isolated by the ground plane, and the phase shifter and filter functions could be integrated with the feed network [48, 76, 77]. Because of direct contact between the feed and patch, higher
efficiency and a low spurious radiation are obtained. Problems of this feed method are similar to the edge fed method that a relatively wide bandwidth is still difficult to obtain.

(iv) Proximity coupled

In order to overcome the disadvantage of direct contact patch antennas, noncontact excitation methods are used such proximity coupled patch antennas and aperture coupled patch antennas [78, 79]. The proximity coupled patch antennas are shown in Fig. 2.8.

![Fig. 2.8 Schematic of proximity coupled patch antenna.](image)

This proximity coupled patch antenna consists of two parts where a substrate is located at the centre of a microstrip feed line and a ground plane at the base. Above the feed line there is another substrate with a radiating patch at the top. The power from the feed is coupled to the patch by means of electromagnetic radiation, thus it is also called the electromagnetic coupled patch antenna. Compared with the direct contact methods, which are predominantly inductive, the indirect contact of the proximity couple mechanism is
capacitive in nature. The important effect of this method is on the impedance bandwidth. The bandwidth of a proximity coupled microstrip patch antenna is inherently greater than that of the direct contact method patch antennas. This is because the substrate thickness of the direct contact structure is limited by the inductive coupling feature. Full wave EM analysis can be used to develop the proximity coupled patch antenna due to the lack of current discontinuity between the feed and radiating patch. However, because of the efficiency of power coupling, feed and radiating element are not fully independent, thus leading to creation of spurious feed radiation. From practical fabrication point of view, due to the multi-layer structure, the alignment procedure needs to be accurate in order to ensure accuracy in results [45].

(v) **Aperture coupled**

The structure of ACMA, which is a noncontact excitation structure, is illustrated in Fig. 2.9 [80].

![Fig. 2.9 Schematic of ACMA.](image)
Unlike the proximity coupled patch, the feed and radiating elements of the aperture coupled structure are separated by a ground plane with the slot etched in. Comparing it with direct contact mechanisms like edge fed and probe fed structures, the feed and radiating elements of the ACMA can be optimized independently; no vertical interconnects are required, and also the spurious radiation is low. The ACMA has more design parameters than other types and therefore more flexibility for designers. The total input impedance is affected by the dimension of the patch, slot and substrate. The gain of the antenna will be influenced by the loss tangent and also height of substrate [9]. Unlike the direct contact fed methods, there are no abrupt current discontinuities. Therefore, relatively simple, TL model and full wave analysis are easy to be developed. Also due to its complex structure, it is easy to enhance the bandwidth up to 10% – 15% with a single layer, and up to 30% - 50% with a stacked patch configuration [81]. Other methods developed to optimise or increase the bandwidth, which produces dual or circular polarization for an ACMA were demonstrated in [24, 82, 83]. However, there are also problems with the ACMA such as alignment and multi-layer issues. Gap between layers of dielectric can change the impedance nature of this antenna. The next chapter will investigate the equivalent circuit of the ACMA.

2.5 Summary

This chapter introduced the basic concept of TL that was proposed to deliver power from the source to the load. The equations for the characteristic impedance and the propagation constant were shown using primary parameters. The ML theory also was reviewed. Equations of the effective dielectric constant and the characteristic impedance were given.
which would be utilized in the future microstrip patch antenna analysis. A two port network with different source and load impedance was proposed for the analysis of S parameters which were derived to determine power reflected back and power passing through the circuit. Finally a number of microstrip patch antennas with different patch shapes and feed methods were presented. Advantage and draw backs of these antennas were reviewed and compared.
Chapter 3 Investigation of Aperture Coupled Microstrip Antenna using Transmission Line Model

3.1 Introduction

There is a requirement for light, low cost, wide bandwidth, multi-band, and high gain microwave antennas in applications such as automatic road tolling, ‘on the move’ satellite communication services and high-capacity data networks [21, 22, 64, 84-88]. These requirements can often be satisfied by an aperture coupled patch antenna [9, 89-92], see Fig. 3.1, and can also been used as a load with a high efficiency PA in the AIA design. $W_p$, $L_p (W_s, L_s)$ are the width and length of patch (slot). $W_f$ and $L_{os}$ are the width of feed line and length of open stub.

![Fig. 3.1 Geometry of an ACMA.](image)

An ACMA normally consists of a radiating patch and a microstrip feed line. A ground plane is used to separate the antenna substrate and the feed substrate with the slot etched in the ground plane. The shape of the slot is normally rectangular to improve coupling [14,
21, 78, 93,94]. Such an antenna has many parameters that could be exploited to improve its performance. In order to simplify the design procedure and to readily optimize the dimensions of an ACMA, the transmission line model analysis is still the best option for the speed and simplicity [69].

To obtain a wide bandwidth and a high gain, different substrate materials as well as a range of the stub length and size of coupling slot have been investigated [95-99]. Dual polarized antennas could be obtained by two orthogonal feeds with no overlapping slots and a rectangular patch element [78, 100-102]. To achieve circular polarization, a 90 degree phase offset hybrid coupler could be used but at the cost of limited isolation and polarization purity [48, 89, 103,104]. To solve this problem, a cross slot solution was suggested by [105] with different arrangement for the of feed lines [95], which resulted in a very wide bandwidth of return loss and also a 3 dB axial ratio up to 50% [81]. Due to flexible features of the aperture coupled patch antenna, sufficient space is allocated for arrays and feed networks to compensate for the limited power radiation by the single element [16, 106, 107]. It is not that simple to model the ACMA due to its complex structure. The cavity model initially developed in [80] was not rigorous enough, thus the development of full wave analysis reported in [8]. Pozar also derived the reciprocity theorem [108] to eliminate complex modelling of the feed and a stub applied to the mutual coupling between radiation elements for the array design. In this chapter, the equivalent circuits of the ACMA are reviewed and investigated with the aim of verifying and simplifying the model adopted for this antenna.

The equivalent circuit of the antenna is depicted in Fig. 3.2 where $G$ and $C$ are the parallel conductance and capacitance of the radiation of the patch. $Z_{0p}$ and $\theta_p$ are the characteristic impedance and electrical length of the patch, respectively. $Z_{0s}$ and $\theta_s$ are the characteristic
impedance and electrical length of the slot, respectively. $Z_0$ and $\theta$ are the characteristic impedance and electrical length of the open stub, respectively, and $n_p$ and $n_f$ are the coupling ratios between slot/patch and the feed/slot, respectively.

![Equivalent circuit of an ACMA](image)

To investigate $n_f$, comparisons are carried out with previous works that used the spectral domain analysis and the spatial solutions [108-111]. The analysis carried out are rigorous and elegant but the dimensions of the physical model and values of the circuit elements of the equivalent circuit are interdependent thus making the design still more challenging. The $n_p$ is a function of the width of the patch and length of the slot [112]. The patch is modelled as a TLM with the power radiation at the edge. The analysis of the equivalent circuit will be given in the following section.
3.2 Analysis of the Equivalent Circuit of the Radiation Patch

TLM is the simplest to be adopted for analysing this type of antenna compared to the cavity and full wave analysis [9]. Although TLM is less accurate and more difficult to model coupling [9] it gives a good physical insight, which will be adopted in investigation and design of the ACMA. This section will outline the TLM analysis of the radiation patch. A rectangular patch, which is straightforward to analyse and the most accurate for thin substrates, is adopted [45]. Because of the finite dimension of the patch, the field at the edge undergoes fringing. A rectangular microstrip antenna could be represented by an array of two radiation slots with the length $\Delta L$ and height $H$, separated by a transmission line with a distance $L$, see in Fig. 3.3:

![Diagram of radiation patch and fringing field](image)

(a)

(b)

Fig. 3.3 Structure of radiation patch and fringing field (a) top view (b) side view.
The amount of the fringing field is a function of the patch length [9]. Also the substrate affects the fringing field, see Fig. 3.3(b), which is a non homogeneous line of two dielectrics [80]. Because most of the electric field lines reside in the substrate and parts are in the air, an effective dielectric constant $\varepsilon_{\text{reff}}$ is introduced for calculating the wave propagation. The effective dielectric constant has values between that of the air and the dielectric constant of substrate and is a function of frequency [14]. As frequency increases, most of the fields are concentrated in the substrate. Hence, the effective dielectric constant approaches the value of the dielectric constant of the substrate. For low frequency applications, the value of effective dielectric constant is referred to as the static value, see (2.10) [9]. Because of the fringing effects, the electrical length of the patch is greater than the physical length, which is extended by $\Delta L$ on each side. The length extension is given by (3.1) as a function of $W/H$ and the effective dielectric constant $\varepsilon_{\text{reff}}$ [9]:

$$\Delta L = 0.412 H \left( \frac{\varepsilon_{\text{reff}} + 0.3}{\varepsilon_{\text{reff}} - 0.258} \right)^{\frac{W}{H} + 0.264} \left( \frac{W}{H} + 0.8 \right).$$

(3.1)

Thus the effective length of the patch is defined as:

$$L_{\text{eff}} = L + 2\Delta L.$$  

(3.2)

Based on the derived equations, a simplified design procedure for the radiation patch is presented below.

(i) The width of the patch for effective radiation is defined:

$$W = \frac{c}{2f} \sqrt{\frac{2}{\varepsilon_r + 1}},$$

(3.3)

where $c$ is the free space speed of light and $f$ is the working frequency.
(ii) Obtain the extension length of patch $\Delta L$ using (3.1).

(iii) Calculate the physical length of the patch from (3.2), where $L_{\text{eff}} = \frac{\lambda}{2}$, $\lambda$ is the wavelength of propagated wave:

$$L = \frac{c}{2f\sqrt{\varepsilon_{\text{eff}}}} - 2\Delta L. \quad (3.4)$$

The fringing fields store the energy in $C$ which is grounded at the edge of the patch. The radiation power at each slot is represented by the conductance $G_1$ and the power losses due to the coupling between two slots are indicated by the conductance $G_{12}$. The equivalent circuit is illustrated in Fig. 3.4.

![Equivalent circuit of radiation patch.](image)

$G_{12}$ is seen as parallel with each side of the patch and therefore Fig. 3.4 can be simplified to Fig. 3.5.
Where $G = G_1 + G_{12}$. So at each slot, $G_1$ for the finite width $W$ and $C$ is represented by the susceptance $B$ as given by [9]:

$$G_1 = \frac{W}{120 \lambda_0} \left[ 1 - \frac{1}{24} (k_0 H)^2 \right] \frac{H}{\lambda_0} < 0.1, \quad (3.5)$$

$$B = \frac{W}{120 \lambda_0} \left[ 1 - 0.636 \ln(k_0 H) \right] \frac{H}{\lambda_0} < 0.1, \quad (3.6)$$

where $\lambda_0$ is the signal wavelength in the air, and $k_0$ is the wave propagation constant in air.

By using the field expression derived by the cavity model, $G_1$ and $G_{12}$ could also be expressed as [9]:

$$G_1 = \frac{1}{120 \pi^2} \int_0^\pi \left( \sin \left( k_0 \frac{W}{2} \cos \theta \right) \right)^2 \left( \sin \theta \right)^3 d\theta,$$

$$G_{12} = \frac{1}{120 \pi^2} \int_0^\pi \left( \sin \left( k_0 \frac{W}{2} \cos \theta \right) \right)^2 \left( \sin \theta \right)^3 \cdot J_0 \left( k_0 L \sin \theta \right) d\theta, \quad (3.8)$$

where $J_0$ is the Bessel’s function of first kind of order zero.
The edge slots are connected by a TL of the characteristic impedance $Z_0$ given by:

$$Z_0 = \begin{cases} \frac{60}{\sqrt{\varepsilon_{reff}}} \ln \left( \frac{8H}{W} + \frac{W}{4H} \right) \frac{W}{H} \leq 1, \\ 120\pi \sqrt{\varepsilon_{reff}} \left[ \frac{W}{H} + 1.393 + 0.667 \ln \left( \frac{W}{H} + 1.444 \right) \right] \frac{W}{H} > 1. \end{cases}$$  \hspace{1cm} (3.9)

The normalized radiation pattern is approximately given by [14]:

$$E_\theta = \frac{\sin \frac{kW}{2} \sin \theta \sin \phi}{kW \sin \theta \sin \phi} \cos \left( \frac{kL}{2} \sin \theta \cos \phi \right) \cos \phi,$$

$$E_\phi = -\frac{\sin \frac{kW}{2} \sin \theta \sin \phi}{kW \sin \theta \sin \phi} \cos \left( \frac{kL}{2} \sin \theta \cos \phi \right) \cos \theta \sin \phi,$$  \hspace{1cm} (3.10) (3.11)

where $k = 2\pi/\lambda$, and the magnitude of the field is given by:

$$f(\theta, \phi) = \sqrt{E_\theta^2 + E_\phi^2}. \hspace{1cm} (3.12)$$

### 3.3 Review of Slot Lines

The slot line (SL) was proposed by Cohn in 1968 [113], which is a planar transmission structure. Cohn employed the transverse resonance approach, which converses SL into a waveguide configuration. The structure of SL is depicted in Fig. 3.6, which shows that a slot is etched in the metallization on one side of a dielectric substrate. This allows the SL to be included into microstrip circuits to produce a range of microwave subsystems.
In SL, a non-transverse electromagnetic (TEM) wave, which is almost transverse electric in nature, [113] propagates along SL with the major electric field oriented across the slot. The field distribution is shown in Fig. 3.7.

There are a number of mathematical methods that have been used to analyse SLs including the approximate analysis, transverse resonance approach [113], Galerkin’s method in Fourier transform domain [114-117], and finite different time domain technique [118].
However, these methods do not lead to any closed form expression for $Z_0$ and wavelength, which could be used in the circuit analysis and design. Based on Cohn’s analysis, the solution was presented by [117] and is given below.

The characteristic impedance for SL for two ranges of $\varepsilon_r$ is given by (3.13) and (3.14) where $W_s$ is the width of the slot and $h$ is the height of the substrate.

For $0.0015 \leq \frac{W_s}{\lambda_0} \leq 0.075$ and $2.22 \leq \varepsilon_r \leq 3.8$,

$$Z_{0s} = 60 + 3.69 \sin \left[ \frac{(\varepsilon_r - 2.22)\pi}{2.36} \right] + 133.5 \ln(10\varepsilon_r) \sqrt{\frac{W_s}{\lambda_0}}$$

$$+ 2.81[1 - 0.011\varepsilon_r(4.48 + \ln(\varepsilon_r))] \left( \frac{W_s}{h} \right) \ln \left( \frac{100h}{\lambda_0} \right)$$

$$+ 131.1(1.028 - L_s(\varepsilon_r)) \sqrt{\frac{h}{\lambda_0}}$$

$$+ 12.48(1 + 0.18 \ln(\varepsilon_r)) \frac{W_s}{h \sqrt{\varepsilon_r - 2.06} + 0.85 \left( \frac{W_s}{h} \right)^2} \quad (3.13)$$

For $0.0015 \leq \frac{W_s}{\lambda_0} \leq 0.075$ and $3.8 \leq \varepsilon_r \leq 9.8$,
\[
Z_{0s} = 73.6 - 2.15\varepsilon_r + (638.9 - 31.37\varepsilon_r) \left(\frac{W_s}{\lambda_0}\right)^{0.6}
\]

\[
+ \left(36.23\sqrt{\varepsilon_r^2 + 41 - 225}\right) \frac{W_s}{h} + 0.876\varepsilon_r
\]

\[
+ 0.51(\varepsilon_r + 2.12) \left(\frac{W_s}{h}\right) \ln\left(\frac{100h}{\lambda_0}\right)
\]

\[
- 0.753 \frac{h}{W_s} \varepsilon_r
\]

(3.14)

The above equations are used to determine \(Z_{0s}\).
Fig. 3.8 Frequency response of characteristic impedance for substrates PCB FR4, Duroid 5870 and Duroid 6010 with height: (a) 1.575 mm, and (b) 0.7875 mm.

From the results shown in Fig. 3.8, the characteristic impedances are proportional to the frequency for both heights, and at one fixed frequency point, the characteristic impedance is inversely proportional with the dielectric constant value.

Closed form expressions for the slot wavelength, which is also a function of effective dielectric constant \( \frac{\lambda_s}{\lambda_0} = \frac{1}{\sqrt{\varepsilon_{reff}}} \), are given in (3.15) and (3.16) and the frequency response is shown in Fig. 3.9.
For $0.0015 \leq \frac{W_s}{\lambda_0} \leq 0.075$ and $2.22 \leq \varepsilon_r \leq 3.8$,

$$\frac{\lambda_s}{\lambda_0} = 1.045 - 0.365 \ln(\varepsilon_r) + \frac{6.3 \left( \frac{W_s}{h} \right) \varepsilon_r^{0.945}}{238.64 + \frac{100W_s}{h}}$$

$$- \left[ 0.148 - \frac{8.81(\varepsilon_r + 0.95)}{100\varepsilon_r} L_s \left( \frac{h}{\lambda_0} \right) \right].$$  \hspace{1cm} (3.15)

For $0.0015 \leq \frac{W_s}{\lambda_0} \leq 0.075$ and $3.8 \leq \varepsilon_r \leq 9.8$,

$$\frac{\lambda_s}{\lambda_0} = 0.9217 - 0.277 \ln(\varepsilon_r) + 0.0322 \left( \frac{W_s}{h} \right) \left[ \frac{\varepsilon_r}{\frac{W_s}{h} + 0.435} \right]^{\frac{1}{2}}$$

$$- 0.01 \ln \left( \frac{h}{\lambda_0} \right) \begin{bmatrix} 4.6 \end{bmatrix}$$

$$- \frac{3.65}{\varepsilon_r^2 \left[ \frac{W_s}{\lambda_0} \left( 9.06 - 100 \frac{W_s}{\lambda_0} \right) \right]}.$$  \hspace{1cm} (3.16)

This wavelength ratio within specified slot line width and dielectric constant range are decreasing in terms of frequency and also with the dielectric constant of the substrate for a fixed frequency.
Fig. 3.9 Frequency response of wave length for PCB FR4, Duroid 5870 and Duroid 6010 with different height of substrate: (a) 1.575 mm, and (b) 0.7875 mm.
3.4 Investigation of Microstrip/Slot Structure and Coupling Ratio between Microstrip Feed and Slot $n_f$

A SL fed by a ML is shown in Fig. 3.10 where the two lines are oriented at right angle to each other to obtain tight coupling. This structure is investigated by different researchers and the most frequent used is Galerkin’s method in the spectral domain. From this analysis, two models are used which are quasi microstrip model and quasi slot line model. The electric fields are shown in Fig. 3.11.

![Fig. 3.10 Physical structure of microstrip/slot structure.](image)

![Electric field and Microstrip line](image)

(a)
In Fig. 3.11(a) this field propagates like a ML, which has even symmetry and called even model. The model transferred in Fig. 3.11(b) behaves like SL which is called the odd model. The equivalent circuit of a microstrip/slot structure is shown in Fig. 3.12.
In the equivalent circuit the transformer (with $n_f$) models the coupling between SL and the microstrip feed line, while $Z_s$ is the SL input impedance and $Z$ is the impedance produced on the microstrip feed line. To investigate $n_f$, Knorr [119] derived equation (3.17) for $n_f$ by assuming that the SL is infinitely long in one direction and extends a quarter-wave length beyond the strip line in the opposite direction. Also the microstrip feed line is infinitely long in one direction and extends a quarter-wave length beyond the SL in the other direction.

$$n_f = \cos\left(\frac{2\pi h u}{\lambda_0}\right) - \cot(\theta) \sin\left(\frac{2\pi h u}{\lambda_0}\right),$$

(3.17)

where $\nu = \sqrt{\varepsilon_{rs} - 1}$, $u = \sqrt{\varepsilon_{rm} - \varepsilon_{rs}}$, $q = \frac{2\pi h u}{\lambda_0} + \tan^{-1}\left(\frac{u}{\nu}\right)$,

$\varepsilon_{rm}$ is the effective dielectric constant of the microstrip line, and $\varepsilon_{rs}$ is the effective dielectric constant of slot line.

Das [120] derived the following approximate closed form equation for the turn ratio shown in (3.18), in terms of the microstrip and SL parameters for infinitely long slot and MLs.

$$n_{FD} = \left(\frac{I_0(\frac{\beta_s W_s}{2})}{I_0(\frac{\beta_m W_m}{2})} \frac{\beta_m^2 k_2 \varepsilon_r}{k_2 \varepsilon_r \cos(h k_1) - k_1 \sin(h k_1)} + \frac{\beta_m^2 k_1}{k_1 \cos(h k_1) + k_2 \sin(h k_1)}\right),$$

(3.18)

where $n_{FD}$ is turns ratio $n_f$ derived by Das. $\beta_s = k_0 \varepsilon_{rs}$, $\beta_m = k_0 \sqrt{\varepsilon_{rm}}$, $k_1 = k_0 \sqrt{|\varepsilon_r - \varepsilon_{rs} - \varepsilon_{rm}|}$, $k_2 = k_0 \sqrt{|\varepsilon_{rs} + \varepsilon_{rm} - 1|}$. 
Both equations are plotted in Fig. 3.13 for a range of frequently used substrates in the frequency range 1 to 5 GHz.

(a)

(b)
The frequency response of $n_f$ predicted by Knorr and Das decreases gradually with frequency and the value of the dielectric constant of the substrate. For the same frequency and substrate conditions, the turn ratio based on Knorr’s derivation is lower than that predicted by Das. Himdi[121], and Jaisson[112] derived equations for $n_f$ in terms of substrate and finite slot dimensions. Himdi modelled the slot as a cavity consisting of four magnetic and two electric walls in deriving the formula of the turn ratio shown in (3.19), where $k_s \left( k_s = \frac{2\pi}{\lambda_s} \right)$ is the propagation parameter in the slot line.

$$n_{fH} = \frac{2(\cos(k_s\frac{w_f}{2}) - \cos(k_s\frac{t}{2}))}{k_s \sin(k_s\frac{t}{2})/W_f h},$$  \hspace{1cm} (3.19)$$

where $n_{fH}$ is turns ratio $n_f$ derived by Himdi.
Jaisson simplified Pozar’s piecewise \([108]\) sinusoidal function for the usual condition that the design frequency is below the resonant frequency of the slot. Then using Taylor’s series \([122, 123]\) the derived equation for the turns ratios is given by:

\[
n_{ff} = \frac{2G(w) - G(w+l) - G(w-l)}{2\pi w l},
\]

where \(n_{ff}\) is turns ratio \(n_f\) derived by Jaisson.

\[G(x) = (1 - x^2) \times (\tan^{-1}x) + x \times (\ln(1 + x^2))\] and \(w = \frac{W_f}{2h} \& l = \frac{L_s}{2h}\).

This coupling ratio in terms of slot length (2 GHz) for PCB FR4, Duroid5870 and Duroid 6010 is plotted in Fig. 3.14.

Fig. 3.14 \(n_f\) as a function of slot length for Jaisson and Himdi equations using PCB FR4, Duroid 5870 and Duroid 6010.
These results are not in good agreement. Based on Himdi’s derivations, $n_f$ is proportional to the slot length and tend to a constant value when the slot length is greater than 10 mm. However, substrates with different dielectric constants will affect $n_f$. Jaisson’ results also tend to a constant when the slot length is greater than 10 mm but the substrate effects are small. As the derived equations do not agree, it is decided to model the above structure using the $S_{21}$ and $S_{11}$in terms of slot length. Then the predicted results for $n_f$ are compared to measured S parameters as given in the next section.

3.5 A Novel Method to Determine the Coupling Ratio of Feed/Slot and Slot/Patch using the S Parameter

As discussed in the analysis from the last section, Knorr and Das derived equations for $n_f$ for an infinitely long SL showing that $n_f < 1$. Bhattacharyya [124] used the full wave analysis to obtain integral equations to plot $n_f$ as a function of the SL length and height of the substrate. It was shown $n_f$ increases with the SL length and decreases with the substrate thickness, but does not change much with the SL width. Bhattacharyya [110] also used the spectral domain analysis to derive complex equations computed numerically to obtain a matched ACMA. Himdi and Jaisson derived different equations for $n_f$ (and similarly for $n_p$), however it was found that the equations did not agree with each other and the value of $n_f > 1$ as the SL length increased. Hence in this section $n_f$ and $n_p$ are investigated by simulation and practical measurements.
3.5.1 Determine Turns Ratio $n_f$ using $S_{21}$ Parameter

To obtain $n_f$ it is first necessary to determine $Z$ from the $S_{21}$ parameter as shown in Fig. 3.15. In Fig. 3.16(a), the SL is fed by a 50 Ω microstrip feed line of length $L_1+L_2$ and to calibrate for measurement errors produced by the length $L_1+L_2$ a 50 Ω calibration line of the same length is used as in Fig. 3.16(b).

![Fig. 3.15 Equivalent impedance of slot after coupling into microstrip feed line.](image)

![Fig. 3.16 Geometries of: (a) feed and slot lines, and (b) calibration line.](image)
Fig. 3.17 Signal flow graphs: (a) the feed line with coupling slot effects, and (b) the calibration line.

The impedance of the ports is 50 Ω and the signal flow graphs of the two structures in terms of S parameters are shown in Fig. 3.17. In Fig. 3.17(a), $S_{21L1}$, $S_{21L2}$ are the transmission parameters for $L_1$ and $L_2$ of the microstrip feed line, respectively. $Z$ is modelled by a two port network defined by $S_{11Z}$, $S_{22Z}$, $S_{21Z}$, and $S_{12Z}$. In Fig. 3.17(b) $S_{21L1}$ and $S_{21L2}$ are the transmission parameters of the microstrip calibration line. Equations (3.21) and (3.22) are obtained from the two signal flow graphs where $S_{21T}$ is the transmission parameter between ports 1 and 2 as in Fig. 3.17(a) and $S_{21C}$ between ports 1 and 2 as in Fig. 3.17(b).
\[ S_{21T} = S_{21L1} \ast S_{21Z} \ast S_{21L2}. \]  
\[ (3.21) \]

\[ S_{21C} = S_{21L1} \ast S_{21L2}. \]  
\[ (3.22) \]

(3.23) and (3.24) are used to determine \( S_{21Z} \) and \( Z \) by means of practical measurements and simulation.

\[ S_{21Z} = \frac{S_{21T}}{S_{21C}}. \]  
\[ (3.23) \]

\[ Z = \frac{2Z_0 - 2Z_0 S_{21Z}}{S_{21Z}}. \]  
\[ (3.24) \]

To investigate how \( n_f \) depends on the relative permittivity of the substrate, substrate PCB FR4, Duroid 5870 and Duroid 6010 are used with the slot length up to 50 mm. The simulated results are shown in Fig. 3.18.

Fig. 3.18 \( n_f \) as a function of slot length with PCB FR4, Duroid 5870 and 6010 substrate.
Fig. 3.19 Microstrip feed lines on one side, and five slot lines on the other, of a fabricated PCB board.

The PCB FR4 board shown in Fig. 3.19 was used for practical measurements: one side of the board shows 5 SLs of lengths 10, 20, 30 40 and 50 mm and the other side shows the five 50 Ω feed MLs, as well as a 50 Ω microstrip calibration line. The width of the SL was 1 mm and the equations derived in [117] were used to determine the SL input impedance $Z_S$. $n_f$ was obtained from the $S_{21}$ parameter determined by both practical measurement and simulation. Fig. 3.20 shows excellent agreement between these two approaches for determining $n_f$. It is important to note that this turns ratio has a limited range of 0.9 to 0.98.
for a slot line length over 25 mm that is typical in the design of an antenna at around 2 GHz.

The effect of three different substrate thicknesses (0.7875, 1.575 and 2.5 mm) on \( n_f \) was also investigated by simulation as described above and (3.25) was obtained by means of curve fitting of Fig. 3.20.

\[
n_f = 1 - e^{-\frac{jz}{4h}}. \tag{3.25}
\]

For three substrates of different permittivity, with a fixed SL of length 30mm, the above method was used to obtain the frequency response of \( Z \) for the physical structure and the equivalent circuit. It was found that the obtained frequency response of the physical structure, even over an extended range of 1 GHz to 5 GHz, agreed very closely with the frequency response obtained from the equivalent circuit. As \( n_f \) has a constant value in the equivalent circuit it can be concluded that \( n_f \) is effectively independent of both frequency and the relative permittivity of the substrate across the parameter ranges investigated.

### 3.5.2 Determine Turns Ratio \( n_f \) using \( S_{11} \) Parameter

To obtain \( n_f \) it is first necessary to determine \( Z \) from the \( S_{11} \) parameter. SL is fed by a 50 \( \Omega \) microstrip feed line of length \( L_1 + L_2 \) as in Fig. 3.21(a) and to calibrate out the measurements errors produced by \( L_1 \) a 50 \( \Omega \) calibration open circuit microstrip shown in Fig. 3.21(b) is used.
Fig. 3.21 Structure of model established for $S_{11}$ test: (a) ML with slot, and (b) open circuit microstrip calibration line.
The signal flows of models in Fig. 3.21 are given in Fig. 3.22. In Fig. 3.22(a), the incident signal is $a_1$ while the reflected signal at the input is $2a_1A_1\rho\exp(-2j\theta)$, where $A_1$ is the attenuation, $\rho$ is the reflection coefficient and $\theta$ is the phase delay. For the open circuit the reflection coefficient is one so the reflected signal is $2a_1A_1\exp(-2j\theta)$. At the source part, the reflected signal $S_{11T}$ and $S_{11oc}$ are given by (3.26) and (3.27):

$$S_{11T} = \frac{2a_1A_1\rho e^{-2j\theta}}{a_1} = 2A_1\rho e^{-2j\theta}, \quad (3.26)$$

$$S_{11oc} = \frac{2a_1A_1 e^{-2j\theta}}{a_1} = 2A_1 e^{-2j\theta}. \quad (3.27)$$

The reflection coefficient $\rho$ and then the series impedance $Z$ can now be obtained using (3.28) and (3.29):
\[
\frac{S_{11T}}{S_{11ac}} = \frac{2A_1 \rho e^{-2j\theta}}{2A_1 e^{-2j\theta}} = \rho, \quad (3.28)
\]

\[
Z = \frac{2\rho Z_0}{1 - \rho}, \quad (3.29)
\]

Note \( Z_S = \frac{1}{2jZ_0 \tan(\theta_s/2)} \). \( Z_0 \) and \( \theta_s \) of SLs can be obtained from [117]. The final \( n_f \) can be calculated by (3.30):

\[
n_f = \sqrt{\frac{Z}{Z_c}}, \quad (3.30)
\]

Simulations have been carried out by using substrates PCB FR4, Duroid 5870 and Duroid 6010 which agree with the results shown in Fig. 3.18 obtained using the \( S_{21} \) method. It is obvious that \( n_f \) increases rapidly with SLs. For the SL > 20 mm, \( n_f \) is almost constant (closer to 1) and the results from these three substrates are in good agreement. Hence, \( n_f \) is only marginally affected by the dielectric constant of the substrate. These results could be used in future designs where the numbers of design parameters of ACMA can be reduced.

Fig. 3.23 Microstrip feed lines with slot lines (0 – 50 mm) and open circuit microstrip calibration line.
The fabricated boards using PCB FR4 substrate as shown in Fig. 3.23 are used to obtain $S_{11T}$, $S_{11oc}$, the reflection coefficient $\rho$ and hence the series impedance $Z$. The simulation and measured results are in good agreement as shown in Fig. 3.24. By using curve fitting the equation obtained is the same as (3.25).

![Fig. 3.24 Measured and simulation results for the turn ratio $n_f$ as a function slot line lengths.](image)

In order to validate the results obtained, a practical PCB board was fabricated with 40 mm open circuit ML, 80 mm microstrip through line with 30 mm slot length as shown in Fig. 3.25. By using the turn ratio obtained from (3.30), circuit simulation results and practical measurement carried out for $Z$ to validate this method are compared in Fig. 3.26, which are in good agreement.

![Fig. 3.25 Fabricated boards with (a) feed and open circuit side, and (b) slot line side.](image)
3.6 Investigation of the End Effects of the Slot

The two types of discontinuities of slot are investigated, which are short-end and open-end. The open end structure is not commonly used due to the impractical implementation and lots of radiation loss. A short end is created by just ending the slot with a conducting surface. Due to the current flows in the conductor plane at both ends of the SL there is stored magnetic energy which gives an inductive reactance that behaves as an electrical extension $\Delta L_s$ to physical length of the slot. Full wave analysis was presented by [125, 126] and also practical measurements were carried out in [127] showing the normalized reactance in terms of the thickness to wavelength ratio, which is in a good agreement. Losses of the short end also exist due to the power propagation in surface waves and radiation, which could be modelled as $R_s$. Yang and Alexopoulos [126] presented the investigation of the normalized resistance in terms of thickness to wavelength ratio of the substrate.
In this section, a simplified method to investigate $\Delta L$ by comparing the resonant frequency of the slot with tuned circuit results and measured results is given. Based on the application of the proposed antenna design, the width of slot is fixed to 1 mm and working frequency is 2 GHz. To determine $\Delta L_s$, $S_{21}$ could be used to determine the resonant frequency as the value drops to minimum at that point. A two port network shown in Fig. 3.27(a) is used to measure $S_{21}$ physically and compare it with the tuned circuit results based on Fig. 3.27(b) in terms of physical slot length. Results given in Fig. 3.28 show that $\Delta L$ is proportional to the physical length and inversely proportional to the dielectric constants for a fixed substrate height of 1.575 mm.

Fig. 3.27 Two port network of feed slot structure used for $S_{21}$ test: (a) physical structure, and (b) circuit structure.
Fig. 3.28 Extended end effect slot length in terms of physical slot length using substrate PCB FR4, Duroid 5870 and Duroid 6010.

Using the same methodology for determining $\Delta L_s$, the equivalent end resistance $R_s$ could be measured and obtained by $S_{21}$ parameters using (3.21) - (3.24) at the resonant frequency. Increase the physical length of slot (0 – 50 mm) by comparing the measured results with tuned circuit results based on Fig. 3.27. Results are given in Fig. 3.29, which indicates that $R_s$ is slightly reduced from 0 to 20 mm and levelling off at 7, 11, and 2 $\Omega$ for PCB FR4, Duroid 5870 and Duroid 6010, respectively between the range of 20 to 50 mm of slot length. Also shown is that $R_s$ is inversely proportional to dielectric constants for a fixed substrate height of 1.575 mm.
3.7 Investigation of the Coupling Ratio between the Slot and the Patch

Coupling between the slot and patch is modelled by $n_p$, and the equivalent circuit of the slot/patch physical structure with transformer is shown in Fig. 3.30.

Fig. 3.29 $R_s$ varies in terms of the physical slot length with the effects of substrate PCB FR4, Duroid 5870 and Duroid 6010.
From the literature review, Himdi [121] suggested that $n_p$ is a function of the SL and patch width as given by:

$$n_{pH} = \frac{L_s}{W_p}, \quad (3.31)$$

where $n_{pH}$ is $n_p$ defined by Himdi.

However, Jaisson [112] proposed different suggestions based on the theorem of reciprocity and computed with a table of integrals in hand that the coupling ratio is affected by the effective width of patch $W_p'$ and length of slot, which is given by:

$$n_{pJ} = \frac{L_s}{2W_p'}, \quad (3.32)$$

where $n_{pJ}$ is $n_p$ defined by Jaisson.

Kyriacou [128] considered the patch as a short but wide ML and using the curve fitting derived the following:

$$n_{pK} = \sqrt{2.42 \frac{W_p^2}{L_s W_s \sqrt{\epsilon_r}}}, \quad (3.33)$$

where $n_{pK}$ is $n_p$ defined by Kyriacou.

Equations (3.31-3.33) are plotted in Fig. 3.31 with SLs up to 50 mm for the patch width of 50 and 60 mm, showing large differences for the turns ratio.
Fig. 3.31 $n_p$ as a function of slot length and the patch width of: (a) 50 mm, and (b) 60 mm.
To address this problem, the following analysis is carried out. First, the feed/slot dimensions were kept constant to ensure that \( n_f \) had a fixed value and the patch width was varied from 50 mm to 70 mm. Then the SL length was varied up to 50 mm and for each SL, \( n_p \) was tuned using the AWR software until the input impedance of the equivalent circuit and that of the physical structure using CST simulation were in good agreement. The determined turns ratio agreed very closely with (3.32) derived by Jaisson, see Fig. 3.32.

![Graph showing \( n_p \) as a function of \( L_s \) and \( W_p \) with the comparison of simulation and Jaisson’s results.]

3.8 Design Procedure of an ACMA

Based on the analysis carried out in this chapter, a simplified design procedure for a typical ACMA could be obtained. The patch and SLs are connected in parallel, see Fig 3.33, and the input admittance looking up from slot is given by Fig. 3.34. Because of the parallel structure, the admittance instead of impedance is adopted in the analysis.
Fig. 3.33 Equivalent structure of the parallel patch and slot.

Due to the slot coupling technique, the patch behaves as a series tuned circuit and the resonant frequency of the patch is slightly larger than the design frequency. Hence the length $L_p$ is slightly less than the half-wavelength at the design frequency ($\sim 0.9\lambda_p/2$), where $\lambda_p$ is the patch wavelength. The imaginary part of the admittance has a capacitive value,
which is used to calibrate the inductive value produced by the slot. The frequency response of the input admittance of the SL is shown in Fig. 3.35

![Frequency response of the input admittance of the SL](image)

Fig. 3.35 Input admittance of SL.

The resonant frequency of the slot is again higher than the design frequency however the inductive value of the imaginary admittance could be used to cancel out the value produced by the patch. The slot length should be ~0.7\(\lambda_s\)/2. Based on the above results and the investigations carried out previously, the design process and the approximate starting values of the components in the equivalent circuit are suggested below.

1) In the investigation of this antenna it has been found that the resonant frequency of the series impedance of the patch is above the design frequency. Hence \(L_p<0.9\lambda_p/2\).

2) \(W_p\) could be determined by (3.3).

3) To reduce spurious radiation, \(W_s\) is specified as 1 mm. So \(Z_{0s}\), which is mainly based on \(W_s[9]\), is ~100 \(\Omega\).
4) The parallel resonant frequency of the slot is also higher than the design frequency and \( L_s = -0.7\lambda_s/2 \), and \( n_p = L_s/2W_p \).

5) \( n_f \) is largely independent of relative permittivity of the substrate. Above a slot length of \(~20\) mm it has a constant value of 0.9.

6) All the parameters of the physical and equivalent circuit of the antenna are now approximately known but are required to be fine-tuned so that the input impedance at the microstrip feed position is in the form \( 50 + jX \Omega \). The open circuit length beyond the above feed position of the microstrip line can be obtained so that the antenna is matched.

Following the design procedure, a narrow bandwidth ACMA is designed. The dimensions are shown in table 3.1 and the return as a function of the frequency loss for \( S_{11} \) for the equivalent circuit simulation and full wave simulation is depicted in Fig. 3.36, showing good agreement. The bandwidth is about 50 MHz. The height of substrate between patch/slot, and the slot feed line are both 1.575 mm and \( n_f \) and \( n_p \) are 0.89 and 0.22, respectively.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit: mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>( W_p )</td>
<td>55</td>
</tr>
<tr>
<td>( L_p )</td>
<td>30.9</td>
</tr>
<tr>
<td>( W_s )</td>
<td>1</td>
</tr>
<tr>
<td>( L_s )</td>
<td>19.1</td>
</tr>
<tr>
<td>( W_{st} )</td>
<td>3</td>
</tr>
<tr>
<td>( L_{st} )</td>
<td>8</td>
</tr>
</tbody>
</table>

Table 3.1 Dimension of an ACMA.
3.9 Design of Broadband Dual Frequency ACMA

To obtain a dual frequency antenna, modes at 1.9 GHz and 2.4 GHz are excited by the two SLs near the edges of the patch as shown in Fig. 3.37(a).

Fig. 3.36 Frequency response of the return loss.
In this figure $L_{p1}$ and $L_{p2}$ are the physical dimensions of the patch while $L_{s1}$ and $L_{s2}$ are the lengths of the two slots. The height of the air substrate above the ground plane was designed as to be 8 mm (it is easy to achieve practically) and the substrate below the ground plane was PCB FR4. The equivalent circuits of the two modes are shown in Fig. 3.37(b) where $G$ models the radiated power from the patch’s radiating slots and $C$ models the fringing fields at the physical edges of the patch [9].

A wide matching bandwidth and a high gain can be obtained by the antenna if a thick air substrate is used below the patch [45]. However, a thick substrate will change the surface wave efficiency and equation (3.1) will not fit for this case. In Fig. 3.38, results obtained from (3.1) are compared with the simulation data for $\Delta L$ of the fringing field as function of the height of the air substrate for patch widths of 43 mm and 57 mm that will be used in the
dual frequency aperture coupled antenna design. The obtained $\Delta L$ of the air substrate of both patch widths is greater than predicted from (3.1).

![Graph showing Length of the fringing field $\Delta L$ as a function of the height of air substrate obtained from simulation and equation (3.1).](image)

Equation (3.34) was derived for the length of the fringing field as a function of the height $H$ (mm) of the air substrate using a curve fitting approach.

$$\Delta L = 12\left(1 - e^{-\frac{H}{5}}\right).$$

(3.34)

The resonant frequency of the series input impedance of the patch at the position of SL is normally above the design frequency. Hence the effective length of the patch should be slightly less than half-wavelength ($\sim 0.9\lambda_p/2$) where $\lambda_p$ is the patch wavelength at the design frequency. The approximate effective dimensions of the patch are 76 mm at 1.9 GHz and 61 mm at 2.4 GHz. The corresponding physical dimensions of the patch are 57 mm at 1.9
GHz and 43 mm at 2.4 GHz. The resonant frequency of the SL is normally higher than the
design frequency so that $L_s \sim 0.7\lambda_s/2$. Consequently the assumed initial physical lengths of
SLs obtained are 33 mm at 2.4 GHz and 42 mm at 1.9 GHz. These lengths were then used
in (3.25) and the initial approximate value of $n_f$ was 0.96 at 1.9 GHz and 0.95 at 2.4 GHz.
By substituting the above SL lengths and the physical widths of the patch into (3.32) the
approximate values for $n_p$ are 0.217 and 0.33 at 2.4 GHz and 1.9 GHz, respectively. For the
two frequencies the initial and final tuned values for the two equivalent circuits and
physical dimensions of the two antennas are close to each other as shown in table 3.2.

<table>
<thead>
<tr>
<th>Dimension of dual frequency ACMA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
</tr>
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<td>1.9 GHz</td>
</tr>
<tr>
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</tr>
<tr>
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</tr>
<tr>
<td>$W_s$</td>
</tr>
<tr>
<td>$L_s 1$</td>
</tr>
<tr>
<td>$\Delta L_p 1$</td>
</tr>
<tr>
<td>Turn ratio $n_f$</td>
</tr>
<tr>
<td>Turn ratio $n_p$</td>
</tr>
<tr>
<td>$R$</td>
</tr>
<tr>
<td>2.4GHz</td>
</tr>
<tr>
<td>$L_p 1$</td>
</tr>
<tr>
<td>$L_p 2$</td>
</tr>
<tr>
<td>$W_s$</td>
</tr>
<tr>
<td>$L_s 1$</td>
</tr>
<tr>
<td>$\Delta L_p 1$</td>
</tr>
<tr>
<td>Turn ratio $n_f$</td>
</tr>
<tr>
<td>Turn ratio $n_p$</td>
</tr>
<tr>
<td>$R$</td>
</tr>
</tbody>
</table>

Table 3.2 Dimension of a broadband dual frequency ACMA.
The obtained frequency responses of the return loss of the equivalent circuit and the physical antenna at ports 1 and 2 are shown in Fig. 3.39.

![Frequency response of the return loss of the two matched antenna.](image)

Fig. 3.39 Frequency response of the return loss of the two matched antenna.

The -10 dB matching bandwidth at 1.9 GHz is 260 MHz and at 2.4 GHz it is 430 MHz. Also there is a good agreement for the return loss obtained from the circuit simulation carried out by AWR and the full wave simulation by CST.

Finally the two feed ports shown in Fig. 3.37(b) are joined together by two arms (50 Ω MLs) of lengths $L_{f1}$ and $L_{f2}$, see Fig. 3.40. The input impedance of $Z_1$ at 1.9 GHz and 2.4 GHz are 50 Ω and $101.6+j221$ Ω, respectively. Matching the impedance that for $L_{f1}$ of 71.4 mm the input impedance $Z_f$ at the feed port increases to 689 Ω at 2.4 GHz but of course the antenna is still matched at 1.9 GHz. Similarly at 2.4 GHz, $Z_2$ is 50 Ω and, $Z_5$ is $7.63-j41.14$ Ω at 1.9 GHz. For $L_{f2}$ of 35.4 mm the input impedance $Z_f$ at the feed port increases to 984 Ω at 1.9 GHz but at 2.4 GHz the antenna is still matched.
The fabricated board of the designed antenna is shown in Fig. 3.41 and simulated and practical frequency responses of the return loss and measured gain are shown in Fig. 3.42.

Fig. 3.41 Photograph of the fabricated antenna (a) radiation element, and (b) feed line.
Fig. 3.42 Simulated and practical frequency responses: (a) reflection coefficient, and (b) gain of the antenna.

A very good agreement has been obtained between the simulated and measured frequency responses for the reflection coefficient and for the gain of the antenna. Simulation results showed that gain of 6.3dB and 7dB at 1.9 GHz and at 2.4 GHz, respectively with corresponding practical measurements of 6.6 dB at 1.9 GHz and 7.2 dB at 2.4GHz.
3.10 Summary

This chapter analysed the equivalent circuit of an ACMA, which consisted of radiating patch, slot line and microstrip feed line. The patch was reviewed using TL model. Numerical methods were given to calculate the physical width and length of the patch. The coupling ratio between feed and slot was defined as $n_f$; and the coupling ratio between the slot and patch was defined as $n_p$. In this chapter a novel method using the S parameter to investigate $n_f$ was proposed and validated by practical measurement, thus showing that $n_f$ mainly varied with the slot length and height of substrate. $n_p$ also was investigated by fix feed/slot dimension, tuning width of path until the frequency response of impedance agreed with full wave simulation results. A simplified design procedure was proposed for an ACMA by reducing the number of design parameter and obtaining a matched antenna logically. Finally, a dual polarized dual frequency wide bandwidth ACMA was designed by using the design procedure. Practical results showed a good agreement with the circuit simulation results.
Chapter 4 Review and Theoretical Analysis of Power Amplifier using Linear Model

4.1 Introduction

A PA is one of the most commonly used electrical elements for converting the input DC power into the microwave output signal. It can be utilized in wireless communication systems, radar and medical applications, as well as in RF heating systems where high efficient PAs are used [129-131]. The main objective in the design of these amplifiers is to produce high efficiency conversion from DC to AC that is used in the transmitter. If the high efficiency is to be achieved then considerable reduction in dissipated power becomes increasingly an important issue [132-135]. This chapter introduces design parameters of typical PAs. Gain and efficiency are the key parameters to measure the ability of signal amplification and DC to AC power conversion respectively. PAs are defined as classical type (class A to class C PAs) and high efficiency type (class D to inverse class F PAs) which depend on the quiescent bias point Q to the conduction angel θ. The class F and inverse class F PAs are picked out for the further investigation due to their high gain and high efficiency performance. The active device is modelled by an ideal switch connected with a resistor which models the power loss. Harmonic load matching networks are designed with infinity harmonics and up to third harmonic frequency to shape the voltage and current waveforms over the active device. Effects of internal resistance of transistor and harmonics of frequencies on the power convert efficiency are presented.
4.2 Reviews of PAs

Historically RF power was generated by spark, arc, and alternator techniques for wireless communications between 1890 and 1920s. In 1907, the RF signal was generated and controlled by the thermoionic vacuum tubes, and the vacuum tube based PAs were widely used from 1920s to 1970s [136]. In 1948, Bardeen, Brattain, and Shockley [137, 138] invented the first bipolar transistor, which lead to a telecommunication revolution, but with poor gain and noise figures. In 1965, a Germanium (Ge) based transistor was fabricated that was limited by the low band gap thus leading to a high leakage current and poor thermal performance. In 1990s a number of novel solid state devices [139, 140] based on the high electron mobility transistor (HEMT), pseudomorphicHMET (pHEMT), heterojunction field effect transistor (HFET), and heterojunction bipolar transistor (HBT) using new materials such as indium phosphide (InP), aluminium gallium arsenide (AlGaAs), indium gallium arsenide (InGaAs), silicon carbide (SiC), and gallium nitride (GaN) offered additional improvement in performance. The efficiency and linearity of the combination of digital signal processing [141, 142] and microprocessor control could be further enhanced by using feedback and pre-distortion technologies. In today’s world, the applications of PAs are diverse. E.g. communications, navigation and broadcasting applications across a wide frequency range from very low frequency (VLF) to extremely high frequency with power levels from 10 mW to 1 MW [1, 143, 144]. Also in radar, RF heating, plasma generation, laser drivers, magnetic resonance, and miniature DC/DC converters, PAs and transmitters are widely used.
4.3 Design Parameters of PAs

The block diagram of a PA is shown in Fig. 4.1 where $P_{DC}$ is the DC power supply, $P_{AC}$ is the AC input power, $P_{diss}$ is the total power dissipation and $P_{out}$ is the output power. The circuit model of a PA is given by Fig. 4.2. $V_{DD}$ and $I_{dc}$ are the DC voltage and current from the DC power supply, respectively. $V_{ds}$ and $I_{ds}$ are the voltage and current that flow through the active device, respectively, and $R_L$ is the load resistance of the active device.
The total input power must equal to the output power as defined by (4.1):

\[ P_{DC} + P_{AC} = P_{out} + P_{diss}. \]  

(4.1)

Efficiency is a critical factor in PA design, which is normally described as the drain efficiency and PAE. Also the instantaneous efficiency (i.e. the efficiency at one specific output level) is the highest at the peak output power (PEP) for most PAs.

The drain efficiency is defined as the ratio of output power to the DC power input which is defined by:

\[ \eta = \frac{P_{out}}{P_{DC}}. \]  

(4.2)

For time varying amplitude measurement, the average efficiency is defined by:

\[ \eta_A = \frac{P_{outA}}{P_{DCA}}, \]  

(4.3)

where \( P_{outA} \) and \( P_{DCA} \) is the average output power and average DC power, respectively.

PAE indicates the AC power by subtracting it from the output power, which gives a reasonable indication of PA performance, as defined by:

\[ PAE = \frac{P_{out} - P_{AC}}{P_{DC}}. \]  

(4.4)

The power gain \( G_p \) could be defined by:
4.4 Types of PAs

PAs are normally classified as class A to F [145] which operate in different efficiency and output power capabilities. The power capability is the output power per transistor normalized to the peak drain voltage and current of 1 V and 1 A, respectively [131]. The single end topology is used to analyse a typical PA shown in Fig. 4.2, which includes the active device, DC power supply, and an output harmonic matching network.

4.4.1 Classical PAs

The type of the amplification determines the kind of bias applied to a RF power transistor. The classical PAs (classes A, AB, B, and C) operate in the linear region and the output current is in the saturation area, which is controlled by the input voltage $V_{gs}$. For these classes of PAs it is convenient to relate to $Q$ and $\theta$ [146, 147].

A class A PA is defined by the output current flowing for a full-cycle (360 degrees) of the input signal. The drive level is kept small enough to avoid driving the transistor into the cut-off mode (i.e. the transistor remains forward biased throughout the input cycle). In class A PA, the transistor is active at all times acting as a current source controlled by the gate voltage. The drain voltage and current are both sinusoids, see Fig. 4.3 [148] where $V_p$ is the pinch off voltage and $i_{max}$ is the peak current of active device. This PA is typically used for its low power requirement, high linearity, high gain, low distortion and broadband operation [14, 149, 150].
However, class A PA is not very efficient in that the instantaneous efficiency is proportional to the output power offering theoretically a maximum of 50%. In addition such amplifiers are large, heavy, and operating at high temperature and full power [151].

For class B PA, the Q point is set such that only half of the input wave cycle is amplified. Thus leading to generation of a large amount of distortion, but with greatly improved efficiency (up to 78.5%) compared to class A PAs [132]. The $\theta$ of class B PA is approximately $180^0$ [152]. The load line, voltage and current waveforms are shown in Fig. 4.4 [152, 153].
Class AB PA is a compromise between class A and class B in terms of the efficiency and linearity. As shown in Fig. 4.5 [154, 155], the Q point is set between the cut off region and class A point. So the transistor will be on more than a half cycle but less than a full circle. \( \theta \) is between 180° and 360° and the efficiency is between 50 % and 78.5 % [2, 156].
Class C PA is biased below $V_p$ and $\theta$ is less than 180°, see Fig. 4.6 [154, 155]. This PA is biased under the steady state conditions and there is no flow of the collector current. It has the poorest linearity of these PAs with the efficiency reaching more than 80% but large amount of signal distortion. [147, 157].

4.4.2 High Efficiency PAs

Due to the overlapping of the voltage and current waveforms of classical PAs, the power dissipation is considerable, which can lead to degradation of the efficiency. In order to minimise the power dissipation from the active device, higher efficiency PAs [152, 158-161] are introduced and the most popular and typical types are class D, E, F and inverse F. For the class D PA, where the circuit shown in Fig. 4.7 [154, 155], two active devices behave as switches, which are alternatively switched on and off by the drive signal to generate the square drain voltage waveform, see Fig. 4.8 [152, 162, 163]. The load resonant circuit is used to ensure that PA is only working at the fundamental frequency. However, it is difficult to realize this particularly at higher frequencies. The available
active devices for the upper switch are limited and losses are due to the saturation, switching speed and drain capacitance.

![Diagram of Class D PA]

Fig. 4.7 Class D PA.

![Diagram of Voltage and Current Waveform]

Fig. 4.8 Voltage and current waveform of class D PA.

The class E PA is a switching type device, which has a single active device acting as an ideal switch [158, 164-166]. It can achieve 100% efficiency theoretically but the internal resistance of the transistor and the non-ideal filter at the output stage will degrade the efficiency. As shown in Fig. 4.9, the load tuned circuit is used to ensure that only the fundamental current can flow through the load. The voltage and current waveforms
through the active device are shown in Fig. 4.10. It is the result of summation of DC and RF currents charging the capacitance $C_p$ which is in parallel with the transistor.

![Fig. 4.9 Class E power amplifier.](image)

The class F and inverse class F PAs are both highly efficient with the drain waveforms mainly shaped by controlling the output harmonic resonators. The theoretical analysis and modelling of the class F and inverse class F PAs are presented in the next section.

![Fig. 4.10 Voltage and current waveform of class E PA.](image)
4.5 Theoretical Analysis and Comparison of Class F and Inverse Class F PAs

The active device of class F PA and inverse class F PA could be modelled as an ideal switch connected with an internal resistance $R_{on}$ which indicate the power dissipation in the transistor, see Fig. 4.11. The voltage and current flow over the drain are controlled by harmonic load resonators in the output network. To obtain maximum DC to AC power convert efficiency, the voltage waveform is square while the current waveform is half sinusoid for a class F PA. Alternately, half sine voltage wave and square current wave are applied for inverse class F PA, see Fig. 4.12.

![Fig. 4.11 Circuit model for class F and inverse class F PA.](image)

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$v_{max}$ ($v'_{max}$) and $i_p$ ($i'_p$) are the peak voltage and current flowing through the active device, respectively of class F PA (inverse class F PA). $v_k$ ($v'_k$) is the knee voltage, which is due to the effects of $R_{on}$ of class F PA (inverse class F PA).

The required impedance of the load harmonic network for the class F and inverse class F PAs to obtain ideally 100% efficiency is defined by:

$$Z_{Fun} = R_L, \quad (4.6a)$$

$$Z_{2n} = 0, \quad (4.6b)$$

$$Z_{2n+1} = \infty, \quad (4.6c)$$
where $Z_{Fun}$ is the load impedance of the active device at the fundamental frequency, $Z_{2n}$ is the impedance at even harmonics, $Z_{2n+1}$ is the impedance at odd harmonics, and $n = 1, 2, 3\ldots$

Similarly, for the inverse class F PA:

\begin{align*}
Z_{Fun} &= R_L, \quad (4.7a) \\
Z_{2n} &= \infty, \quad (4.7b) \\
Z_{2n+1} &= 0. \quad (n = 1, 2, 3\ldots) \quad (4.7c)
\end{align*}

The ideal current and voltage waveforms are expanded by the Fourier series [9] for the class F PA and are given by:

\begin{align*}
V_{ds}(\theta) &= V_{DD} - \frac{4(V_{DD} - v_k)}{\pi} \sum_{n=1,3,5\ldots} \sin(n\theta), \quad (4.8a) \\
I_{ds}(\theta) &= i_p \left[ \frac{1}{\pi} + \frac{1}{2} \sin(\theta) - \frac{2}{\pi} \sum_{n=2,4,6\ldots} \frac{\cos(n\theta)}{n^2 - 1} \right]. \quad (4.8b)
\end{align*}

From (4.6) and (4.7), $I_{dc}$, $P_{DC}$, fundamental voltage $V_{Fun}$, fundamental current $I_{Fun}$, fundamental power output $P_{Fun}$, $R_L$, and $\eta$ could be derived by:

\begin{align*}
I_{dc} &= \frac{i_p}{\pi}, \quad (4.9a) \\
V_{Fun} &= \frac{4(V_{DD} v_k)}{\pi}, \quad (4.9b)
\end{align*}
\[ I_{Fun} = \frac{i_p}{2}, \quad (4.9c) \]

\[ P_{DC} = \frac{V_{DD}i_p}{\pi}, \quad (4.9d) \]

\[ P_{Fun} = \frac{(V_{DD}-v_k)i_p}{\pi}, \quad (4.9e) \]

\[ R_L = \frac{V_{Fun}}{I_{Fun}} = \frac{8(V_{DD}-v_k)}{\pi i_p}, \quad (4.9f) \]

\[ \eta = \frac{V_{DD}-v_k}{V_{DD}}. \quad (4.9g) \]

The voltage and current waveforms are expanded by the Fourier series for the inverse class F PA and defined by:

\[ V'_{ds}(\theta) = v_k' + (v_{max}' - v_k')(\frac{1}{\pi} - \frac{1}{2}\sin(\theta) + \frac{2}{\pi} \sum_{n=2,4,6,...} \frac{\cos(n\theta)}{n^2-1}), \quad (4.10a) \]

\[ I'_{ds}(\theta) = \frac{i_p'}{2} \left( 1 + \frac{4}{\pi} \sum_{n=1,3,5,...} \frac{\sin(n\theta)}{n} \right). \quad (4.10b) \]

The corresponding equations for the inverse class F PA are defined by:

\[ I_{dc} = \frac{i_p'}{2}, \quad (4.11a) \]

\[ V_{Fun}' = \frac{\pi(V_{DD}-v_k)\sin(\theta)}{2}, \quad (4.11b) \]

\[ I_{Fun}' = \frac{2i_p' \sin(\theta)}{\pi}, \quad (4.11c) \]
\[ P_{DC}' = \frac{V_{DD}i_p'}{2}, \]  
(4.11d)

\[ P_{Fun}' = \frac{\pi(V_{DD}-v_k)i_p'}{2}, \]  
(4.11e)

\[ R_L' = \frac{V_{Fun}}{I_{Fun}} = \frac{\pi^2(V_{DD}-v_k')}{4i_p'}, \]  
(4.11f)

\[ \eta' = \frac{V_{DD}-v_k'}{V_{DD}}. \]  
(4.11g)

The performance of the two amplifiers can be compared by deriving equations for the inverse class F amplifier in terms of the design parameters of the class F amplifier. This is obtained by ensuring that the DC input power for both amplifiers is the same so that \( i_p' \) can be expressed in terms of \( i_p \):

\[ i_p' = \frac{2i_p}{\pi}. \]  
(4.12a)

\( v_k' \) is obtained in terms of \( i_p \) and \( R_{on} \):

\[ v_k' = i_p'R_{on} = \frac{2i_p}{\pi}R_{on}. \]  
(4.12b)

Similarly \( R_L' \) is defined by:

\[ R_L' = \frac{\pi^3(V_{DD}-\frac{2i_p}{\pi}R_{on})}{8i_p}. \]  
(4.12c)
From the derived equations, the output characteristics of an active device are shown in Fig. 4.13.

![Output characteristic of the active device](image)

Fig. 4.13 Output characteristic of the active device.

To compare the efficiencies of the two amplifiers the following modified equations for the inverse class F amplifier can be obtained by using the following equations:

\[
P_{Fun} = \frac{(V_{DD} - \frac{2ipR_{on}}{\pi})ip}{\pi}, \quad (4.12d)
\]

\[
\eta' = \frac{V_{DD} - \frac{2ipR_{on}}{\pi}}{V_{DD}}. \quad (4.12e)
\]

Assuming the condition that for \(V_{DD} = 5 \text{ V}\) and \(i_p = 0.5 \text{ A}\), the input DC power is 0.796 W. The output power, efficiency and the load resistance in terms of \(R_{on}\) (0 to 5 ohms) for the two amplifiers are shown in Fig. 4.14.
Fig. 4.14 Effects of $R_{on}$: (a) power output, (b) DC to AC power conversion efficiency, and (c) load resistance.

Fig. 4.14 indicates that the efficiency reduces as a function of $R_{on}$ but this reduction is greater for the class F amplifier than it is for the inverse class F. For $R_{on} = 2 \ \Omega$ the power conversion efficiencies are 87.3% and 80% for the inverse class F and the class F amplifiers, respectively. The calculated load resistances will be used to design the load harmonic networks for the two amplifiers as discussed in the next section.

### 4.6 Linear Switch Model Analysis of Class F and Inverse Class F PAs

As discussed in the last section, efficiency degrades with increasing $R_{on}$. The efficiency is also affected by the load impedance of active device not only at the fundamental frequency but also at all the other harmonics [160, 167]. Tyler [168] has produced a class F PA
design using multiple resonators for amplitude modulation (AM) broadcast transmitters at low frequency (LF) to high frequency (HF) ranges. He also proposed a TLM to overcome the difficulty in using it in the very high frequency (VHF) range. Also other researchers have proposed different methods to control the second, third, and even fifth and seventh harmonics [169-174] in order to minimise the overlap of voltage and current waveforms. However, these topologies were complicated and created higher power losses with increased frequency. Hence, in the following sections, simplified and novel designs of the harmonic load matching networks are given to produce impedance conditions at infinity harmonics and up to third harmonic using lump elements model and TLM for the Ultra high frequency (UHF) applications. Also the effects on efficiency and the waveforms of voltage and current flowing through the active device are discussed.

4.6.1 Linear Switch Model Analysis with Infinite Harmonics Conditions

Theoretical investigation of the harmonics effects for the class F was well reviewed in [160, 167] outlining that the efficiency drops with decreasing numbers of harmonics. However, this theory has only been introduced roughly without rigorous investigation. In this section the transistor is modelled by using an ideal switch with an internal resistance $R_{on}$, and details of design investigation for an infinity harmonic load, and harmonic load up to third harmonics using the lump elements and TLs are given. Since ideal voltage and current waveforms are the requirement with the harmonic load matching network to make the even harmonic impedance equal to 0 and the odd harmonic equal to infinity for the class F PA, the structure of linear switch model with infinity harmonic load matching network is show in Fig. 4.15.
Fig. 4.15 Ideal linear switch model of class F PA.

An infinite harmonics load matching network consists of a TL (50 $\Omega$, 90 degree, and 2 GHz) which series connect with an RLC parallel tuning circuit. The RLC circuit resonant at 2 GHz, and the TL makes even and odd harmonics to be 0 and $\infty$, respectively. The drain voltage and current waveforms are produced by ADS software which is shown in Fig. 4.16.
Fig. 4.16 Voltage and current drain waveforms of ideal linear switch model of class F PA.

Square voltage and half sine current wave forms are obtained as predicted in Fig. 4.12. For the inverse class F PA, the structure of the circuit and waveforms are shown in Fig. 4.17, and Fig. 4.18.

Fig. 4.17 Ideal linear switch model of inverse class F PA.
Fig. 4.18 Voltage and current drain waveforms of ideal linear switch model of inverse class F PA.

The simulation waveforms shown in Fig. 4.18 are in good agreement with predicted results outlined in Fig. 4.12.

4.6.2 Linear Switch Model Analysis with up to Third Harmonics Conditions using Lump Element

It is impossible to obtain load matching with an infinite number of harmonics. It is also not necessary to do this because of the power dissipation produced by the network elements. Up to third harmonics matching networks has been widely reported in [131, 160,175]. Designs carried out in [176, 177] have shown that intelligent based approach in tuning the separate harmonic matching load has been adopted to obtain the predicted voltage and current waveforms through the active device. A simplified novel design method is presented in this section, which does require no tuning but with logical and accurate
calculation of the harmonic load matching networks for both class F and inverse class F PAs. The schematic shown in Fig. 4.19 is a lumped element design for the class F PA.

In order to obtain square voltage and half sine current waveforms for the class F PA, the load impedance of the active device has to be 0 at the second harmonic and infinity at the third harmonic frequencies. The block S_2 in Fig. 4.19 is an LC resonant circuit, which produces a short circuit at the second harmonic and a positive reactance value at the third harmonic. The impedance produced by LC circuit at fundamental frequency, second and third harmonic frequencies are shown in Fig. 4.20.

Fig. 4.19 Lumped elements harmonic load design for class F PA.
Block $S_3$ is used to obtain infinite impedance at the third harmonic. The series LC resonant circuit $L_3$ and $C_3$ are used to obtain a short circuit at point A for the third harmonic, which aims to eliminate the fundamental matching effects. The capacitance $C_4$ is used to add the negative reactance to obtain an opposite sign but the same value created by the block $S_2$. Due to the shunt connection, the infinite impedance could be obtained from this parallel network by looking from the load of active device model. The fundamental matching circuit could be easily obtained by using the LC impedance matching method [14] and calculating $R_L$ from the last section. The voltage and current waveforms are shown in Fig. 4.21, which indicates the waveform overlap due to the reduced number of harmonics.
Fig. 4.21 Voltage and current drain waveforms of class F PA with up to third harmonics condition.

The design of lumped element harmonic load matching network for the inverse class F PA uses a similar principle as the class F PA. The design schematic is shown in Fig. 4.22.

![Diagram of lump elements harmonic load design for inverse class F PA]

Fig. 4.22 Lump elements harmonic load design for inverse class F PA.
The inverse class F PA requires half sine voltage and square current waveforms through the active device, so block $S_3$ is used to produce a short circuit for the third harmonic and negative reactance at the second harmonic. $C_2$ and $L_2$ create a short circuit at point A for the second harmonic and $L_4$ is used to add a positive reactance in parallel connected with $S_3$ circuit to obtain the predicted infinite impedance. The voltage and current waveforms through drain are shown in Fig. 4.23.

![Waveform Diagram](image)

Fig. 4.23 Voltage and current drain waveforms of inverse class F PA with up to third harmonics.

Based on the model established above, simulations were carried out using ADS by varying $R_{on}$ and using different load harmonic matching networks to obtain the effects on the efficiency. The results are given in Table 4.1.
Table 4.1 Efficiency comparison of class F and inverse class F PAs with $R_{on}$ and harmonics effects

Table 4.1 indicates that the efficiency is reduced with increasing $R_{on}$ as expected. The harmonics also affect the efficiency for both PAs and the effects are reduced with increasing $R_{on}$. For the same $R_{on}$ and harmonics conditions, the efficiency of the inverse class F PA enhances by ~2% to 15% (depending on the value of $R_{on}$) compared to the class F PA.

### 4.6.3 Novel Methods of Harmonic Load Matching Network Design using TL

Instead of lumped elements, which cannot be used for UHF applications, TLM is normally used in PAs design. By using the same principle as in section 4.6.2, the schematic diagram of the class F PA harmonic matching network is shown in Fig. 4.24.
Block $S_2$ indicates a short circuit produced by a 90 degree 50 Ω TL at the second harmonic, which also make a negative susceptance at the third harmonic. To obtain infinite impedance at the third harmonic, short circuit is produced at joint point $A$ by a 90 degree 50 Ω TL working at 6 GHz in block $S_3$. A 135 degree 50 Ω TL working at 6 GHz is connected with the short circuit produced by the joint point $A$. The infinity impedance is obtained with eliminating the susceptance produced by block $S_2$ using that from $S_3$. Using the same topology on the inverse class F PA, the schematic is shown in Fig. 4.25.

A 90 degree, 6 GHz, and 50 Ω open circuit TL in block $S_3$ is adapted to produce a short circuit at third harmonic. A 180 degree, 4 GHz, and 50 Ω short circuit TL is utilized to
make a short circuit at the joint point A. Another TL in S2 is used in connection with the open circuit TL in S3 to produce an infinite impedance effect at the second harmonic. The value obtained is 50 Ω, 30 degree operating at 4 GHz.

4.7 Summary

This chapter reviewed PAs and the output stages were classified as A to F based on the different Q points and θ. The active device of classical A, B, AB, and C PAs work in the linear region and the output current is linearly controlled by the input voltage, but practically the efficiency of these PAs is low or a low output power is produced, which is the trade off. Classes D, E, F and inverse F PAs have high efficiency as the active device behaves as a switch. The objectives of the design were to minimize the voltage and current overlap through the active device and power dissipation. A switch model of active device, which consists of an ideal switch connected with an internal resistance $R_{on}$ was proposed. $R_{on}$ effects on the efficiency were analysed and it was theoretically shown that the efficiency linearly reduced with increasing $R_{on}$. The comparison results showed that the inverse F PA had improved performance over the class F PA with the same $R_{on}$ and harmonic load conditions. The reduction of load harmonics also degraded the efficiency. Simplified and novel methods of the harmonic load matching network with infinite and up to the third harmonic were designed using the lumped elements. Simulation results showed less than 10% efficiency reduction due to using a load matching network with fewer harmonics. Also with higher value of $R_{on}$, the power of harmonics effects became weaker. Finally, the TLM harmonic matching networks were designed for UHF application using the same principle as the lump elements design.
Chapter 5 Investigation and Design of Non-linear Class F and Inverse Class F Power Amplifiers

5.1 Introduction

The linear model of class F and inverse class F PAs were investigated in Chapter 4. The power loss from the internal resistance of a transistor was modelled by a resistor $R_{on}$ and also it was shown that a limited number of load harmonics affected the efficiency [178-183]. In this chapter, the investigation of the power dissipation from the load matching TL is carried out using S parameters. The nonlinear model of active device ATF 33143 is presented using Statz model by the harmonic balance (HB) method [184-186]. In order to obtain predicted voltage and current waveforms through the active device and the determination of the maximum PAE and gain, a novel simplified simulated load/source pull method is proposed. Based on these analysis and results, novel methods for the class F and inverse class F PAs designs are presented.

5.2 Loss Investigation of Harmonic Matching Network using S Parameter

The load harmonic matching network of transmission line model consists of series and shunt connected elements. These power losses in series TLs have been extensively investigated showing that it is proportional to the line length [187]. The shunt stub loss is investigated by Helaoui[188], who presented a good solution by using a microstrip open stub based network and gave a numerical method to calculate the power loss. In this
section, a novel method to investigate and model the power dissipation of the shunt element caused by impedance using mathematically modelling and S parameter measurement is proposed. In order to simplify the design, PCB FR4 has been chosen as substrate of 50 Ω TLs where the height is 1.575 mm.

5.2.1 Loss Investigation of Impedance Effects of Shunt Stub using $S_{21}$ Parameter

To investigate the impedance effects of the loss for the harmonic load network, a shunt microstrip stub parallel with a load $R_{o2}$ and its equivalent circuit are proposed in Fig. 5.1.

![Diagram of microstrip open/short shunt stub network and equivalent model](image)

Fig. 5.1 Microstrip open/short shunt stub network and equivalent model.
The resistance $R$ and an ideal lossless TL are used to model the shunt stub where $Z_{st}$ is the input impedance looking into the stub. To ensure that the circuit is matched with no power being reflected back to the source $R_{01}$ and $X_s$ are added to the circuit with the impedance $Z_s = Z_{in}^*$ where $Z_{in} = R_{in} + jX_{in}$. The power obtained by the load $P_L$ and the power available from the source $P_a$ can be defined as:

$$P_L = \frac{1}{2} Re\{V \ast I_2^*\} = \frac{|V|^2}{2} \ast \frac{1}{R_{02}},$$

(5.1)

$$P_a = \frac{1}{2} Re\left\{\frac{|V|^2}{Z_{in}}\right\} = \frac{|V|^2}{2} \ast \frac{R_{in}}{|Z_{in}|^2}.$$  

(5.2)

The power dissipated by the impedance effect from the shunt microstrip stub over the total power input can be expressed by:

$$\frac{P_{diss}}{P_a} = 1 - \frac{P_L}{P_a} = 1 - \frac{|Z_{in}|^2}{R_{in}R_{02}}.$$  

(5.3)

Considering a two port network by replacing the source and load by two ports, the transmission parameter $S_{21}$ could be derived from (2.27) which is given by:

$$S_{21} = \frac{2I_2\sqrt{R_{01}R_{02}}}{E_1}.$$ 

Since $R_{in} = R_{01}$, and $R_{02} = 50 \, \Omega$, then (2.27) could be written as:

$$S_{21} = \frac{2I_2\sqrt{50R_{in}}}{E_1}.$$  

(5.4)
Also, \( Z_{in} I_1 = R_{o2} I_2, I_1 = \frac{E}{2R_{in}} \).

So,
\[
Z_{in} E_1 = 2R_{o2} R_{in} I_2,
\]
(5.5)
\[
\frac{2I_2}{E} = \frac{Z_{in}}{R_{o2} R_{in}}.
\]
(5.6)

Hence (2.27) could be deduced as:
\[
S_{21} = \frac{Z_{in} \sqrt{R_{o2} R_{in}}}{R_{o2} R_{in}}.
\]
(5.7)

From (5.7) and the circuit in Fig. 5.1, it is not too difficult to derive the equation for the power through \( |S_{21}|^2 \), which is given by:
\[
|S_{21}|^2 = \frac{|Z_{in}|^2}{R_{in} R_{o2}}.
\]
(5.8)

Equation (5.8) equals to \( \frac{P_L}{P_a} \). Hence, by combining (5.3) and (5.8), \( \frac{P_{diss}}{P_a} \) can be presented as:
\[
\frac{P_{diss}}{P_a} = 1 - \frac{|Z_{in}|^2}{R_{in} R_{o2}} = 1 - |S_{21}|^2.
\]
(5.9)

Using this method, \( \frac{P_{diss}}{P_a} \) could be calculated and measured by \( S_{21} \). The comparative results are shown in Fig. 5.2.
Fig. 5.2 Ratio of power dissipated over power available \( \frac{P_{\text{dist}}}{P_a} \) in terms of electrical length.

The calculated and simulated results are in good agreement for both open and short circuit shunt stub conditions.Due to the short circuit effect brought by the impedance provided by the stubs, most of the power dissipation are at 90 degree and 180 degree for open and short circuits, respectively.

To investigate how \( R \) varies with the length of the stub, it is assumed that the input impedance of the shunt stub \( Z_{st} = R + jX \). \( X = Z_0 / \tan \theta \) and \( X = Z_0 \tan \theta \) are the calculations for the open circuit and short circuit shunt stubs, respectively. \( R \) could be determined in terms of the stub length \( \theta \) as plotted in Fig. 5.3.
Fig. 5.3 Resistance $R$ varies with shunt stub length.

$R$ is almost independent of the length of the shunt stub. However it increases rapidly when the open circuit stub approaches 0 and 180 degrees and the short circuit stub approaches 90 degrees. At these lengths, the reactance $X$ approaches a maximum value (at these points, $X$ will be infinity and value of $R$ could be ignored).

### 5.2.2 Practical Measurement for Shunt and Series Connected Lines

In order to verify the loss investigation results obtained by section 5.2.1, the circuit shown in Fig. 5.4 is used to measure the shunt stub loss and also a series line loss using the S parameter.
Fig. 5.4 (a) Theoretical circuit model used to calculate shunt connected loss of ML, and (b) a practical board.

Fig. 5.4(a) shows an ideal transmission through line connected with two parallel shunt circuits, which are modelling the shunt lines in Fig. 5.4(b). The matching network is used to match the total circuit to 50 Ω for measurement. The discontinuity line in Fig. 5.4(b) is used to test the T-junction effects for the total circuit. The series loss is tested by a group of
series 50 $\Omega$ MLs (0-80mm) and the measured power loss compared to the theoretical results are shown in Fig. 5.5(b), which are also in good agreement.

Fig. 5.5 (a) Practical design of 0 – 80 mm ML, and (b) power dissipation ratio vs. the physical length.
The total comparison results shown in table 5.1 indicate that the discontinuity of T-junction has little effect. The predicted and measured total power dissipation applied to the series and shunt lines are 33.6% and 31.7%, respectively which are in good agreement.

<table>
<thead>
<tr>
<th></th>
<th>Theoretical</th>
<th>Practical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shunt</td>
<td>22.00%</td>
<td>20.00%</td>
</tr>
<tr>
<td>Series with T</td>
<td>11.74%</td>
<td>11.8%</td>
</tr>
<tr>
<td>Series without T</td>
<td>11.60%</td>
<td>11.70%</td>
</tr>
<tr>
<td>Total</td>
<td>33.60%</td>
<td>31.70%</td>
</tr>
</tbody>
</table>

Table 5.1 Comparison data of theoretical and practical results.

5.3 Characteristics of Nonlinear Device Model

The nonlinear modelling is essential for the PA design using the computer design method, which provides accurate and valuable design parameters for the final practical fabrication. The nonlinear device used for the design in this thesis is ATF 33143 and its large signal modelling is given in Fig. 5.6.
Fig. 5.6 Nonlinear model of low noise pHEMT ATF 33143 (Large figure is shown in appendix).

The manufacturing parameters of ATF 33143 are used in the Statz model and this nonlinear model is simulated by ADS, with characteristics of $I_{ds} - V_{gs}$ and $I_{ds} - V_{ds}$ curves shown in Fig. 5.7 and Fig. 5.8.
Fig. 5.7 $I_{ds} - V_{g}$ characteristics of ATF33143.

Fig. 5.8 $I_{ds} - V_{ds}$ characteristic of ATF 33143.

Fig. 5.7 indicates that the pinch off voltage $V_p$ is -0.9 V with $V_{ds}$ varied from 0 to 10 V. $v_k$ is ~0.5 V with $V_g$ varies from -1 to 0 V. The $I_{ds} - V_{ds}$ characteristic of ATF 33143 indicates that the internal resistance is equal to 2 $\Omega$, and the optimum load impedance $R_L$ calculated using (4.9f) and (4.11f) are 20.372 $\Omega$ and 33.823 $\Omega$ for the class F and inverse class F PAs, respectively.
5.4 Classical Load Pull Method

In order to obtain maximum PAE, the load pull method [189-193] is normally used to obtain the optimum load and the source impedance. The classical block diagram is shown in Fig. 5.9.

![Classical block diagram of load/source pull setup](image)

Fig. 5.9 Classical block diagram of load/source pull setup [194].

The traditional load pull system comprises the signal source, source/load impedance tuners and scalar measurements as the power meter. The source and load tuners are used to adjust the source and load impedances, respectively to obtain the minimum reflected power and the maximum output efficiency. Calibration needs to be carried out to the required accuracy. Should multi – harmonics be required then concatenated tuners could be used, however one option would be handled to use a single passive tuner [195-197]. However, power meters are wideband in nature, which measures both the fundamental and harmonic output power levels. Hence it is difficult to obtain the percentage of power allocated at each frequency. To overcome this problem, a spectrum analyser can be used.
Another method introduced in [194] is shown in Fig. 5.10, which includes a signal source, and impedance tuners with a network analyzer. The network analyzer measures the input and output signals and determines the measurement parameters based on each frequency. So the fundamental and higher harmonics power can be easily separated and measured independently. Also a network analyzer is more accurate than the simple power meter or the spectrum analyzer for practical measurement.

5.5 A Simplified Design Method of Class F PA

The linear model of class F and inverse class F PAs were theoretically investigated with the predicted optimum load impedance to obtain the ideal voltage and current waveforms through the drain. For the nonlinear device, both the source and load harmonic impedances affect the efficiency [198] and the optimum load impedance at the fundamental frequency will change with the modified supply voltage. It is difficult to optimise these impedances at different harmonics to obtain both the maximum efficiency and the wide bandwidth. However, this problem can be solved by using simulation methods based on the nonlinear
Statz modelling of an active device using the HB method. The load and source pull method could be used to obtain the maximum efficiency and to minimize the overlap of voltage and current waveforms of the drain. The basic schematic is shown in Fig. 5.11.

\[ Z_{S1}, Z_{S2}, Z_{S3} \text{ are the source impedances and } Z_{L1}, Z_{L2}, Z_{L3} \text{ are the load impedances at the fundamental frequency, the second, and the third harmonics, respectively. For a class F PA design, the drain voltage and current waveforms are shaped by short circuits for even harmonics, open circuits for odd harmonics and the optimum impedance at fundamental frequency. Also the source harmonic impedances are used to optimise efficiency and gain. The input harmonic control of high efficiency design was proposed in [199-205] indicating that the second harmonic input termination had significant influence on the efficiency and linearity. The rest of this chapter compares the effects of two different harmonic load matching networks on PAE, gain with second and third source harmonic controls. Using the nonlinear TL model, the schematic of the class F PA is depicted in Fig. 5.12.} \]
The harmonic load matching network was proposed in Chapter 4. It has been suggested that the optimum second harmonic of the input impedance of the source for class F PA is close to the short circuit [202, 203]. Hence, a 50 Ω TL is used to make the second harmonic short at the input termination with the simulation results shown in Fig. 5.13 and Fig. 5.14. These figures show the comparison results with and without the second harmonic control at the source termination.
Fig. 5.13 PAE and gain in terms of input power: (a) no input harmonic control, (b) with second harmonic control at input termination.
Fig. 5.14 PAE and gain in terms of frequency: (a) no input harmonic control, (b) with second harmonic control at input termination.
With the second harmonic control the peak PAE is 65%, which is 5% higher than the model without control. For the input power range of 0 to 20 dBm the gain achieved is 10 dB for both models. The bandwidth above 50% PAE level is ~200 – 300 MHz for both models. Another novel class F PA design with the even harmonic short circuit of the load matching network is illustrated in Fig. 5.15.

![Fig. 5.15 Schematic of class F PA with even harmonic short circuit of load matching network.](image)

The ML element connected with the power source \( V_{DD} \) produces even harmonics at the short circuit. Two 50 \( \Omega \), 90 degree TLs operating at 6 GHz produce an open circuit at the third harmonic. The simulated PAE and gain in terms of the input power and frequency with and without the input harmonic control are shown in Fig. 5.16 and Fig. 5.17.
Fig. 5.16 PAE and gain in terms of input power: (a) no input harmonic control, (b) with second harmonic control at input termination.
Fig. 5.17 PAE and gain in terms of frequency: (a) no input harmonic control, (b) with second harmonic control at input termination.
The peak PAE is improved from 69% to 75% by the control of the second harmonic at the input termination. The bandwidth of PAE and gain are also improved considerably. For the non source harmonic control model where the bandwidth of more than 50% PAE is ~500 MHz and the bandwidth of more than 40% PAE is ~2 GHz. With the source impedance at second harmonic short, the bandwidth of PAE over 50% is improved to 2.2 GHz. The gains of both models are over 10 dB and 15 dB for the input power range of 0 – 20 dBm and 1- 3 GHz, respectively.

Consequently, the second harmonic of input termination improves both models. The even harmonics short circuit of the load network has improved performance, which yields about 10% peak PAE improvement.

5.6 A Simplified Design of Inverse Class F PA

For the inverse class F PA design, the harmonic load matching network was proposed in Chapter 4. Using the nonlinear model, the schematic of the design is depicted in Fig. 5.18.

![Fig. 5.18 Nonlinear model of inverse class F PA.](image_url)
Without the source harmonics control, the optimum PAE and the gain are illustrated in Fig. 5.19.

Fig. 5.19 Simulated PAE and gain of the inverse class F PA design without source harmonic control in terms of: (a) input power, and (b) frequency.
From this structure, the maximum PAE obtained is 67% with a 21 dBm input power. The bandwidth of more than 50% PAE is ~600 MHz (from 1.6 GHz to 2.2 GHz) and more than 40% PAE is ~2 GHz (from 0.3 GHz to 2.3 GHz). The gain decreases linearly with the increasing input power with >10 dB gain is obtained between 1.75 GHz and 2.3 GHz frequency range. The short circuit of the second harmonic at the input termination increases the PAE of class F PA, which was well reviewed in [200] and shown experimentally in section 5.5. The inverse class F PA is similar to the class F with the second harmonic behaving as an open circuit (see Fig. 5.20).

![Nonlinear model of inverse class F PA with source harmonics control.](image)

With the condition of open circuit of the second harmonic at the source, the obtained PAE and the gain are shown in Fig. 5.21:
Fig. 5.21 Simulated PAE and gain of the inverse class F PA design with source impedance second harmonic control in terms of: (a) input power, and (b) frequency.
With the control of second harmonic of the source impedance, the peak PAE increases to 75% using 17 dBm input power which is ~7% increase compared with the result carried out by the model without source control. The bandwidth for the 10 dB gain level also increases to 750 MHz. By controlling both the second and third harmonics of the source impedance, the schematic of matching network is illustrated in Fig. 5.22.

![Source matching network of nonlinear model of the inverse class F PA with source control up to third harmonics.](image)

The plots of PAE and the gain in terms of the input power and frequency are depicted in Fig. 5.23.
Fig. 5.23 Simulated PAE and gain of the inverse class F PA design with source impedance second and third harmonic control in terms of: (a) input power, (b) frequency.
By comparing with the model with the second harmonic source control, the results of the model with up to the third harmonic source control show no further improvement. However, the difference is in the peak PAE when the input power is around 20 dBm, which is 16 dBm of the second harmonic control model. To conclude, for both the class F and inverse class F PAs designs, the harmonic load matching network design is the key factor, which affects the voltage and current flow through the active device. PAE is improved with more harmonics controlled by the load matching network but the increased components of matching network will lead to power dissipation from the ML (low pass filtering) [131, 160, 161]. The second harmonic of input termination also improves the PAE and the gain for the class F PA. For the inverse class F design, without source harmonic control circuit, with second harmonic control, and up to the third harmonic control of the source termination circuits are compared and results shown in Fig. 5.19, Fig. 5.21, and Fig. 5.23 indicate that with an open circuit at the second harmonic of the source improve the PAE by up to 75%. This is close to the results of the class F PA with the even harmonics short circuits model.

5.7 Practical Design and Test of Class F PA

In practical designs for the class F PA, ideal TLs are replaced by the MLs and the substrate PCB FR4 is used due to low cost. A T-junction is used to connect MLs for practical design and the load matching network of even harmonics short circuit is utilized to shape the voltage and current waveform flowing through the active device. An 18 Ω resistor is located before the active device for the stability requirement [206-210]. The schematic of ML model is shown in Fig. 5.24.
The PAE and the gain in terms of the input power and frequency are shown in Fig. 5.25. $V_{ds}$ and $I_{ds}$ waveforms through transistor ATF 33143 (see Fig. 5.24) is shown in Fig. 5.26.
Fig. 5.25 PAE and gain of the class F PA design with the ML model in terms of: (a) input power, and (b) frequency.

Fig. 5.26 The $V_{ds}$ and $I_{ds}$ waveform over active device.
By replacing the ideal TL with the lossy ML, the maximum PAE value drops from 75% to 67% due to the power dissipates at the MLs. Square voltage and half sine current waveforms are obtained with little overlaps which are very similar to the predicted results in Chapter 4. The load impedance at fundamental, second and third harmonics are 11.394 + j2.721 Ω, 1.751 + j0.744 Ω, and 542.75 - j31.504 Ω, respectively. The schematic diagram for the class F PA with a T-junction is outlined in Fig. 5.27.

Fig. 5.27 Schematic of the ML model for the class F PA with T-junction.

The simulated $V_{ds}$ and $I_{ds}$ waveform through transistor ATF 33143 (see Fig. 5.27) is depicted in Fig. 5.28.
The printed circuit layouts of the class F PA and the fabricated version are shown in Figs. 5.29(a) and (b), respectively. The dimension of practical board of class F PA is shown in table 5.2.

Fig. 5.29 Footprint mirror layout of class F PA.
Fig. 5.30 Fabricated board of the class F PA.

<table>
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<td>18.89</td>
<td>20</td>
<td>5.5</td>
<td>4</td>
<td>10</td>
</tr>
</tbody>
</table>

Table 5.2 Dimension of fabricated board of class F PA.

The measured and simulated PAE using 2 V $V_{DD}$ (because of the limitation of the transistor, see data sheet of ATF 33143 and also output power of signal generator) are compared in Fig. 5.31 and Fig. 5.32.
Fig. 5.31 Measured and simulated PAE for the class F PA in terms of: (a) input power, and (b) frequency.
Fig. 5.32 Measured and simulated gain for the class F PA in terms of: (a) input power, and (b) frequency.

The peak PAE obtained is ~61% which is 6% less than the results of ML model (with respect to Fig. 5.26) due to the T-junction connection and the loss across the resistor [208]. The square voltage and half sine current waveforms are obtained (see Fig. 5.28) and
overlap is small which is very close to the predicted results given in Chapter 4. The load impedance at the fundamental, second and third harmonics are $15.271 + j3.705 \, \Omega$, $2.44 + j0.331 \, \Omega$, and $323.284 + j175.864 \, \Omega$, respectively which are close to the predicted conditions analysed in Chapter 4. The simulation results are in good agreement with the measured results.

5.8 Practical Design and Test of Inverse Class F PA

Using a lossy ML model instead of the lossless TLM, the schematic of the inverse class F PA is given in Fig. 5.33.

The simulated PAE, the gain in terms of the input power and frequency are shown in Fig. 5.34.
Fig. 5.34 PAE and gain of the inverse class F PA design with the ML model in terms of:

(a) input power, and (b) frequency.
The peak PAE of the ML model for the inverse class F PA is 64% which is 11% lower than the lossless TL model. Over 40% PAE obtained from 1.1 GHz to 2.1 GHz. The gain drop smoothly with the increasing input power, see Fig. 5.34(a). At the frequency domain, the gain drop below 10 dB when the frequency is above 2.45 GHz. Improvement in control of the harmonic load matching network shapes $V_{ds}$ and $I_{ds}$ waveforms (see Fig. 5.33 and Fig. 5.35) with half sine voltage and square current with very little overlaps as theoretical predicted in Chapter 4. For the practical fabrication purpose, The ML model with the T-junction schematic is shown in Fig. 5.36, whereas simulated $V_{ds}$ and $I_{ds}$ waveforms at the transistor is depicted Fig. 5.37.
The printed circuit layouts and the fabricated board version of the inverse class F PA are shown in Fig. 5.38, and Fig. 5.39, respectively. The dimensions of the practical board are given in table 5.3.
Fig. 5.38 Printed circuit layouts of the inverse class F PA.

Fig. 5.39 Fabricated board of the inverse class F PA.

<table>
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<tr>
<th>Unit</th>
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<td>13</td>
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</tr>
</tbody>
</table>

Table 5.3 Dimensions of fabricated board of inverse class F PA.
The measured and simulated results for PAE and the gain in terms of the input power and frequency are illustrated in Fig. 5.40, and Fig. 5.41, respectively.

Fig. 5.40 Measured and simulated PAE for the inverse class F PA in terms of: (a) input power, and (b) frequency.
Fig. 5.41 Measured and simulated gain for the inverse class F PA in terms of: (a) input power, and (b) frequency.

With the T-junction and the resistor loss, 60% peak PAE is obtained at 14 dBm input power, showing a 4% drop compared to the non T-junction and the resistor model. The peak gain is ~12 dB obtained with 14 dBm input power at 2.1 GHz. The $V_{ds}$ and $I_{ds}$
waveforms (see Fig. 5.36 and Fig. 5.37) is shaped and the overlap is minimized because of the effects of load matching network design. The simulated and measured PAE plots are in good agreement, see Fig. 5.41.

5.9 Summary

This chapter investigated the power loss of harmonic matching network. The power dissipation was not only from the internal resistance and non-covered harmonics conditions, but also from the lossy MLs of the harmonic matching network. The MLs of the harmonics matching network were series connected and shunt connected. The series resistance losses of MLs were well reviewed by [187], which was almost linearly increased with increasing length. Also the shunt line was analysed by [188] rigorously. A different model was proposed to analyse the open and short circuit shunt lines with equations derived showing that the $S_{21}$ parameter could be used to measure the power dissipation. The measured results for the short circuit due to the impedance showed that almost all the power was dissipated. Based on the investigation of linear modelling from Chapter 4, the nonlinear model using the transistor ATF 33143 was analysed by the lossless TL and the lossy ML models for UHF applications at around 2 GHz. An even harmonic short circuit load matching network was designed for the class F PA, which had a 6% PAE improvement than the 2nd and 3rd harmonic control models. The harmonic matching network from source termination also improved the performance of PAE for both class F and inverse class F PAs by 5% - 7%. Practical design and measurement were carried out for both class F and inverse class F. ~60% PAE and ~10 dB gain were obtained for both PAs, which were in agreement with ADS simulation results.
Chapter 6 Review and Design of Active Integrated Antenna

6.1 Introduction

In active antennas the radiation element and the active device could be integrated without the need for a matching circuit or connecting cables, which reduces the size and increases the frequency bandwidth. In recent years, the AIA has been rapidly developed using microwave integrated circuit technology and the output or input port of microwave circuit could be free space instead of a traditional 50 Ω interface. In this case, the AIA can integrate certain circuit functions and also build in signal and wave processing capabilities such as: resonators, filters, mixers, and power amplifiers. A typical AIA contains an active device, such as FET or a Gunn diode, and with the radiation element such as dipoles, microstrip patch antennas, bowties, or aperture coupled microstrip antennas. This chapter introduces the history and modelling of AIA. A circular polarized aperture coupled microstrip antenna is modelled and designed as the load of class F and inverse class F PA. Simulations are carried out using ADS software and practical measurements for the circular polarized antenna and AIA are carried out in the anechoic chamber.

6.2 Literature Review of AIA

The active antenna, which consists of a small antenna and an electron tube, was first proposed for the application of radio broadcast receivers at around 1 MHz frequency band [211]. Due to the invention of high frequency transistors, much more attention was
attracted in 1960s and 1970s and some pioneering works were reported in [212-218]. The advantages of implementing the active devices using passive radiating elements helped to improve the performance; such as increasing the efficiency and bandwidth, reducing the size and mutual coupling between the array elements and also improving the noise factors [219]. In the 1980s and 1990s, the AIA was developed by a quasi optical technique [2, 7] which was used to combine the output power from arrays of solid state devices to overcome the combiner loss limitations for millimetre wave frequency use [5, 6]. The innovative designs like practical implementation of microwave and millimetre wave have been developed because it could provide effective solutions for TL power dissipation, limited source power, low antenna efficiency and also low performance phase shifters [1]. Recently, we have seen research in the areas of power combining, beam steering and switching, retro-directive arrays, and high efficiency PA designs. Research of AIA has recently been focussed on integrated antenna oscillators, coupled oscillators and phase control, high efficiency RF front ends, retro-directive arrays and AIA systems. This chapter will focus on the RF front end technologies.

Radisic has proposed three novel methods for AIA designs. A 55% PAE was obtained by using a class B PA working at 2.48 GHz and integrated with a patch antenna with the probe feed method to suppress the second harmonic [220]. The second design used a class F PA integrated with a circular sector patch antenna to obtain a PAE of 63%, which is based on the roots of Bessel function to optimise the power loss for the second and third harmonics [221]. The third method aimed to obtain a broadband response, which used a wide bandwidth slot antenna yielding a peak PAE of 61% and 8% bandwidth over 50% PAE [222]. Also in [223, 224] AIAs were designed using a breakdown voltage active device and circular sector patch antennas. Such AIA designs were used as an output
matching network to obtain the optimum efficiency at the operating frequency. Kim [225] proposed a direct integration method, which obtained a PAE of 67.5% by combining a class F PA with an antenna that provided an optimum impedance at the fundamental frequency, a short circuit at the second harmonic and an open circuit at the third harmonic. A similar method was used by [226] to produce a two layer planar inverted F antenna and the PAE obtained at 1.05 GHz, 1.55 GHz, and 1.8 GHz were 58%, 52%, and 50%, respectively. By using a class E PA, Weiss [227] eliminated the output matching network by using a slot antenna as the harmonic load of PA to achieve 62% of PAE. All these three designs were investigated based on the lossless switch model of an active device. Colantonio [205, 228, 229] investigated the effects of an active device and obtained the optimum load impedance of the fundamental frequency, second and third harmonics. By using an output matching network to transform the second and third harmonics of the patch a maximum PAE of 60% at 5 GHz was achieved.

6.3 Design of AIA

6.3.1 Introduction

The AIA [86, 230-236] is used as the front-end of a transmitter, which normally consists of a PA unit and an antenna unit. High efficiency PA includes the input matching block, active device, harmonic load matching, and fundamental frequency matching blocks that saves power and increase the life of battery. The load of PA can be replaced by antennas. Also space is saved by eliminating the load harmonic matching network of the PA using an antenna that also behaves as the impedance matching function. The basic block diagram of an AIA is shown in Fig. 6.1:
In the following section, the design of a broad band circular polarized ACMA is discussed that was outlined in chapter 5.

### 6.3.2 Design of a Circular Polarized ACMA for AIA Design

The structure and dimension of a broad band circular polarized ACMA is depicted in Fig. 6.2.
To obtain circular polarization, two modes are excited in the square patch by the cross slot in the ground plane, which is fed by a single TL with a 90 degree phase shift. A wide bandwidth of return loss is obtained by supporting the square patch by non metallic screws such that the substrate below the patch is air which has low relative permittivity. Following the design procedure outlined in Chapter 3, the resonant frequency of the patch is slightly higher than the working frequency (2 GHz) so the ‘flat’ imaginary impedance could be obtained. The resonant frequency of the slot is still higher than the working frequency to obtain an almost pure inductance of the impedance to eliminate the capacitance response produced by the patch. The equivalent circuit of this antenna is shown in Fig. 6.3.
Since the two equivalent antennas are connected in series, the open circuit could be used to eliminate the imaginary part of the impedance and the whole antenna would behave as a 50 Ω load. Hence, a matching network is required between the antenna and feed in order to obtain the optimum impedance matching. The fabricated boards are shown in Fig. 6.4:

Fig. 6.4 Practical fabricated boards of the broadband circular polarized ACMA: (a) radiation element, (b) slot, and (c) feed and matching stub.
Using the substrate Duroid 5870 with an 8 mm gap between patch and slot, the simulation and measured results using Agilent Network Analyser N5230A (see Fig. 6.5) are shown in Fig. 6.6:

Fig. 6.5 Agilent Network Analyser N5230A.

![Fig. 6.6 Simulated and measured results for S₁₁.](image)

The bandwidth of $S_{11}$ under -10 dB level is about 350 MHz (1.85 GHz – 2.2 GHz). The simulated results are agreed with measured results.
In order to measure the passive antenna output power and also of AIA, based on the Friis transmission equation (6.1), a conical log spiral antenna (model 3102 from ESCO technologies), see Fig. 6.7 is chosen as the reference antenna with working frequency range of 1 to 10 GHz and a 3-dB gain at 2 GHz.

![Conical log spiral antenna model 3102.](image)

\[
\frac{P_r}{P_t} = G_t G_r \left(\frac{\lambda}{4\pi R}\right)^2
\]

(6.1)

This antenna is left hand circular polarized, which is 38.1 cm long with a diameter of 12.7 cm. Signal generator and power meter are setup to generate RF signal and receive power outside the anechoic chamber separately. The range length \( r \) is designed to meet the Far-Field criterion \( r > \frac{2D^2}{\lambda} \), in which \( D \) is the largest dimension of the source. Axial ratio is the ratio of the major axis to the minor axis of the polarization ellipse which is defined as

\[
\frac{\text{Major axis } (E_{\text{max}})}{\text{Minor axis } (E_{\text{min}})}
\]
Good agreements have been obtained between simulation and measurement results. The accepted gain and the axial ratio (AR) results are also shown in Fig. 6.9 within ~1 dB difference at all frequencies.
Fig. 6.9 Simulated and measured results for: (a) gain, and (b) AR.

The maximum gain at 2.2 GHz is 9 dB and the gain in the frequency range from 1.95 GHz to 2.5 GHz is 8 dB. At the design frequency of 2 GHz the AR is close to 0 dB and the bandwidth below the 3 dB axial ratio is ~100 MHz.
6.3.3 Simulation and Practical Design of AIA using Class F PA

The circuit model of AIA is given in Fig. 6.10 where the high efficiency class F and inverse F PA is investigated in Chapter 5. The load of class F PA is replaced by the circular polarized antenna designed in section 6.3.1, which is an AIA. The S parameter data file of the circular polarized antenna is created by CST software and is used in ADS software for simulation.

![Fig. 6.10 Schematic of AIA by using class F PA.](image)

By replacing the load block by an antenna, the circuit is slightly tuned to make a better match. The bias voltage is -0.9 V and the DC power supply is 2 V. $V_{ds}$ and $I_{ds}$ (see Fig. 6.10) waveforms are shown in Fig. 6.11, illustrating a small amount of overlap between voltage and current.
Fig. 6.11 $V_{ds}$ and $I_{ds}$ waveforms for Fig. 6.10.

The optimum input impedances from the load and source simulated by ADS software are given in table 6.1.

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<td>$Z_{L2}$</td>
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<td>$Z_{L3}$</td>
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</tr>
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</table>

Table 6.1 Load and source impedances (Unit: Ω).
The printed circuits for the class F PA connected to the slot antenna by SMA connector are shown in Fig. 6.12. The comparison of the simulated and measured results of the PAE and the gain of AIA amplifier module are illustrated in Fig. 6.13.

Fig. 6.12 Printed circuits for AIA.

(a)
Due to the losses associated with connectors, and cables, as well as measured errors, the measured peak PAE and the peak gain are ~56% and 12.5 dBm, respectively at the input power of 13 dB. For PAE of 50% the bandwidth is ~ 400 MHz and for the gain of 10 dB the frequency band is from 1.1 GHz to 2.5 GHz.

### 6.3.4 Simulation and Practical Design of AIA using Inverse Class F PA

The schematic circuit diagram of an AIA using the inverse class F PA is shown in Fig. 6.14.
The load of inverse class F PA was replaced by the S parameter data file for simulation. $V_{ds}$ and $I_{ds}$ waveforms are given in Fig. 6.15:

Fig. 6.15 $V_{ds}$ and $I_{ds}$ waveforms for Fig. 6.14.
The optimum input impedances from the load and source simulated by ADS software are given in table 6.2.

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<td>$Z_{L3}$</td>
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</tbody>
</table>

Table 6.2 Load and source impedances (Unit: $\Omega$).

These results are close to the predicted impedance condition for the inverse class F PA as given in Chapter 4. By using the circular polarized antenna as the load of PA, the printed circuits, simulated and measured results of PA section are depicted in Figs. 6.16 and 6.17.

Fig. 6.16 Printed circuit for AIA.
Fig. 6.17 Simulation and measured PAE and gain plots in terms of: (a) the input power, and (b) the frequency.

The peak PAE and the peak gain are 57% and ~12 dB, respectively at the input power of 14 dBm. The frequency band of over 50% PAE is about 300 MHz and over 10 dB gain obtained from 1.6 GHz to 2.3 GHz.
6.4 Summary

This chapter introduced the concept and design of AIA using the microwave integrated circuit technology. The traditional output and input interface were replaced by radiating elements. In addition a number of devices such as resonators, filters, mixers, power amplifiers etc were integrated. A broadband circular polarized aperture coupled microstrip antenna as a front end of AIA and both class F and inverse class F PAs based on the designs given in Chapter 5 were fabricated and tested. For the passive antenna 350 MHz of bandwidth for $S_{11}$ and ~100 MHz for AR were measured. The simulation data for the antenna was used as the optimum load of PAs. About 58 % PAE was achieved for both AIA for different input power values of 13 dBm and 14 dBm for the class F and inverse F designs, respectively. For both designs, the measured gains were in the range of 10 – 12 dB.
Chapter 7 Conclusions and Future Work

7.1 Conclusions

To obtain optimum performance of an AIA, it is essential to fully analyse PA and antenna parts. This thesis investigated an ACMA based on the circuit and TLMs. Research was focused on the turn ratios analysis between feed/slot, and slot/patch. A design procedure was proposed for the ACMA design. Based on these results, a broadband dual frequency ACMA was designed. In order to obtain the optimum performance and minimize the power dissipation of PAs, different types of PAs were reviewed. Switch model class F and inverse class F PAs were analysed using both the linear and non-linear models. Finally, AIAs were designed using the proposed class F and inverse class F PAs by integrating it with a broadband circular polarized ACMA.

In Chapter 1, an introduction and basic review of traditional front-end transmitter and receiver of wireless communication systems were presented and also the limitations were outlined. An AIA was introduced with the advantages of low cost, smaller size, high efficiency, more compact, and easy to integrate with circuit functions as filters, mixer, power amplifier, etc. The motivations, objectives, and contributions of research were proposed.

Chapter 2 reviewed the theories of TLs in terms of primary and secondary parameters. The characteristics of MLs of characteristic impedance, effective relative permittivity, and also the loss factors were analysed in terms of physical structure. The S parameters were reviewed and equations of $S_{21}$ and $S_{11}$ were derived based on unequal source and load impedance. The characteristics of microstrip patch antennas were proposed by different
patch shapes and feed methods. The ACMA was selected to be further analysed due to its independent structure of feed and radiation elements, which was easy to integrate with circuit and array designs for satellite communication application.

Chapter 3 presented the TLM and the design procedure of an ACMA. The radiation element was represented by an array of two radiating slots separated by a TL. The amount of radiation was modelled as a fringing field, which varied in terms of the width of patch, height and effective dielectric constant of substrate. The characteristic impedance and the wavelength of the slot line were reviewed based on Cohn’s analysis. In this work a simplified and novel method was introduced in order to obtain the turns ratio using S parameters, which is based on numerical calculations and simulations. Practical measurement was carried out to verify the predicted results, which showed good agreement. Investigation was also carried out by tuning \( n_p \) in the circuit model to agree with the full wave EM simulation results in terms of the slot lengths and the height of substrate. The results for \( n_p \) agreed well with data published by Jaisson. Finally, a broadband dual frequency dual polarized ACMA was designed with 250 MHz bandwidth, 6.6 dB gain at 1.9 GHz, and 200 MHz bandwidth, 7.2 dB gain at 2.4 GHz.

Chapter 4 introduced a brief review of PAs by classifying them as classical and high efficiency devices. The design equations for Class F and inverse class F PAs were presented for determining the output power, power convert efficiency, and also the optimum load impedance. The effects of internal resistance of the transistor were investigated for the efficiency and the optimum load impedance for both class F and inverse class F PAs. To minimize the voltage and current overlap, harmonic load matching networks were designed using the lumped element and TLMs. The performance of the
linear model of class F and inverse class F PAs were compared in terms of the internal resistance and load harmonics with the inverse class F PA.

Chapter 5 investigated the power loss of the shunt element of ML, which indicated at 90 and 180 degrees of open and short circuit ML, nearly all the power dissipated were due to the short circuit effects. The non linear model of the active device of class F and inverse class F PAs were modelled, and a novel harmonic load matching network for all the even harmonics short circuit for class F PA was used to compare with the inverse class F PA. Similar performance was obtained for the peak PAE and gain which were around 58% and 10 dB.

Chapter 6 presented AIAs design based on the class F and inverse class F PAs investigated in Chapter 5. A broadband circular polarized ACMA design was proposed as the radiating element of the load of PAs. 350 MHz $S_{11}$, 100 MHz AR, and 8.5 dB gain were obtained at 2 GHz centre frequency. The performances for both AIAs were similar which were about 58% PAE and 12 dB gain.

### 7.2 Future Work

The future works of research focus on two parts. First, further improve the gain, efficiency and bandwidth of AIA by eliminating the load matching network of active device. An ACMA can be used as the optimum harmonic load of active device with the function of minimise the power loss of AIA and also enhance the efficiency of radiation. The second suggestion would be further simplification of the circuit model and optimization process of the ACMA using computer aided methods as GA.
7.2.1 Investigation of an AIA without Harmonic Load Matching Networks

The schematic of the proposed design is given in Fig. 7.1.

![Schematic of an AIA without harmonic load matching network.](image-url)

For the microwave, millimetre wave and also photonic applications, the reduction in size of the transmitter or receiver could reduce the power dissipation and also save space for other functional devices [237, 238]. For the class F and inverse class F PAs, the antenna could be directly connected to the power source. However, the antenna has to be designed to include the function of harmonic load matching networks to control the second and third harmonics of the load. To increase the gain of AIA, circular polarized antenna arrays [239-244] can be used for satellite applications. For further reduction in power dissipation, the substrate usage could be more stable, low loss factors such as Duroid 5870, and Duroid 6010, which along with higher cost than PCB FR4.
7.2.2 Optimisation of ACMA using GA

GA is adaptive heuristic search algorithms, which are based on the evolutionary ideas of natural selection and genetics. The pioneer of GA was John Holland in the 1960’s [245] and since then it has been widely used to optimise designs in a variety of engineering fields [246-253]. In further research GA will initially be used to optimise the design of a linear polarised and a circular polarised aperture coupled antenna. Then GA will be used in the design of the load harmonic networks for the high efficiency switch model PAs. Finally in the AIA design the load harmonic networks will be eliminated and GA will be used to optimise AIA to obtain the maximum efficiency. The implementation of the GA flow chart diagram is shown in Fig. 7.2 [245].
The implementation procedure of the GA is defined as:

1. Define the representation (encoding-decoding),
2. Define “fitness” function $F$ (incorporate constraints and objectives),
3. Define the genetic operators (initialization, selection, crossover, mutation, insertion),
4. Execute initial algorithm run (monitor average population fitness and identify best individual),

Fig. 7.2 GA implementation flow chart diagram.
5. The random element of the GA is further enhanced by using a crossover process where a number of bits or genes of selected pairs of chromosomes are exchanged. The iteration of the above process is run until a convergence is obtained to produce an optimum solution. The results obtained in the previous section will be used to ensure that the antenna has the required impedance at the design and harmonic frequencies. This will allow the antenna to be directly connected to the amplifier to realize the AIA having maximum efficiency.

In all of the above investigations selected antennas will be practically realized and tested to support the theoretical designs that have been used.
Reference


[210] G. Collinson and M. Jones, "A Novel Technique for Measuring Small-Signal S-Parameters of an Rf Microwave, Transistor, Power Amplifying Stage for Use in


