Communication-and-Computing Latency Minimization for UAV-Enabled Virtual Reality Delivery Systems

Yi Zhou, Cunhua Pan, Phee Lep Yeoh, Kezhi Wang, Maged Elkashlan, Branka Vucetic, Fellow, IEEE, and Yonghui Li, Fellow, IEEE

Abstract—In this paper, we propose a low-latency virtual reality (VR) delivery system where an unmanned aerial vehicle (UAV) base station (U-BS) is deployed to deliver VR content from a cloud server to multiple ground VR users. Each VR input data requested by the VR users can be either projected at the U-BS before transmission or processed locally at each user. Popular VR input data is cached at the U-BS to further reduce backhaul latency from the cloud server. For this system, we design a low-complexity iterative algorithm to minimize the maximum communications and computing latency among all VR users subject to the computing, caching and transmit power constraints, which is guaranteed to converge. Numerical results indicate that our proposed algorithm can achieve a lower latency compared to other benchmark schemes. Moreover, we observe that the maximum latency mainly comes from communication latency when the bandwidth resource is limited, while it is dominated by computing latency when computing capacity is low. In addition, we find that caching is helpful to reduce latency.

Index Terms—UAV communication, computing, caching, latency minimization, joint optimization.

I. INTRODUCTION

The demand for virtual reality (VR) applications that can create high-definition ultra-immersive VR environments for mobile users has increased significantly in 5G and beyond wireless networks [1,2]. However, due to the low computing capability and finite battery lifetime of VR users, it is extremely challenging for wireless networks to support these computing-intensive and latency-sensitive VR applications. To alleviate computing resource constraints and reduce latency, mobile edge computing (MEC) has emerged as a promising enabler for VR delivery by equipping high-capacity computing resources at the network edge [3,4]. In [5], a task scheduling strategy was proposed to solve a transmission data consumption minimization problem with delay constraint in MEC-enabled VR systems. In [6], by optimizing the bandwidth allocation of the uplink and downlink channels, the authors solved an end-to-end delay minimization problem in a VR mobile social edge network. In [7], the authors proposed an efficient algorithm to minimize the offloading energy consumption under latency and power constraints for augmented reality applications. In [8], an energy consumption minimization framework was developed for a two-tier computing offloading MEC network. In [9], the authors implemented and developed a low-latency management framework for distributed service function chains enabling tactile internet with MEC. In [10], by jointly coordinating the task assignment, computing, and transmission resources among edge devices, multi-layer MEC servers and cloud center, the authors proposed an efficient algorithm that aimed at minimizing the system latency including total computing and transmission time in heterogeneous multi-layer MEC networks. In [11], by jointly optimizing the users’ transmit power, computing capacity allocation, and user association, a latency minimization problem of an MEC system was formulated.

To further reduce latency consumption, caching has been considered for MEC servers to pre-cache popular data files from the cloud servers during off-peak periods [12–14]. By doing so, the backhaul latency for requesting data from the cloud server can be minimized during peak periods. In [12], the authors formulated a joint radio communication, caching and computing decision problem to maximize the average tolerant delay with a given transmission rate constraint in a fog radio access network. In [13], joint caching and computing optimization was proposed to minimize the average transmission rate in MEC-based VR delivery systems. The authors in [14] jointly optimized the computation offloading, content caching and resource allocation such that the total latency consumption is minimized.

Due to its mobility and flexibility, unmanned aerial vehicle (UAV) is an ideal platform to provide high-quality and low-latency transmissions by deploying the UAV in close proximity to serve ground users [15–18]. Different from a ground base station which suffers from highly scattered Rayleigh fading channels, the UAV can exploit a strong line-of-sight (LoS) channel when it is above a certain altitude and the propagation conditions between the UAV and ground users can be approximated as free space. Furthermore, the UAV can be
optimally deployed between the ground users and cloud server to further reduce the transmission and backhaul latency, which is perfectly suitable for latency-sensitive applications. Several papers have addressed the performance of UAV-enabled MEC systems with computing resource constraints [19–21]. In [19], a security maximization UAV-enabled MEC framework was proposed by jointly optimizing the UAV location, users’ transmit power, UAV jamming power, offloading ratio, UAV computing capacity, and offloading user association. The authors in [20] developed a low-complexity power minimization algorithm by jointly optimizing user association, power control, computation capacity allocation and location planning in a MEC network with multiple UAVs. In [21], the UAV trajectory, user association and user offloading ratio were jointly optimized to minimize the maximum latency in UAV-MEC networks. The performance of a UAV-enabled caching system was investigated in [22–24]. In [22], a secure transmission scheme was proposed for a UAV-enabled caching system based on interference alignment. In [23], the UAV location, content caching decision and user association were jointly optimized to maximize the users’ quality-of-experience. In [24], the caching policy, UAV trajectory and file transmission scheduling were jointly optimized in a UAV-enabled network with proactive caching. Notably, no prior works have jointly considered the communication, computing, and caching (3C) performance of UAV systems which is critical for successful low-latency VR delivery, thus motivating this work.

In this paper, we present a novel framework with the aim of minimizing the maximum latency of a UAV-enabled communication, computing and caching VR delivery system as shown in Fig. 1, which consists of one cloud server, one UAV aerial base station (U-BS) equipped with both caching and computing capabilities, and multiple ground VR users with local computing resources. To reduce the traffic burden on the backhaul link and backhaul communication latency, the U-BS caches the most popular input data in its cache container and the data which has not been cached at the U-BS needs to be transmitted from the cloud server via a wireless backhaul link. Moreover, to further reduce latency, the U-BS may choose to process the input data with its computing resource and transmit the projected output data to VR users for display, or send the input data to VR users directly for local computing. We note that compared to [5–7] where a VR delivery system was proposed for ground communications, our work exploits the advantages of UAV communications where the latency consumption can be further reduced by optimizing the UAV location, UAV computing capacity allocation and UAV caching policy. In addition, our work which jointly considers the computing and caching capabilities of UAV-enabled systems is different from other research on UAV communications such as [19–21] and [22–24] which solely focused on either computing or caching capabilities, respectively.

The main contributions of this paper are summarized as follows.

- We formulate a maximum latency minimization problem of a UAV-enabled VR delivery system by jointly optimizing the U-BS location, fronthaul and backhaul bandwidth allocation, computing capacity allocation, data caching policy and computing offloading policy subject to computing, caching and power constraints.

- To solve the non-convex optimization problem, we first apply the block coordinate descent (BCD) method to decouple the original optimization problem into six subproblems and propose a low-complexity algorithm to solve each subproblem alternately. We solve the U-BS location subproblem by applying a successive convex approximation (SCA) on the U-BS data rate. Then, we apply Lagrangian dual decomposition method to efficiently solve the bandwidth and computing capacity allocation subproblems. Finally, we obtain efficient closed-form solutions for the caching and computing policy subproblems.

- Simulation results show that our proposed algorithm achieves a lower latency compared to benchmark strategies and highlight a tradeoff between latency and the primary resource requirements of communication, computing and caching.

The rest of this paper is organized as follows. Section II introduces the UAV-enabled communication, computing and caching VR delivery system model and formulates the joint optimization problem. In Section III, we propose an efficient iterative algorithm to minimize the maximum latency consumption. The effectiveness of our proposed solution is shown through simulation results in Section IV. Finally, we conclude the paper in Section V.

II. System Model

Fig. 1 depicts our proposed UAV-enabled communication, computing and caching VR delivery system with N ground VR users, one U-BS and one ground cloud server, where the set of VR users is denoted as \( \mathcal{N} = \{1, 2, ..., N\} \). We
consider that the U-BS has caching and computing capabilities which enable it to cache the data requested by each VR user from the cloud server via wireless backhaul and compute the data, respectively. Each VR user with computing capability is able to compute the data locally. We assume that all devices are equipped with a single antenna for transmitting or receiving. Due to the long distance and blockages from the cloud server to the VR users, the direct links between them are not applicable.

### A. Computing Model

We assume that the $i$-th VR user has the computationally intensive task $U_i$ to be executed as follows [13]

$$U_i = (I_i, O_i, F_i), \forall i \in \mathcal{N},$$  
(1)

where $I_i$ is the input data in bits of the VR video required by the $i$-th user which is available in the remote cloud server, and may or may not be cached at the U-BS, $O_i = \alpha I_i$ is the output data in bits after being processed at the U-BS or locally with $\alpha \geq 2$ as the ratio of size between $O_i$ and $I_i$ [13], and $F_i$ is the number of CPU cycles for computing one bit of input data $I_i$.

We consider VR projection and rendering in our system and define $a_i = \{0, 1\}, \forall i \in \mathcal{N}$, as the computing policy variable where $a_i = 1$ indicates that the input data $I_i$ required by the $i$-th VR user will be projected at the U-BS. Thus, the U-BS processes the input data and transmits the output data $O_i$ to VR users for display. On the other hand, $a_i = 0$ indicates that the $i$-th VR user decides to compute its data locally, but this user also needs to receive the input data, $I_i$, from the U-BS for calculation. Thus, the fronthaul transmission latency between the U-BS and each VR user is jointly decided by the computing policy, data size, and transmission rate, which is given by

$$t_i^c = a_i \cdot I_i \cdot F_i + (1 - a_i) \cdot I_i \cdot \frac{F_i}{f^\text{local}}, \forall i \in \mathcal{N},$$  
(2)

where $t_i^c$ is the transmission rate between the U-BS and the $i$-th VR user which is shown in (10). The first term in the right-hand-side (RHS) of (2) shows that if the data is computed at the U-BS, the output data $O_i$ after being processed will be transmitted from U-BS to the VR user and the second term means that if the data is computed locally, the U-BS transmits the input data $I_i$ to the VR user for calculation.

The computing latency which depends on computing policy, data size, computing capacity, and the required CPU cycles of the computing data, is given by

$$t_i^e = a_i \cdot \frac{I_i}{r_i} \cdot F_i + (1 - a_i) \cdot \frac{I_i}{r_i} \cdot f^\text{local}, \forall i \in \mathcal{N},$$  
(3)

where $f^\text{local}$ is the local computing capacity at the $i$-th VR user and $f_i$ is the computing capacity of the U-BS assigned to compute the data requested by the $i$-th VR user, which is constrained by a maximum computing capacity given by

$$\sum_{i=1}^{N} a_i f_i \leq f_{\text{max}}.$$  
(4)

We note that if the $i$-th VR user decides to locally compute its data and $a_i = 0$, the U-BS will not allocate any computing capacity to this VR user and $f_i = 0$. We set the first term in the RHS of (3) to zero when $a_i = 0$ and $f_i = 0$.

We model the power consumption at the U-BS for computing the input data requested by the $i$-th VR user as [19]

$$p_i^c = \kappa f_i^3, \forall i \in \mathcal{N},$$  
(5)

where $\kappa$ is the effective switched capacitance on the chip.

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**TABLE I**

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mathcal{N}$</td>
<td>Set of VR users</td>
</tr>
<tr>
<td>$\theta_i$</td>
<td>Fraction of fronthaul bandwidth allocated to the $i$-th VR user</td>
</tr>
<tr>
<td>$\eta_i$</td>
<td>Fraction of backhaul bandwidth allocated for transmitting $I_i$</td>
</tr>
<tr>
<td>$f_i$</td>
<td>Computing capacity of U-BS assigned to the $i$-th VR user</td>
</tr>
<tr>
<td>$c_i$</td>
<td>Caching policy variable</td>
</tr>
<tr>
<td>$a_i$</td>
<td>Computing policy variable</td>
</tr>
<tr>
<td>$p_{uc}, p_c$</td>
<td>Transmit power for the U-BS and cloud server</td>
</tr>
<tr>
<td>$\sigma^2$</td>
<td>Noise spectral density</td>
</tr>
<tr>
<td>$\beta_0$</td>
<td>Reference channel power gain</td>
</tr>
<tr>
<td>$y, w, v$</td>
<td>Horizontal location of the U-BS, the $i$-th VR user and cloud server</td>
</tr>
<tr>
<td>$H_u$</td>
<td>Altitude of U-BS</td>
</tr>
<tr>
<td>$r_i^f$</td>
<td>Fronthaul data rate at the $i$-th VR user</td>
</tr>
<tr>
<td>$r_i^b$</td>
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<tr>
<td>$I_i, O_i$</td>
<td>Input and output data size of the $i$-th VR user</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Ratio of size between $O_i$ and $I_i$</td>
</tr>
<tr>
<td>$F_i$</td>
<td>CPU cycles for computing data $I_i$</td>
</tr>
<tr>
<td>$f^\text{local}$</td>
<td>Local computing capacity at the $i$-th VR user</td>
</tr>
</tbody>
</table>
The total power consumption at the U-BS which consists of transmit power, $p_u$, and computing power should be limited by a maximum budget $p_{\max}$, which is given by

$$ p_u + \sum_{i=1}^{\mathcal{N}} a_i \kappa f_i^2 \leq p_{\max}. $$

\(6\)

B. Caching model

We define $c_i = \{0, 1\}, \forall i \in \mathcal{N}$ as the caching policy variable where $c_i = 1$ represents that the input data requested by the $i$-th VR user has been cached in the U-BS and $c_i = 0$ otherwise. We note that if the U-BS has cached the input data requested by the $i$-th VR user, it can apply the data directly from its cache container. Otherwise, the input data has to be transmitted from the cloud server to the U-BS and the corresponding backhaul latency is given by

$$ t_i^b = (1 - c_i) \cdot \frac{I_i}{r_i}, \forall i \in \mathcal{N}, $$

\(7\)

where $r_i^b$ representing the backhaul rate for transmitting $I_i$ is given in \(12\).

Since different portions of the VR video are viewed by different VR users based on their geographical locations, we assume that the input data required by each VR user is different from each other. Note that the caching storage at the U-BS should be bounded by a maximum budget $c_{\max}$, which is given by

$$ \sum_{i=1}^{\mathcal{N}} c_i I_i \leq c_{\max}. $$

\(8\)

C. Communication Model

Assume that the coordinate of the $i$-th VR user is denoted by $\mathbf{w}_i = (x_i, y_i)^T \in \mathbb{R}^{2 \times 1}, \forall i \in \mathcal{N}$. The U-BS is fixed at altitude $H_u$, which is the minimum altitude required by regulations to avoid building obstacles, and its horizontal location is denoted by $\mathbf{y} = (x_u, y_u)^T \in \mathbb{R}^{2 \times 1}$. For the air-to-ground channel, we adopt a simple channel model where the channel power gains are dominated by the U-BS and the i-th VR user is given as [25, 26]

$$ h_i = \frac{\beta_0}{||\mathbf{y} - \mathbf{w}_i||^2 + H_u^2}, \forall i \in \mathcal{N}, $$

\(9\)

where $\beta_0$ denotes the channel power gain at the reference distance of one meter.

Define $\theta_i \geq 0, \forall i \in \mathcal{N}$ as the fronthaul bandwidth allocation factor which represents the fraction of fronthaul bandwidth that the U-BS allocates to the $i$-th VR user. The achievable data rate at the $i$-th VR user is denoted by $r_i$ in bits/second (bps), which is expressed as

$$ r_i = \theta_i B \log_2 \left(1 + \frac{p_u h_b}{\theta_i B \sigma^2}\right), \forall i \in \mathcal{N}, $$

\(10\)

where $p_u$ is the transmit power at the U-BS, $B$ is the total fronthaul bandwidth, and $\sigma^2$ is the noise spectral density.

Assume that the coordinate of the cloud server is denoted by $\mathbf{v} = (x_c, y_c)^T \in \mathbb{R}^{2 \times 1}$. Then, the channel power gain between the cloud server and the U-BS is given as [25, 26]

$$ h_b = \frac{\beta_0}{||\mathbf{y} - \mathbf{v}||^2 + H_u^2}. $$

\(11\)

We define $\mathcal{N}_{\text{uncached}} = \{i | c_i = 0, \forall i \in \mathcal{N}\}$ as the set of VR users whose input data has not been cached in the U-BS and $\eta_i \geq 0, \forall i \in \mathcal{N}_{\text{uncached}}$ as the backhaul bandwidth allocation factor which represents the fraction of backhaul bandwidth that the cloud allocates to transmit the input data $I_i$ which has not been cached in the U-BS. We note that for the $i$-th VR user whose requested input data $I_i$ has been cached in the U-BS, i.e., $c_i = 1$, the cloud will not allocate any backhaul bandwidth for transmitting $I_i$ and $\eta_i = 0, \forall i \in \mathcal{N}_{\text{uncached}}$. The achievable backhaul data rate for transmitting $I_i$ is denoted by $r_i^b$ in bits/second (bps), which is expressed as

$$ r_i^b = \eta_i B_{\text{back}} \log_2 \left(1 + \frac{p_c h_b}{\eta_i B_{\text{back}} \sigma^2}\right), \forall i \in \mathcal{N}_{\text{uncached}}, $$

\(12\)

where $p_c$ is the transmit power at the cloud server and $B_{\text{back}}$ is the total backhaul bandwidth.

According to (2), (3), (7), (10), and (12), the total latency to complete the task at each VR user is given by

$$ t_i = t_i^r + t_i^c + t_i^b = a_i \left(\frac{O_i}{r_i} + \frac{I_i f_i}{f_{\text{local}}} + \frac{I_i}{r_i} \right) + \frac{(1 - c_i) I_i}{r_i^b}, \forall i \in \mathcal{N}. $$

\(13\)

D. Problem Formulation

We note that the satisfaction of VR experience among all users is dominated by the user who experiences the worst latency. To achieve the fairness among all VR users, we formulate an optimization problem aimed at minimizing the maximum latency among all VR users subject to computing capacity, caching storage and total power constraints. We jointly optimize the U-BS location $\mathbf{y} = \{(x_u, y_u)^T\}$, fronthaul bandwidth allocation $\theta = \{\theta_i, \forall i \in \mathcal{N}\}$, backhaul bandwidth allocation $\eta = \{\eta_i, \forall i \in \mathcal{N}_{\text{uncached}}\}$, computing capacity allocation $f = \{f_i, \forall i \in \mathcal{N}\}$, data caching policy $\mathbf{c} = \{c_i, \forall i \in \mathcal{N}\}$, and computing policy $\mathbf{a} = \{a_i, \forall i \in \mathcal{N}\}$.

The optimization problem can be formulated as

$$ \min_{\mathbf{y}, \theta, \eta, f, c, a} \max_{i \in \mathcal{N}} t_i $$

$$ \text{s.t.} \sum_{i=1}^{\mathcal{N}} a_i f_i \leq f_{\text{max}} $$

$$ \sum_{i=1}^{\mathcal{N}} c_i I_i \leq c_{\max} $$

$$ p_u + \sum_{i=1}^{\mathcal{N}} a_i \kappa f_i^2 \leq p_{\max} $$

$$ a_i = \{0, 1\}, \forall i \in \mathcal{N} $$

$$ c_i = \{0, 1\}, \forall i \in \mathcal{N} $$

$$ \sum_{i=1}^{\mathcal{N}} \theta_i \leq 1 $$

$$ \sum_{i=1}^{\mathcal{N}} \eta_i \leq 1. $$

\(14\)

Define an auxiliary variable $T \triangleq \max_{i \in \mathcal{N}} t_i$ as the maximum latency among all VR users, we can reformulate the original
optimization problem as
\[
\min_{y, \theta, \eta, f, w, c, \epsilon} T
\]
\[
\text{s.t. } a_i \left( O_i \frac{1}{r_i} + \frac{I_i F_i}{r_i} \right) + \left( 1 - a_i \right) \left( \frac{I_i F_i}{r_i} \right) + \left( 1 - c_i \right) I_i \leq T, \forall i \in N
\]
(15b)

where the newly defined constraint (15b) is based on the intrinsic limitation that the latency consumption of each user should be less than its maximum value. Although reformulated, Problem (15) is still a non-convex optimization problem due to the following reasons. First, the optimizing variables for computing policy \(a\) and data caching policy \(c\) are binary integers. Second, even with given \(a\) and \(c\), (15b) is still a non-convex constraint with respect to U-BS location \(y\). Therefore, the main challenge that we will address in the following section is to develop an efficient algorithm to solve the latency optimization problem in (15).

### III. Proposed Latency Minimization Algorithm

In this section, we detail our proposed latency minimization algorithm for UAV-enabled VR delivery systems. To solve Problem (15), we apply the BCD method which alternately optimizes one block of optimization variable in each iteration while keeping other blocks of optimization variables fixed to obtain a high-quality suboptimal solution [15]. Therefore, we can decouple the original optimization problem into six subproblems to solve the U-BS location \(y\), fronthaul bandwidth allocation \(\theta\), backhaul bandwidth allocation \(\eta\), computing capacity allocation \(f\), data caching policy \(c\), and computing policy \(a\) in an iterative manner.

#### A. U-BS Location Subproblem

For any given \(\theta, \eta, f, c, \) and \(a\), the U-BS location of Problem (15) can be optimized by solving the following problem

\[
\min_{y, \omega} T
\]
\[
\text{s.t. } \theta_i \log_2 \left( 1 + \frac{\omega_i}{||y - w_i||^2 + H_2^2}\right) - \eta_i \log_2 \left( 1 + \frac{\gamma_i}{||y - v||^2 + H_2^2}\right) \leq T - \rho_i, \forall i \in N
\]
(16b)

where the constraint (16b) corresponds to (15b), and all the other constraints in (15) are not applicable. In (16), we define \(\zeta_i = \frac{\theta_i}{B \log_2 2}, \gamma_i = \frac{\eta_i}{B \log_2 2}, \) and \(\rho_i = \frac{a_i O_i}{\frac{1}{r_i} + \frac{I_i F_i}{r_i}}, \) \(1 - a_i \frac{I_i F_i}{r_i}\). Note that (16) is a non-convex optimization problem and the non-convexity arises from the logarithm terms. In the following, we first introduce slack variables \(\epsilon, \forall i \in N\) and \(\omega, \forall i \in N_{uncached}\), and reformulate the U-BS location subproblem as

\[
\min_{y, \epsilon, \omega} T
\]
\[
\text{s.t. } \alpha_i O_i + (1 - a_i) I_i \leq T - \epsilon_i, \forall i \in N
\]
(17b)

We note that the constraint (17b) is convex now and the non-convexity of Problem (17) arises from constraints (17c) and (17d). Next, we adopt the SCA technique, where the original function can be approximated by a more tractable expression at a given local point in each iteration [15][19]. We note that \(T_i\) is convex with respect to \(||y - w_i||^2\), thus, a concave lower bound expression \(T^{lb}_i\) can be derived by applying the first-order Taylor expansion with given U-BS location \(y[m]\) in the \(m\)-th iteration, which is given by

\[
T^{lb}_i = \theta_i \log_2 \left( 1 + \frac{\zeta_i}{||y[m] - w_i||^2 + H_2^2}\right)
- \eta_i B_{back} \log_2 \left( 1 + \frac{\gamma_i}{||y[m] - v||^2 + H_2^2}\right)
(18)

We apply a similar approach on \(Z_i\) and the corresponding concave lower bound \(Z^{lb}_i\) is given by

\[
Z^{lb}_i = \eta_i \log_2 \left( 1 + \frac{\gamma_i}{||y[m] - v||^2 + H_2^2}\right)
- \eta_i B_{back} \gamma_i \log_2 \left( 1 + \frac{\gamma_i}{||y[m] - v||^2 + H_2^2}\right)\ln 2.
(19)

With given U-BS location \(y[m]\) and the lower bound expressions in (18) and (19), the U-BS location subproblem can be solved as

\[
\min_{y, \epsilon, \omega} T
\]
\[
\text{s.t. } \alpha_i O_i + (1 - a_i) I_i \leq T - \epsilon_i, \forall i \in N
\]
(20a)

\[
\epsilon_i \leq T - \rho_i, \forall i \in N
\]
(20b)

\[
Z^{lb}_i \geq \epsilon_i, \forall i \in N
\]
(20c)

\[
Z^{lb}_i \geq \omega_i, \forall i \in N_{uncached}
\]
(20d)

We note that Problem (20) is a convex optimization problem and it can be efficiently solved by utilizing mathematical optimization software with the polynomial complexity [27].

#### B. Fronthaul Bandwidth Allocation Subproblem

For any given \(y, \eta, f, c, \) and \(a\), the fronthaul bandwidth allocation of Problem (15) can be optimized by solving the following problem

\[
\min_{\theta, \epsilon} T
\]
\[
\text{s.t. } \theta_i \log_2 \left( 1 + \frac{\epsilon_i}{||y - w_i||^2 + H_2^2}\right) \geq \epsilon_i, \forall i \in N
\]
(21c)

We adopt the SCA technique, where the original function can be approximated by a more tractable expression at a given local point in each iteration [15][19]. We note that \(T_\theta\) is convex with respect to \(||y - w_i||^2\), thus, a concave lower bound expression \(T^{lb}_\theta\) can be derived by applying the first-order Taylor expansion with given U-BS location \(y[m]\) in the \(m\)-th iteration, which is given by

\[
T^{lb}_\theta = \theta_i \log_2 \left( 1 + \frac{\epsilon_i}{||y[m] - w_i||^2 + H_2^2}\right)
- \theta_i B_{f} \log_2 \left( 1 + \frac{\epsilon_i}{||y[m] - w_i||^2 + H_2^2}\right)\ln 2.
(22)

We apply a similar approach on \(T_\theta\) and the corresponding concave lower bound \(T^{lb}_\theta\) is given by

\[
T^{lb}_\theta = \theta_i \log_2 \left( 1 + \frac{\epsilon_i}{||y[m] - w_i||^2 + H_2^2}\right)
- \theta_i B_{f} \log_2 \left( 1 + \frac{\epsilon_i}{||y[m] - w_i||^2 + H_2^2}\right)\ln 2.
(23)

With given U-BS location \(y[m]\) and the lower bound expressions in (22) and (23), the fronthaul bandwidth allocation subproblem can be solved as

\[
\min_{\theta, \epsilon} T
\]
\[
\text{s.t. } \theta_i \log_2 \left( 1 + \frac{\epsilon_i}{||y[m] - w_i||^2 + H_2^2}\right) \geq \epsilon_i, \forall i \in N
\]
(24c)

\[
\epsilon_i \leq T - \rho_i, \forall i \in N
\]
(24b)

\[
\epsilon_i \geq \omega_i, \forall i \in N_{uncached}
\]
(24d)

We note that Problem (24) is a convex optimization problem and it can be efficiently solved by utilizing mathematical optimization software with the polynomial complexity [27].
The partial Lagrangian function of Problem (21) is given by

\[
\min_{\theta, T} \quad T
\]
\[
s.t. \quad \frac{\chi_i}{T - \nu_i} \leq \theta_i \log_2 \left(1 + \frac{p_i h_i}{\theta_i B \sigma^2}\right), \quad \forall i \in \mathcal{N} \tag{21a}
\]
\[
\sum_{i=1}^{N} \theta_i \leq 1, \tag{21b}
\]
\[
\theta_i \geq 0, \forall i \in \mathcal{N}, \tag{21c}
\]
\[
T \geq \nu_i, \forall i \in \mathcal{N}, \tag{21d}
\]
\[
\theta_i \geq 0, \forall i \in \mathcal{N}, \tag{21e}
\]
where \( \nu_i = a_i \frac{L_i^2}{\nu_i} + (1 - a_i) \frac{L_i^2}{\nu_i} + (1 - a_i) I_i \) and \( \chi_i = a_i O_i + (1 - a_i) I_i \). We define \( \theta_i \log_2 \left(1 + \frac{p_i h_i}{\theta_i B \sigma^2}\right) \) \( \leq 0 \) when \( \theta_i = 0, \forall i \in \mathcal{N} \), such that the RHS of (21b) is continuous with respect to \( \theta_i \) over the whole domain. We analyze the convexity of Problem (21) in the following lemma.

**Lemma 1.** Problem (21) is a convex problem.

**Proof.** It can be easily noted that (21a), (21c), (21d), and (21e) are convex terms due to their linearity. Therefore, proving Lemma 1 is equivalent to proving that the constraint (21b) is convex. To show this, we define \( g(x) = x \log_2 \left(1 + \frac{1}{x}\right), x > 0 \), and we have

\[
\frac{\partial^2 g}{\partial x^2} = -\frac{1}{x(x+1)^2} \log 2 < 0, \forall x > 0, \tag{22}
\]
which indicates that \( g(x) \) is a concave function. Thus, we can conclude that the RHS of (21b) is a concave term with respect to \( \theta_i \). Moreover, we note that the left-hand-side (LHS) of (21b) is a convex term with respect to \( T \). Therefore, we show that the constraint (21b) is convex and prove that Problem (21) is a convex problem. \( \square \)

Next, we apply the Lagrange dual decomposition method to solve this convex problem. It can be verified that the Slater’s condition is satisfied for Problem (21), which indicates that the duality gap between (21) and its dual problem is zero [27]. The partial Lagrangian function of Problem (21) is given by

\[
\mathcal{L}(T, \theta, \mu, \epsilon) = T + \sum_{i=1}^{N} \frac{\mu_i \chi_i}{T - \nu_i} + \sum_{i=1}^{N} \left[ \theta_i - \mu_i \theta_i \log_2 \left(1 + \frac{p_i h_i}{\theta_i B \sigma^2}\right) \right] - \epsilon, \tag{23}
\]
where \( \mu = \{\mu_i, \forall i \in \mathcal{N}\} \) and \( \epsilon \) are Lagrangian multipliers associated with constraints (21b) and (21c), respectively. The boundary constraints (21d) and (21e) will be absorbed into the optimal solution in the following. The dual function is given by

\[
f(\mu, \epsilon) = \min_{T, \theta} \mathcal{L}(T, \theta, \mu, \epsilon) \tag{24a}
\]
\[
s.t. \quad \theta_i \geq 0, T \geq \nu_i, \forall i \in \mathcal{N}, \tag{24b}
\]
and the dual problem of (21) is given by

\[
\max_{\mu, \epsilon} f(\mu, \epsilon) \tag{25a}
\]
\[
s.t. \quad \mu \succeq 0, \epsilon \geq 0. \tag{25b}
\]
To derive the primal optimal solution of Problem (21), we apply the Lagrange duality and derive \( f(\mu, \epsilon) \) by solving Problem (24). We note that with given dual variables \( \mu \) and \( \epsilon \), Problem (24) can be decomposed into \( N + 1 \) independent subproblems where one subproblem is for optimizing \( T \) and the other \( N \) subproblems are for optimizing \( \theta_i, \forall i \in \mathcal{N} \). The subproblem for optimizing \( T \) can be formulated as

\[
\min_{T} \quad T + \sum_{i=1}^{N} \frac{\mu_i \chi_i}{T - \nu_i} \tag{26a}
\]
\[
s.t. \quad T \geq \nu_i, \forall i \in \mathcal{N}. \tag{26b}
\]

By setting the first-order derivative of (26a) with respect to \( T \) to zero, we observe that the optimal \( T \) should satisfy

\[
T = \left\{ T \left| \sum_{i=1}^{N} \frac{\mu_i \chi_i}{(T - \nu_i)^2} = 1, \nu_i \right. \right\}, \tag{27}
\]
which can be found by applying the bisection method. Moreover, the subproblem for optimizing \( \theta_i, \forall i \in \mathcal{N} \) can be formulated as

\[
\min_{\theta_i} \quad \theta_i - \mu_i \theta_i \log_2 \left(1 + \frac{p_i h_i}{\theta_i B \sigma^2}\right) \tag{28a}
\]
\[
s.t. \quad \theta_i \geq 0, \forall i \in \mathcal{N}. \tag{28b}
\]

By setting the first-order derivative of (28a) with respect to \( \theta_i \) to zero, we obtain the closed-form expression of the optimal bandwidth allocation as

\[
\theta_i = \left[ \frac{p_i h_i}{B \sigma^2} \left( -\frac{1}{\mathcal{W} \left( -\frac{1}{\exp(1+\frac{\mu_i \chi_i}{\nu_i})} \right)} - 1 \right)^\dagger \right], \tag{29}
\]
where \( [x]^\dagger = \max\{x, 0\} \) and \( \mathcal{W}(x) \) is the Lambert function, which is defined as the inverse function of \( f(x) = x \exp(x) \).

The value of dual variables \( \mu \) and \( \epsilon \) can be determined by the sub-gradient method. The updating procedure can be given by

\[
\mu_i = \left[ \mu_i + \phi \left( \frac{\chi_i}{T - \nu_i} - \theta_i \log_2 \left(1 + \frac{p_i h_i}{\theta_i B \sigma^2}\right) \right) \right], \forall i \in \mathcal{N} \tag{30a}
\]
\[
\epsilon = \left[ \epsilon + \phi \left( \sum_{i=1}^{N} \theta_i - 1 \right) \right]^\dagger, \tag{30b}
\]
where \( \phi > 0 \) is a dynamic step-size sequence, which can be selected by using the typical self-adaptive scheme [18].

We note that in the primal problem of (21), the optimal \( T \) and \( \theta \) can be derived by solving (27) and (29), respectively. Moreover, in the dual problem of (21), the optimal dual variables \( \mu \) and \( \epsilon \) can be found by solving (30a) and (30b), respectively. The details for obtaining the optimal solution to Problem (21) are summarized in Algorithm 1. We note that Problem (24) has been decomposed into \( N + 1 \) subproblems. To solve the subproblem for optimizing \( T \), the complexity of solving (27) via the bisection method is \( O(\log(1/\epsilon)) \) with \( \epsilon \) being the iterative accuracy. To solve each of the \( N \) subproblems, since the closed-from solution has been derived in (29), the complexity for these \( N \) subproblems is \( O(N) \). Moreover, the complexity of updating dual variables is \( O(N) \) according to (30a) and (30b). As a result, the total complexity
of Algorithm 1 is \( O(L_1L_2N^2 \log_2(1/\epsilon)) \), where \( L_1 \) is the number of iterations for outer layer in Algorithm 1 and \( L_2 \) is the number of iterations via the dual method of solving Problem (21).

**Algorithm 1** Fronthaul Bandwidth Allocation Algorithm for Solving Problem (21).

1. Initialize \( \mu \) and \( \iota \).
2. repeat
3. Obtain the optimal \( T \) and \( \theta \) by solving (27) and (29), respectively;
4. Update the Lagrangian multipliers \( \mu \) and \( \iota \) by solving (30a) and (30b), respectively;
5. until The objective function in (21a) converges.

**C. Backhaul Bandwidth Allocation Subproblem**

For any given \( y, \theta, f, c, \) and \( a \), the backhaul bandwidth allocation of Problem (15) can be optimized by solving the following problem

\[
\begin{align*}
\min_{\eta, \iota} \quad & T \\
\text{s.t.} \quad & \frac{I_i}{T - z_i} \leq \eta_i B_{\text{back}} \log_2 \left( 1 + \frac{p_i h_b}{\eta_i B_{\text{back}} \sigma^2} \right), \forall i \in N_{\text{cached}} \\
\end{align*}
\]

(31a)

where

\[
\begin{align*}
\eta_i = 0, \forall i \in N_{\text{cached}}, \quad \text{and} \quad \iota_i = \frac{Q_{\text{cached}}}{c_i} + \frac{L_i F_i}{I_i} + \frac{L_i f_i}{I_i} + \frac{L_i}{I_i} \\
\end{align*}
\]

We set \( \eta_i B_{\text{back}} \log_2 \left( 1 + \frac{p_i h_b}{\eta_i B_{\text{back}} \sigma^2} \right) \leq 0 \) when \( \eta_i = 0, \forall i \in N_{\text{cached}}, \) such that the RHS of (31b) is continuous with respect to \( \eta_i \) over the whole domain. We note that Problem (31) is a convex problem and the proof is similar to that of (21) in Subsection III-B.

As such, we can apply the Lagrangian dual decomposition method to solve Problem (31). We denote \( \lambda = \{ \lambda_i, \forall i \in N_{\text{cached}} \} \) and \( \varsigma = \{ \varsigma_i, \forall i \in N_{\text{cached}} \} \) as Lagrangian multipliers associated with constraints (31b) and (31c), respectively. The boundary constraints (31d) and (31e) will be absorbed into the optimal solution in the following. The partial Lagrangian function of Problem (31) is given by

\[
\mathcal{L}(T, \eta, \lambda, \varsigma) = T + \sum_{i=1}^{N_{\text{cached}}} \frac{\lambda_i I_i}{T - z_i} + \sum_{i=1}^{N_{\text{cached}}} \left[ \varsigma_i - \lambda_i \eta_i B_{\text{back}} \log_2 \left( 1 + \frac{p_i h_b}{\eta_i B_{\text{back}} \sigma^2} \right) \right] - \varsigma.
\]

(32)

The dual function is given by

\[
\begin{align*}
f(\lambda, \varsigma) &= \min_{T, \eta} \mathcal{L}(T, \eta, \lambda, \varsigma) \quad \text{s.t.} \quad \eta_i \geq 0, T \geq z_i, \forall i \in N_{\text{cached}}, \quad \lambda_i = 0, \varsigma \geq 0. \\
\end{align*}
\]

(33a)

(33b)

(34a)

(34b)

To derive the primal optimal solution of Problem (31), we apply the Lagrange duality method and derive \( f(\lambda, \varsigma) \) by solving Problem (33). We note that with given dual variables \( \lambda \) and \( \varsigma \), Problem (33) can be decomposed into \( N_{\text{cached}} + 1 \) independent subproblems where one subproblem is for optimizing \( T \) and the other \( N_{\text{cached}} \) subproblems are for optimizing \( \eta_i, \forall i \in N_{\text{cached}} \). The subproblem for optimizing \( T \) can be formulated as

\[
\begin{align*}
\min_{T} & \quad T + \sum_{i=1}^{N_{\text{cached}}} \frac{\lambda_i I_i}{T - z_i} \\
\text{s.t.} \quad & T \geq z_i, \forall i \in N_{\text{cached}}.
\end{align*}
\]

(35a)

(35b)

By setting the first-order derivative of (35a) with respect to \( T \) to zero, we find that the optimal \( T \) should satisfy

\[
\begin{align*}
T &= \left\{ T \left| T \sum_{i=1}^{N_{\text{cached}}} \frac{\lambda_i I_i}{(T - z_i)^2} = 1, T \geq z_i \right. \right\}.
\end{align*}
\]

(36)

which can be solved by applying the bisection search method. Moreover, the subproblem for optimizing \( \eta_i, \forall i \in N_{\text{cached}} \) can be formulated as

\[
\begin{align*}
\min_{\eta_i} & \quad \varsigma_i - \lambda_i \eta_i B_{\text{back}} \log_2 \left( 1 + \frac{p_i h_b}{\eta_i B_{\text{back}} \sigma^2} \right) \\
\text{s.t.} \quad & \eta_i \geq 0, \forall i \in N_{\text{cached}}.
\end{align*}
\]

(37a)

(37b)

By setting the first-order derivative of (37a) with respect to \( \eta_i \) to zero, we obtain the closed-form expression of the optimal backhaul bandwidth allocation as

\[
\eta_i = \left[ \frac{p_i h_b}{B_{\text{back}} \sigma^2} \left( \frac{1}{\exp \left( \frac{1}{\gamma_i B_{\text{back}} \sigma^2} \right)} - 1 \right) \right]^{-1}. +
\]

(38)

The value of dual variables \( \lambda \) and \( \varsigma \) can be determined by the sub-gradient method. The updating procedure is given by

\[
\begin{align*}
\lambda_i &= \left[ \lambda_i + \phi \left( \frac{I_i}{T - z_i} - \eta_i B_{\text{back}} \log_2 \left( 1 + \frac{p_i h_b}{\eta_i B_{\text{back}} \sigma^2} \right) \right) \right]^{+} \\
\varsigma &= \left[ \varsigma + \phi \left( \sum_{i=1}^{N_{\text{cached}}} \eta_i - 1 \right) \right]^{+}. \quad (39a)
\end{align*}
\]

The procedures for obtaining the optimal solution to Problem (31) is summarized in Algorithm 2. Similar to the complexity analysis in Subsection III-B, we note that the total complexity of Algorithm 2 is \( O(L_3 L_4 N^2 \log_2(1/\epsilon)) \), where \( L_3 \) is the number of iterations for outer layer in Algorithm 2 and \( L_4 \) is the number of iterations via the dual method of solving Problem (31).

**D. Computing Capacity Allocation Subproblem**

We define \( N_{\text{cas}} = \{ i | a_i = 1, \forall i \in N \} \) as the set of VR users who choose to compute their input data at the U-BS. Note that for the VR users who choose to self-execute their tasks, the U-BS will not allocate computing capacity to them and \( f_i = 0, \forall i \notin N/N_{\text{cas}} \). For any given \( y, \theta, \eta, c, \) and \( a \), the computing capacity allocation of Problem (15) can be optimized by solving the following problem

\[
\begin{align*}
\max_{\lambda, \varsigma} \quad & f(\lambda, \varsigma) \\
\text{s.t.} \quad & \lambda \geq 0, \varsigma \geq 0. \\
\end{align*}
\]

(34a)

(34b)
We note that with given dual variables $\tau$, $\delta$, and $\xi$, Problem (42) can be decomposed into $N_{as}$ + 1 independent subproblems where one subproblem is for optimizing $T$ and the other $N_{as}$ subproblems are for optimizing $f_i, \forall i \in N_{as}$. The subproblem for optimizing $T$ can be formulated as

$$\min_{\tau} \quad T \quad \text{s.t.} \quad T + \sum_{i=1}^{N_{as}} \frac{\tau_i I_i F_i}{T - \varpi_i} \geq 1, T \geq \varpi_i, \forall i \in N_{as}. \tag{44a}$$

By setting the first-order derivative of (44a) with respect to $T$ to zero, we observe that the optimal $T$ should satisfy

$$T = \left\{ T \left| \sum_{i=1}^{N_{as}} \frac{\tau_i I_i F_i}{(T - \varpi_i)^2} = 1, T \geq \varpi_i \right\} \right., \tag{45}$$

which can be solved by applying the bisection search method.

Moreover, the subproblem for optimizing $f_i, \forall i \in N_{as}$, can be formulated as

$$\min_{f_i} \quad \delta \kappa f_i^3 + \xi f_i \quad \text{s.t.} \quad f_i \geq 0, \forall i \in N_{as}. \tag{46a}$$

The objective function in (40a) converges.

We denote $\tau = \{\tau_i, \forall i \in N_{as}\}$, $\delta$, and $\xi$ as the Lagrangian multipliers associated with constraints (40b), (40c), and (40d), respectively. The boundary constraints (40e) and (40f) will be absorbed into the optimal solution in the following. The partial Lagrangian function of Problem (40) is given by

$$\mathcal{L}(T, f, \tau, \delta, \xi) = T + \sum_{i=1}^{N_{as}} \frac{\tau_i I_i F_i}{T - \varpi_i} + \sum_{i=1}^{N_{as}} \left( \delta \kappa f_i^3 + \xi f_i - \tau_i f_i \right) + \delta p_u - \delta p_{\text{max}} - \xi f_{\text{max}}. \tag{41}$$

The dual function is given by

$$f(\tau, \delta, \xi) = \min_{T, f} \mathcal{L}(T, f, \tau, \delta, \xi) \tag{42a}$$

s.t. $f_i \geq 0, T \geq \varpi_i, \forall i \in N_{as}, \tag{42b}$

and the dual problem of (40) is given by

$$\max_{\tau, \delta, \xi} \quad f(\tau, \delta, \xi) \tag{43a}$$

s.t. $\tau \geq 0, \delta \geq 0, \xi \geq 0. \tag{43b}$

To derive the primal optimal solution of Problem (40), we apply the Lagrange duality method and derive $f(\tau, \delta, \xi)$ by solving Problem (42). We note that with given dual variables $\tau$, $\delta$, and $\xi$, Problem (42) can be decomposed into $N_{as}$ + 1 independent subproblems where one subproblem is for optimizing $T$ and the other $N_{as}$ subproblems are for optimizing $f_i, \forall i \in N_{as}$. The subproblem for optimizing $T$ can be formulated as

$$\min_{T} \quad T + \sum_{i=1}^{N_{as}} \frac{\tau_i I_i F_i}{T - \varpi_i} \quad \text{s.t.} \quad T \geq \varpi_i, \forall i \in N_{as}. \tag{44b}$$
\[
\begin{align*}
\min_{s,t} & \quad T \quad (49a) \\
\text{s.t.} & \quad g_i + \frac{(1 - c_i)I_i}{r_i} \leq T, \forall i \in \mathcal{N} \quad (49b) \\
& \quad \sum_{i=1}^{N} c_i I_i \leq c_{\text{max}} \quad (49c) \\
& \quad a_i \in \{0,1\}, \forall i \in \mathcal{N}, \quad (49d)
\end{align*}
\]

where \( g_i = a_i \left( \frac{\omega_i}{r_i} + \frac{f_i}{T_r} \right) + (1 - a_i) \left( \frac{I_f}{f_{\text{max}}} + \frac{I_r}{r_i} \right) \). Due to the linearity of the objective function and all constraints, we note that Problem (49) is a binary linear programming.

We first analyze the ideal scenario where the U-BS has a sufficiently large storage capability, i.e., \( c_{\text{max}} \geq \sum_{i=1}^{N} I_i \). In this case, since a lower maximum latency \( T \) might be achieved with a higher \( c_i \) according to (49b), we can easily obtain that the optimal solution for Problem (49) is \( c_i = 1, \forall i \in \mathcal{N} \), i.e., the U-BS has cached the input data requested by all VR users and all requested input data can be directly obtained from the cache container of the U-BS without the backhaul transmission, which significantly reduces the latency by eliminating the backhaul latency for all VR users.

For the general scenario where \( c_{\text{max}} \leq \sum_{i=1}^{N} I_i \), due to the limited storage capability of the U-BS, only specific data which is requested by the VR users with high latency consumption will be pre-cached so that the maximum latency can be reduced via caching. Thus, to minimize the maximum latency \( T \), we first sort the users based on the descending order in terms of \( g_i + \frac{I_f}{f_{\text{max}}} \). Next, we consider the input data required by the user with a higher \( g_i + \frac{I_f}{f_{\text{max}}} \) will be cached at the U-BS with higher priority until the caching constraint cannot be satisfied. To derive the closed-form solution, we define a new indicator set \( S \triangleq \{ s_1, s_2, \ldots, s_N \} \) which is sorted in a descending order in terms of \( g_i + \frac{I_f}{f_{\text{max}}} \), i.e., \( s_1 = \arg \max_{\forall i \in \mathcal{N}} (g_i + \frac{I_f}{f_{\text{max}}}) \) and \( s_N = \arg \min_{\forall i \in \mathcal{N}} (g_i + \frac{I_f}{f_{\text{max}}}) \). We further define the set \( S_0 \triangleq \{ s_1, s_2, \ldots, s_{m-1} \}, m = \min \{ m, \sum_{i=1}^{m} I_{s_i} > c_{\text{max}} \} \).

By following [28], a closed-form expression for the optimal solution of (49) is given as

\[
c_i = \begin{cases} 
0, & \text{if } c_{\text{max}} \leq \sum_{i=1}^{m} I_{s_i} \text{ and } i \notin S_0 \\
1, & \text{otherwise}.
\end{cases}
\]

We note that the complexity for the caching policy subproblem is upper bounded by \( O(N) \) and the actual complexity may be much smaller than this upper bound since the proposed approach may terminate when the caching storage constraint cannot be satisfied.

\[\min_{s,t} \quad T \quad (51a)\]
\[\text{s.t.} \quad a_i v_i + o_i \leq T, \forall i \in \mathcal{N} \quad (51b)\]
\[\sum_{i=1}^{N} a_i f_i \leq f_{\text{max}} \quad (51c)\]
\[p_u + \sum_{i=1}^{N} a_i r_i f_i \leq p_{\text{max}} \quad (51d)\]
\[a_i \in \{0,1\}, \forall i \in \mathcal{N}, \quad (51e)\]

where \( v_i = \frac{\Omega_i}{r_i} + \frac{f_i}{T_r} - \frac{f_{\text{max}}}{r_i} - \frac{I}{r_i} \) and \( o_i = \frac{I_f}{f_{\text{max}}} + \frac{I_r}{r_i} + \frac{(1-c_i)I_f}{f_{\text{max}}} \). We note that Problem (51) is a binary linear programming since the objective function and all constraints are linear.

To solve Problem (51), we first analyze the scenario when \( v_i \geq 0 \). In this case, we observe that a larger \( a_i \) might result in a higher \( T \) according to (51b). Thus, to minimize \( T \), we can easily derive that \( a_i = 0 \) when \( v_i \geq 0 \). This corresponds to the scenario that when the transmission and computing latencies at the \( i \)-th user of local computing is less than that of U-BS processing, the VR user chooses to self-execute its input data to reduce latency.

When \( v_i \leq 0 \), a lower maximum latency consumption might be achieved with a larger \( a_i \) according to (51b). However, due to the computing capacity and power constraints, only specific input data which is requested by the VR users with higher latency consumption will be processed at the U-BS so that the maximum latency can be minimized benefiting from the higher computing capacity at the U-BS. Thus, to minimize the maximum latency \( T \), we first sort the users based on the descending order in terms of \( o_i \). Next, we consider the input data of the user with a higher \( o_i \) will be processed at the U-BS with higher priority until the computing capacity constraint or the power constraint cannot be satisfied. To derive the closed-form solution, we define a new indicator set \( K \triangleq \{ k_1, k_2, \ldots, k_N \} \) which is sorted in a descending order in terms of \( o_i \), i.e., \( k_1 = \arg \max_{\forall i \in \mathcal{N}} o_i \) and \( k_N = \arg \min_{\forall i \in \mathcal{N}} o_i \). We further define the set \( K_0 \triangleq \{ k_1, k_2, \ldots, k_{l-1}, l \} \) where \( l = \min \{ l_1, l_2 \} \) with \( l_1 = \min \{ l_1 : \sum_{i=1}^{l_1} I_{k_i} > f_{\text{max}} \} \) and \( l_2 = \min \{ l_2 : p_u + \sum_{i=1}^{l_2} k_i f_{k_i} > p_{\text{max}} \} \). Similar to the caching policy subproblem, a closed-form optimal solution of Problem (51) with complexity of \( O(N) \) is given as

\[
a_i = \begin{cases} 
1, & \text{if } v_i \leq 0 \text{ and } i \in K_0 \\
0, & \text{otherwise}.
\end{cases}
\]

### G. Proposed Iterative Algorithm

The iterative procedure for solving Problem (15) is summarized in Algorithm 4, where the U-BS location, fronthaul and backhaul bandwidth allocation, computing capacity allocation, data caching policy and computing policy are successively optimized while keeping the other variables fixed until convergence, and the suboptimal solutions to Problem (15) can be obtained. In addition, the derived solution in each iteration will be applied as the input for the next iteration. We note that for U-BS location subproblem, since we only solve the

### F. Computing Policy Subproblem

For any given \( y, \theta, \eta, f, \) and \( c \), the computing policy Problem (15) can be optimized by solving the following problem
According to (53)-(55), we can conclude that
\[ T(y[m], \theta[m], \eta[m], f[m], c[m], a[m]) \geq T(y[m+1], \theta[m+1], \eta[m+1], f[m+1], c[m+1], a[m+1]), \]
which shows that the algorithm yields a non-increasing sequence of the objective value. In addition, the objective value is lower bounded by zero. Hence, our proposed algorithm is guaranteed to converge. Although the obtained solution is generally suboptimal, we validate the effectiveness of our proposed Algorithm 4 in reducing the latency consumption via simulation results by comparing it with other benchmark strategies in Section IV. We note that the complexity of Algorithm 4 is the addition of the complexity in each step [20]. According to the aforementioned complexity analysis of each subproblem, we obtain that the overall complexity of Algorithm 4 is \( O(L_1L_2N^2\log_2(1/\epsilon) + L_3L_4N^2\log_2(1/\epsilon) + L_5L_6N^2\log_2(1/\epsilon) + 2N) \), which shows that the complexity of Algorithm 4 is polynomial in the worst scenario.

IV. Simulation Results

In this section, numerical results are presented to evaluate the performance of our proposed algorithm. We consider \( N = 6 \) VR users that are randomly and uniformly distributed within a 400m \( \times \) 400m square area. We set the altitude of U-BS as \( H_u = 150 \) m. The channel power gain is set as \( \beta_o = 10^{-5} \). We set the effective switched capacitance at the UAV as \( \kappa = 10^{-27} \) [21]. The noise spectral density is \( \sigma^2 = -169 \) dBm/Hz. The transmit powers at the U-BS and the cloud server are \( p_u = p_c = 0.5 \) W. We consider the input data size \( I_i \) follows a uniform distribution with \( I_i \sim U[10, 15] \) KB, the ratio between \( O_i \) and \( I_i \) is set as \( \alpha = 2 \), and the required number of CPU cycles per bit is distributed as \( F_i \sim U[500, 800] \) cycles/bit. The computing capacity of VR users follows a distribution of \( f_i \sim U[0.5, 1] \) GHz. The maximum computing capacity, power budgets and caching storage of U-BS are set as \( f_{max} = 5 \) GHz, \( P_{max} = 4 \) W, and \( c_{max} = 60 \) KB, respectively. The fronthaul and backhaul bandwidth are \( B = B_{back} = 1 \) MHz.

Fig. 2 shows the convergence behavior of Algorithm 4 with different U-BS altitude \( H_u \). This figure shows that our proposed algorithm quickly converges within 8 iterations. Moreover, we observe that compared to its initial value, the maximum latency reduces by 63.7\% from 47.6 ms to 17.3 ms when \( H_u = 150 \) m, which verifies the effectiveness of our proposed solution.

Fig. 3 shows the initial latency and optimized latency of each VR user where the initial latency is generated based on one set of random realization of input data, computing capacity of each VR user and required number of CPU cycles per bit. It can be seen that our proposed joint optimization solution significantly reduces the maximum latency consumption among all VR users by comparing the initial latency and optimized latency. Moreover, we can see that the optimized latency of each VR user is almost equal, which shows that minimizing the maximum latency among all VR users is equivalent to guaranteeing the fairness among all VR users, so that the minimum quality-of-service can be improved.
In Fig. 4, we plot the maximum latency as a function of maximum computing capacity $f_{\text{max}}$. We compare our proposed Algorithm 4 with the following five benchmark schemes: 1) Fuzzy C-Means Clustering algorithm (FCM) [20]: the U-BS location is optimized based on FCM algorithm and all the other variables are optimized by using Algorithm 4; 2) Equal bandwidth and computing capacity (EBCC): We set $\theta_i = 1/N, f_i = a(i) \ast \min \left( f_{\text{max}}/N_a, \left( \frac{P_{\text{max}} - p_u}{N_a/k} \right)^{1/3} \right), \eta_i = (1 - c(i))/N_{\text{uncached}}, \forall i \in \mathcal{N}$ and all the other variables are optimized by using Algorithm 4; 3) No caching: We set $c_{\text{max}} = 0$ KB and all the other variables are optimized by using Algorithm 4; 4) All offloading: We set $a_i = 1, \forall i \in \mathcal{N}$ and all the other variables are optimized by using Algorithm 4; 5) Binary search: We solve the caching policy and computing policy subproblems by applying the binary search method and all the other variables are optimized by using Algorithm 4. It can be seen that compared to the “Binary search” scheme which has an exponential complexity of $\mathcal{O}(L_1L_2N^2 \log_2(1/\epsilon) + L_3L_4N^2 \log_2(1/\epsilon) + L_5L_6N_a \log_2(1/\epsilon) + 2^{N+1})$, our proposed Algorithm 4 with polynomial complexity achieves the same latency performance, which indicates that our proposed algorithm is stable and computationally efficient. Moreover, Fig. 4 shows that our proposed Algorithm 4 achieves a lower latency compared to other benchmark schemes except the “Binary search” scheme. Interestingly, we find that the performance gap between Algorithm 4 and “All offloading” scheme is significant when $f_{\text{max}}$ is low, while it reduces to 0 when $f_{\text{max}}$ is greater than 6 GHz. This is because when $f_{\text{max}}$ is limited, e.g., $f_{\text{max}} = 1$ GHz, each VR user chooses to project the input data locally to reduce latency and the maximum latency is dominated by the computing latency which occupies 87%. While when $f_{\text{max}} \geq 6$ GHz, the input data requested by all VR users will be processed at the U-BS, resulting in the same performance as “All offloading” scheme.

Fig. 5 shows the maximum latency as a function of maximum power budget $P_{\text{max}}$. It can be seen that our proposed Algorithm 4 achieves the same latency performance compared to the “Binary search” scheme and outperforms all the other baseline solutions. Moreover, we find that the maximum la-
tency first decreases then keeps unchanged with an increasing $P_{max}$. This is because when $P_{max}$ is limited, increasing $P_{max}$ increases the computing resource allocated to process the input data requested by offloading VR users, resulting in a lower computing latency. However, when $P_{max}$ is sufficient, the computing resource allocation is bounded by the maximum computing capacity, which makes the latency unchanged. In addition, we observe that caching is helpful to reduce the latency.

![Maximum latency as a function of fronthaul bandwidth $B$.](image)

In Fig. 6, we plot the maximum latency as a function of fronthaul bandwidth $B$. We observe that our proposed Algorithm 4 achieves the same latency performance compared to the “Binary search” scheme and outperforms all the other baseline. Moreover, we observe that when $B$ is limited, e.g., $B = 0.5$ MHz, the maximum latency can be up to $26.5$ ms and it mainly comes from the transmission latency, which occupies $57\%$. While when $B = 1$ MHz, the maximum latency is $17.3$ ms and the portion of transmission latency reduces to $27\%$.

V. CONCLUSIONS

In this paper, we have presented the maximum latency minimization problem for a UAV-enabled communication, computing and caching VR delivery network. Specifically, we have jointly optimized the the U-BS location, fronthaul and backhaul bandwidth allocation, computing capacity allocation, caching and computing policies. To solve this nonconvex optimization problem, we have proposed an efficient iterative algorithm by applying the block coordinate descent method, the successive convex approximation technique and Lagrangian dual decomposition method. Simulation results demonstrated that our proposed algorithm significantly reduces the latency compared to benchmark schemes. Moreover, it can be seen that the maximum latency is mainly due to the transmission latency when the bandwidth is limited, whereas it is dominated by the computing latency when the computing resource is low. In addition, we showed that caching is helpful to reduce latency. We note that our work can be extended to consider that each VR user will execute multiple computation tasks to address the impact of queueing delay and consider the use of multiple UAVs to address limited battery capacity. Moreover, the extension to a more practical scenario that different VR users may require the same input data would be an interesting future research direction which results in a more-complex optimization problem with multiple possible computing and caching strategies.

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