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Analytical Model to Predict Dilation Behavior of FRP Confined Circular Concrete Columns Subjected to Axial Compressive Loading

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3 Abstract:

Experimental research and real case applications are demonstrating that the use of fiber-reinforced 4 5 polymer (FRP) composite materials can be a solution to substantially improve circular crosssection concrete columns in terms of strength, ductility, and energy dissipation. The present study 6 is dedicated to developing a new model for estimating the dilation behavior of fully and partially 7 8 FRP-based confined concrete columns under axial compressive loading. By considering experimental observations and results, a new relation between secant Poisson's ratio and axial 9 strain is proposed. In order the model be applicable to partial confinement configurations, a 10 confinement stiffness index is proposed based on the concept of confinement efficiency factor. A 11 12 new methodology is also developed to predict the ultimate condition of partially FRP confined concrete taking into account the possibility of concrete crushing and FRP rupture failure modes. 13 By comparing the results from experimental tests available in the literature with those determined 14 with the model, the reliability and the good predictive performance of the developed model are 15 demonstrated. 16

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17 Keywords: FRP confined concrete columns; Full and partial confinement; Dilation behavior; Analytical

18 model; Confinement stiffness index

Notations

A_{eff}	Effectively confined concrete area	V_{con}	Volume of concrete
A_g	Entire concrete area	V_{FRP}	Volume of fibers
c_1	Non-dimensional empirical coefficient	v_s	Secant Poisson's ratio
c_2	Non-dimensional empirical coefficient	$\mathcal{V}_{s,0}$	Initial Poisson's ratio of unconfined concrete
<i>c</i> ₃	Non-dimensional empirical coefficient	$V_{s,max}$	Maximum Poisson's ratio at the critical section
C_4	Non-dimensional empirical coefficient	$V_{s,u}$	Ultimate Poisson's ratio
D	Diameter of circular column	v'_s	Poisson's ratio at the mid-plane of FRP strips
D'	Width of effective confinement area	$v'_{s,max}$	Maximum Poisson's ratio at strip region
E_f	FRP modulus elasticity	W_f	FRP width
f_c	Axial stress corresponding to ε_c	$\mathcal{E}_{\mathcal{C}}$	Axial strain corresponding to σ_c
f_f	FRP confining stress of full system	ε_{c0}	Axial strain corresponding to f_{c0}
f_l	FRP confinement pressure of full system	ε_{cc}	Axial strain corresponding to f'_{cc}
$f_{l,i}$	Confinement pressure at the mid-plane of FRP strips	\mathcal{E}_{CU}	Ultimate axial strain
$f_{l,j}$	Confinement pressure at the critical section	E _{cu,r}	Ultimate axial strain at FRP rupture
f_{c0}	Peak compressive stress of unconfined concrete	E _{cu,c}	Ultimate axial strain at concrete crushing
f'_{cc}	Peak compressive stress of confined concrete	ε_{fu}	Ultimate FRP tensile strain
f'_f	FRP confining stress of partial system	$\varepsilon_{h.P}$	FRP hoop strain in partial confinement
f'_l	Effective confinement pressure	$\mathcal{E}_{h,F}$	FRP hoop strain in full confinement
K_e	Confinement efficiency factor = $k_{\varepsilon} \times k_{\nu}$	$\mathcal{E}_{h,rup}$	FRP hoop rupture strain
k_v	Reduction factor	$\mathcal{E}_{l,i}$	Concrete expansion at the mid-plane of FRP strips
k_{ε}	Reduction factor	$\varepsilon_{l,j}$	Lateral concrete expansion at the critical section
n_f	FRP layer number	$\mathcal{E}_{c,m}$	Axial strain corresponding to v _{s,max}
S_f	Distance between FRP strips	\mathcal{E}_{V}	Volumetric strain
s'	Clear distance between two adjacent steel stirrups	ρ_K	FRP confinement stiffness index
<i>t</i> _f	FRP thickness	$v_{t,eff}$	Effective tangential Poisson's ratio

24 Introduction

It is well-known that the application of fiber-reinforced polymer (FRP) composites to externally confine concrete columns can lead to substantial enhancements in terms of strength, ductility, and energy dissipation, as confirmed by analytical and experimental studies conducted by Shehata *et al.* (2002), Teng and Lam (2002), Xiao and Wu (2003), Berthet *et al.* (2005), Barros and Ferreira (2008), Benzaid and Mesbah (2013), Vincent and Ozbakkaloglu (2015), Shayanfar and Akbarzadeh (2018), and Suon *et al.* (2019).

Real reinforced concrete (RC) columns have always a certain percentage of steel hoops, which 31 ensures some concrete confinement. Therefore, some researchers (Perrone et al. (2009), Mai et al. 32 (2018) and Janwaen et al. (2019)) have demonstrated that the application of FRP strips between 33 existing steel hoops can be a strengthening technique of proper compromise in terms of 34 35 confinement effectiveness and cost competitiveness for this type of structural elements. However, 36 the application of discrete FRP strips might pose less confinement efficiency compared to full confinement configuration, as confirmed by experimental studies conducted by Barros and 37 Ferreira (2008), Zeng et al. (2017, 2018a and 2018b), Wang et al. (2018), Guo et al. (2018 and 38 2019). Barros and Ferreira (2008) experimentally investigated the confinement efficiency in the 39 case of circular RC columns partially confined with different carbon fiber-reinforced polymer 40 (CFRP) configurations. The test results revealed that the axial response of RC columns in terms of 41 42 strength and deformability can be improved by increasing the thickness and the width of the CFRP jacket. The confinement efficiency was also verified to be noticeably dependent on the distance 43 44 between CFRP strips.

To evaluate the effectiveness of a FRP confining system for axial strengthening of concrete columns, several theoretical models have been developed. These models generally can be

categorized in two distinctive groups: design-oriented and analysis-oriented models. In general, 47 the former group provides an estimation of the ultimate axial capacity, whereas the latter 48 determines axial stress at any level of axial strain. A comprehensive review of available models in 49 the literature can be found in Ozbakkaloglu et al. (2013) and Huang et al. (2016). In the analysis-50 oriented models a relationship between concrete lateral expansion (representative of dilation 51 behavior) and axial strain is considered. Consequently, their predictive performance highly 52 depends on the reliability of this relation. In this regard, several analytical models have been 53 proposed to predict dilation behavior of FRP confined concrete. In case of fully confined concrete 54 columns of circular cross section, Mirmiran and Shahawy (1997) proposed a dilation model to 55 56 predict the tangential Poisson's ratio (the rate of change of lateral strain with respect to axial strain as shown in Fig. 1) versus axial strain relation, depending on the confinement stiffness parameter 57 (known as the ratio of confinement pressure over lateral strain). Furthermore, Xiao and Wu (2003) 58 derived a relation between secant Poisson's ratio (the ratio between lateral strain and axial strain, 59 as shown in Fig. 1) and axial strain, which is a function of unconfined concrete compressive 60 strength and confinement stiffness. For fully confined concrete elements of circular cross section, 61 Teng et al. (2007) and Lim and Ozbakkaloglu (2014a) proposed lateral strain versus axial strain 62 relations dependent on the level of confinement pressure. In the case of partial confinement, Zeng 63 et al. (2018a) adopted Teng et al. (2007) dilation model by applying a reduction factor in the 64 65 confinement pressure due to the vertical arching action. It should be noteworthy that the existing dilation models were formulated for fully confined concrete columns and calibrated based on the 66 67 results from experimental tests with this type of specimens, therefore their applicability for partial 68 confining system is, at least, arguable.

69 Regarding the partial confinement system, the concrete at the middle distance between FRP strips, hereafter designated by critical section, would experience more lateral expansion compared to the 70 concrete at the strip regions, as confirmed by Guo et al. (2018 and 2019) and Zeng et al. (2018a). 71 Particularly, for the case of partial confinement configuration with a large distance between FRP 72 strips, the concrete expansion at the strip regions might not be strong enough to considerably 73 activate FRP confining stress (Barros and Ferreira (2008) and Wang et al. (2018)). To the best of 74 75 the authors' knowledge, the impact of non-uniform lateral expansion of concrete on the confinement efficiency has not been addressed comprehensively in the existing formulations. 76 Accordingly, a generalized dilation model applicable for both full and partial confinement 77 78 configurations, considering the effect of non-uniform expansion, is still lacking.

In this study, a new dilation model is developed by considering the confinement stiffness for both full and partial confinement configurations. This model takes into account the influence of nonuniform distribution of concrete lateral expansion on the confinement stiffness. For this purpose, relations between secant Poisson's ratio versus axial strain at critical section and at mid-plane of FRP strips are proposed. Based on the assembled database of test results, available in the literature, of fully and partially FRP confined concrete specimens, the reliability and the good predictive performance of the developed model is demonstrated.

86 Concept of confinement efficiency factor

During axial loading, in a partial confinement system, the vertical arching action between the strips induces concrete regions of different confinement level. Accordingly, the axial compressive stress of a FRP partially confined concrete can be assumed to be carried through two separate components corresponding to the areas where confinement is effective and ineffective. With the determination of the axial stress versus axial strain relationships of each area, the entire uniaxial stress-strain curve of FRP partially confined concrete can be calculated. On the other hand, for the sake of simplicity, a reduction factor is applied to the confinement stress (f_l) acting on the effectively confined area in order to reduce the confinement pressure actuating on the whole crosssection. This reduction factor is generally called "*confinement efficiency factor*, K_e ". Accordingly, the whole cross-section can be assumed to be uniformly subjected to an effective confinement stress $f'_l = K_e \times f_l$.

In the case of steel partially confined concrete, Mander *et al.* (1988) proposed an empirical equation to calculate K_e as A_{eff} / A_g in the determination of confinement characteristics of peak axial stress; where A_{eff} is the effectively confined concrete core area at the critical section (at the middle of the clear distance between two adjacent steel hoops) and A_g is the entire concrete area. Accordingly, assuming a second order parabola function with the vertical arching angle equal to 45° , K_e can be obtained as:

$$K_e = \frac{A_{eff}}{A_g} = \left(\frac{D'}{D}\right)^2 = \left(\frac{D - \frac{s'}{2}}{D}\right)^2 = \left(1 - \frac{s'}{2D}\right)^2 \tag{1}$$

where *D* is the diameter of the column's cross section; *D*' is the diameter of the effectively confined concrete at the critical section; *s*' is the clear distance between two adjacent steel hoops. This approach has been adopted for the case of FRP partially confined concrete, by substituting *s*' in Eq. (1) with s_f (the clear distance between two adjacent FRP strips as shown in Fig. 2) (see *fib* Bulletin No. 14 (2001), CNR-DT 200 (2004), and ACI 440.2R-08 (2008)).

A closer examination of the concept of confinement efficiency factor developed by Mander *et al.*(1988) reveals that this model only empirically addresses the detrimental effect of the vertical

arching action on the confinement pressure at the critical section defined at the middle distance 111 between two consecutive confining materials. However, in partial FRP confinement 112 configurations, the critical section, in addition of the lowest confinement pressure, experiences the 113 maximum concrete lateral expansion, while the lowest concrete expansion occurs at the strip 114 region due to the highest FRP confining pressure. In this regard, the distance between two 115 116 consecutive FRP strips plays a key role for the confinement efficiency of FRP partial configuration. In the case of relatively large distance between FRP strips, the concrete expansion 117 is similar to that of unconfined concrete and it might not be strong enough at the strip regions to 118 considerably activate FRP confining stress (Barros and Ferreira (2008) and Wang et al. (2018)). 119 120 Accordingly, in partial FRP confinement configurations, in addition to the vertical arching action, the impact of concrete lateral expansion should be taken into account on the determination of K_e . 121

122 Concrete lateral expansion

Fig. 2 illustrates a typical concrete column of circular cross section partially confined by FRP 123 strips. The region of the RC column, composed by an influencing width of FRP strip of $w_f/2$ and 124 a clear distance of s_{f} , is assumed representative of a partial confinement region for the 125 determination of axial and dilation behavior of the confined column during axial loading. As 126 shown in Fig. 3a, in a partial confinement configuration, the critical section, at the middle distance 127 between FRP strips, experiences the maximum concrete lateral expansion, $\varepsilon_{l,j}$ (the "j" in the 128 subscript aims to represent the halfway between two adjacent FRP strips). It is noteworthy that the 129 experimental results evidenced that at the stage close to failure, the increase of the concrete lateral 130 strain occurs more rapidly at the mid-height of the unconfined zone as confirmed by Guo et al. 131 (2019). Due to the lack of sufficient experimental results in the literature to reliably evidence the 132

pattern of concrete lateral strain variation between two adjacent strips, in the present study, this 133 pattern was inspired by the pattern of vertical arching action but in the opposite direction 134 (expansion direction), with the strain gradient equal to zero at the critical section. Furthermore, 135 based on the experimental observation reported by Zeng et al. 2018b, a uniform concrete lateral 136 distribution was assumed for the strip zone, evenly subjected to FRP confining stress. As can be 137 seen in Fig. 3a, for a certain $\varepsilon_{l,i}$, concrete at the mid-plane of the FRP strips experiences lower 138 dilatancy ($\varepsilon_{l,i}$) due to the fact that this area is directly subjected to FRP confinement pressure (the 139 "i" in the subscript aims to represent the mid-plain of the FRP strips). Here, k_{e} is defined as the 140 ratio between concrete lateral strain at the strip mid-plane and at the critical section ($k_{\varepsilon} = \varepsilon_{l,i} / \varepsilon_{l,j}$ 141). Accordingly, assuming that lateral (radial) and hoop (circumferential) strains are identical, FRP 142 tensile strain $\varepsilon_{h,P}$ at strip region would be equal to $\varepsilon_{h,P} = \varepsilon_{l,i} = k_{\varepsilon} \varepsilon_{l,j}$ (the "P" in the subscript aims 143 to represent a strain concept in a partial wrapping confinement configuration). In the case of full 144 confinement presented in Fig. 3b, existing models (fib Bulletin No. 14 (2001), CNR-DT 200 145 146 (2004), ACI 440.2R-08 (2008)) assume that the column subjected to axial loading would experience a uniform distribution of lateral expansion $\varepsilon_{l,i} = \varepsilon_{l,j}$ (this simplification is quite 147 acceptable up to the compressive strength of unconfined concrete as evidenced by Guo et al. 148 (2018)). Hence, considering FRP hoop strain $\varepsilon_{h,F} = \varepsilon_{l,j}$ (the "F" in the subscript aims to represent 149 a strain concept in a full wrapping confinement configuration), FRP confining stress f_f is equal 150 to $E_f \varepsilon_{l,j}$. Therefore, at a certain level of $\varepsilon_{l,j}$, the ratio of FRP confining stress in the cases of 151 partial and full configurations, named as f'_f and f_f , respectively, is: 152

$$\frac{f'_{f}}{f_{f}} = \frac{E_{f}\varepsilon_{h,P}}{E_{f}\varepsilon_{h,F}} = \frac{\varepsilon_{l,i}}{\varepsilon_{l,j}} = k_{\varepsilon}$$
(2)

As a result, at a certain level of axial stress f_c (corresponding to ε_c), full and partial confinement 153 configurations generate FRP confining stress equal to f_f and $k_{\varepsilon}f_f$, respectively. In fact, the 154 reduction factor k_{ε} addresses the influence of non-uniform distribution of concrete lateral 155 expansion in the determination of FRP confining stress, and it can be assumed to be a function of 156 the distance between FRP strips, s_f . The maximum value of k_{ε} $(k_{\varepsilon,max})$ is equal to 1 in the case 157 of full confinement with $s_f = 0$, while the minimum value of k_{ε} ($k_{\varepsilon,\min}$) might occur in the case 158 of partially confined concrete with a relatively large s_f , resulting in extensive damage around the 159 critical section (concrete transverse expansibility), and marginal concrete dilation at the two end 160 confined regions. In other words, in the case of relatively large s_f , the critical section can be 161 assumed to behave like unconfined concrete with abrupt increase in expansibility when concrete 162 experiences ultimate axial strain ε_{cu} , leading to a large concrete volumetric expansion, while 163 164 concrete at the mid-plane of the FRP strips remains in the maximum confinement stage. Based on the dilation responses of a series of unconfined concrete specimens tested by Osorio et al. (2013), 165 $\varepsilon_{l,j}$ corresponding to $\varepsilon_{cu} = 0.004$ was assumed to approximately equal to 0.01, inducing an 166 ultimate secant Poisson's ratio $v_{s,u}^{unc} = \varepsilon_{l,j} / \varepsilon_{cu} = 2.5$. Assuming the elastic behavior with initial 167 Poisson's ratio of $v_i = 0.2$ for the concrete located at the mid-plane of FRP strips, $\varepsilon_{l,i}$ would be 168 equal to 0.0008 ($\varepsilon_{l,i} = v_i \varepsilon_{cu}$). Accordingly, for confined concrete with a relatively large s_f , the 169 ratio of concrete expansion at the critical section (assumed as unconfined concrete) and at the mid-170 plane of FRP strip, representative of $k_{\varepsilon} = k_{\varepsilon,min}$, can be calculated as $\varepsilon_{l,i} / \varepsilon_{l,j} = 0.08$, whereas in 171 the case of full confinement with $s_f = 0$, k_{ε} is equal to 1. 172

In the present study, to formulate the relation between k_{ε} and s_{f} , a set of the experimental dilation 173 results reported by Barros and Ferreira (2008), Wang et al. (2018), Zeng et al. (2018a and 2018b) 174 was used. For partially FRP confined concrete specimens with $s_f > 0.75D$, Wang et al. (2018) 175 demonstrated that the FRP confinement effectiveness, even with thick FRP jacket, would be 176 minimal in compliance with the experimental observations reported by Barros and Ferreira (2008). 177 Likewise, according to the failure mode of the test results reported by Zeng et al. (2018a and 178 2018b), for specimens with a relatively large s_f , the concrete between two adjacent FRP strips is 179 highly expected to experience concrete crushing failure, instead of simultaneous FRP 180 rupture/concrete crushing failures. Details of the reported dilation results of the test specimens 181 with a relatively large s_f / D and marginal confinement efficiency (determined as f_{cc}^{exp} / f_{c0}) can 182 be found in Table 1, where f_{cc}^{exp} is the experimental peak axial stress of confined concrete, and 183 f_{c0} is the peak axial stress of unconfined concrete. In this table, $v'_{s,u}^{exp}$ represents the ultimate 184 secant Poisson's ratio at the mid-plane of FRP strips (obtained experimentally as the ultimate ratio 185 of FRP tensile strain $\varepsilon_{h,P}$ recorded by strain gauge and corresponding axial strain ε_c in the 186 column). In the present study, with a slightly conservative assumption, the ultimate secant 187 Poisson's ratio of the test specimens at the critical section, $v_{s,u}^{exp}$, was taken into account equal to 188 2.5, similar to that of unconfined concrete. Then, k_{ε}^{exp} can be calculated as $v'_{s,u}^{exp}/2.5$. 189

Fig. 4 demonstrates the proposed relation between k_{ε} and s_f / D , determined based on the experimental dilation results. As can be seen, k_{ε} can be reasonably assumed to decrease linearly from 1 at $s_f = 0$ (full confinement) to 0.08 at $s_f = D$, as:

$$k_{\varepsilon} = 1 - 0.92 \frac{s_f}{D} \qquad \qquad \text{for } \frac{s_f}{D} \le 1 \tag{3a}$$

$$k_{\varepsilon} = 0.08$$
 for $\frac{s_f}{D} \ge 1$ (3b)

As shown in Fig. 4, for $s_f / D \ge 1$, the dilation response of FRP partially confined concrete tends to be similar to unconfined concrete, since FRP confining stress $f'_f = k_{\varepsilon} f_f$ is not capable of limiting transversal concrete deformation. Furthermore, the proposed relationship between k_{ε} and s_f seems to provide good agreement with the test data.

197 Vertical arching action

Fig. 5 illustrates the uniform and non-uniform distribution of confinement pressure in full and 198 partial confinement arrangements, respectively. For partial arrangements, the maximum and 199 minimum influence of the confinement pressure on the dilation behavior of concrete would occur 200 at mid-plane of FRP strips and at critical section, respectively. Here, $f_{l,i}$ is the confinement 201 pressure generated by FRP confining stress f'_{f} at the strip region. In the present study, due to the 202 nonlinear distribution of confinement pressure in a partial arrangement, a reduction factor k_v is 203 proposed to simulate the confinement distribution as uniform with a constant confinement pressure 204 called "effective confinement pressure" applied on the whole concrete: 205

$$f'_{l} = k_{v} \times f_{l,i} \tag{4}$$

Contrarily, in the case of full confinement, there is a constant distribution of confinement pressure, equal to $f_{l,i} = f_{l,j} = f_l$ developed by FRP confining stress f_f (Fig. 5b). Here, $f_{l,j}$ defines the confinement pressure at the middle height of the column, equal to that at the strip regions. Since confinement pressure is a function of the confining stress (Mander *et al.* 1988), the ratio of confinement pressure in partial $(f_{l,i})$ and full $(f_{l,j} = f_l)$ confinement arrangements can be as:

$$\frac{f_{l,i}}{f_l} = \frac{f'_f}{f_f} \to f_{l,i} = \frac{f'_f}{f_f} \times f_l \tag{5}$$

211 Replacing Eq. (2) into Eq. (5) gives:

$$f_{l,i} = k_{\varepsilon} \times f_l \tag{6}$$

212 Therefore, putting Eq. (6) into Eq. (4), the effective confinement pressure, f'_{l} , would be:

$$f'_{l} = k_{v}k_{\varepsilon}f_{l} = K_{e}f_{l} \tag{7}$$

213 in which

$$K_e = k_v k_\varepsilon \tag{8}$$

where K_e defines the efficiency confinement factor as a function of k_e and k_v , as shown in Fig. 5. Hence, the determination of the reduction factor k_v in Eq. (8) is necessary, as an input parameter for partial confinement arrangements. In this regard, for the case of partial confinement arrangement, considering nonlinear and constant distributions of confinement pressure (Fig. 5a) and, the equilibrium of confinement forces results in:

$$k_{v}f_{l,i}\left(s_{f}+w_{f}\right)D = 2f_{l,i}\frac{w_{f}}{2}D + 2\int_{0}^{s_{f}/2}f_{z}d_{z}dx \rightarrow k_{v} = \frac{f_{l,i}w_{f}D + 2\int_{0}^{s_{f}/2}f_{z}d_{z}dx}{f_{l,i}\left(s_{f}+w_{f}\right)D}$$
(9)

where w_f is the FRP width; f_z and d_z are the functions of FRP lateral pressure and the diameter of effective confinement area, respectively, as shown in Fig. 5a. It should be noted that the diameter of the effective confinement area decreases from D to D' due to arching action, as illustrated in Fig. 5a. In the present study, according to the geometric constraints provided by Eqs. (12) and (13), two separate second order parabola functions for f_z and d_z were assumed in compliance with the vertical arching angle equal to 45° (Mander *et al.* 1988) as:

$$f_z = a_1 x^2 + a_2 x + a_3 \tag{10}$$

$$d_z = b_1 x^2 + b_2 x + b_3 \tag{11}$$

in which

$$f_z(x=0) = f_{l,i} \tag{12a}$$

$$f_z\left(x = \frac{s_f}{2}\right) = f_{l,j} \tag{12b}$$

$$\frac{df_z}{dx}\left(x = \frac{s_f}{2}\right) = 0 \tag{12c}$$

226 and

$$d_z \left(x = 0 \right) = D \tag{13a}$$

$$d_z \left(x = \frac{s_f}{2} \right) = D' = D - \frac{s_f}{2}$$
(13b)

$$\frac{dd_z}{dx}\left(x = \frac{s_f}{2}\right) = 0 \tag{13c}$$

To derive the minimum confinement pressure at the critical section, $f_{l,j}$, as demonstrated in Fig. 5, it was assumed that $f_{l,j} = f_{l,i}$ and $f_{l,j} = 0$ in the cases of confined concrete with $s_f = 0$ and $s_f \ge 2D$, respectively. It should be noted that when $s_f / D = 2$, due to the vertical arching action (assumed as a second order parabola equation with the vertical arching angle equal to 45°), the diameter of effective confined area at the critical section is zero. Consequently, confinement pressure could not restrain concrete expansion at this section. Accordingly, the relationship of $f_{l,j}$

233 and s_f as a second order parabola equation is:

$$f_{l,j} = \left(1 - \frac{s_f}{D} + 0.25 \left(\frac{s_f}{D}\right)^2\right) f_{l,i} \qquad \text{for } \frac{s_f}{D} < 2 \tag{14a}$$

$$f_{l,j} = 0$$
 for $\frac{s_f}{D} \ge 2$ (14b)

According to the geometric constraints (Eqs. (12) and (13)), f_z and d_z equations are:

$$f_{z} = \left[\left(\frac{4}{Ds_{f}} - \frac{1}{D^{2}} \right) x^{2} - \left(\frac{4}{Ds_{f}} - \frac{1}{D^{2}} \right) s_{f} x + 1 \right] f_{l,i}$$
(15)

$$d_{z} = \left[\left(\frac{2}{Ds_{f}} \right) x^{2} - \left(\frac{2}{D} \right) x + 1 \right] D$$
(16)

Introducing Eqs. (15) and (16) into Eq. (9), and then solving the integration leads to:

$$k_{v} = \frac{f_{l,i}w_{f}D + f_{l,i}Ds_{f}\left(1 - \frac{s_{f}}{D} + \frac{13s_{f}^{2}}{30D^{2}} - \frac{s_{f}^{3}}{15D^{3}}\right)}{f_{l,i} \times (s_{f} + w_{f})D}$$
(17)

236 Rearranging Eq. (17) gives:

$$k_{v} = \frac{w_{f} + s_{f} \left(1 - \frac{s_{f}}{D} + \frac{13s_{f}^{2}}{30D^{2}} - \frac{s_{f}^{3}}{15D^{3}}\right)}{s_{f} + w_{f}} \le 1$$
(18)

As a result, Eq. (8) can be rewritten as:

$$K_{e} = k_{v}k_{\varepsilon} = \frac{w_{f} + s_{f} \left(1 - \frac{s_{f}}{D} + \frac{13s_{f}^{2}}{30D^{2}} - \frac{s_{f}^{3}}{15D^{3}}\right)}{s_{f} + w_{f}} \left(1 - 0.92\frac{s_{f}}{D}\right) \qquad \text{for } \frac{s_{f}}{D} < 1$$
(19a)

$$K_{e} = k_{v}k_{\varepsilon} = 0.08 \frac{w_{f} + s_{f} \left(1 - \frac{s_{f}}{D} + \frac{13s_{f}^{2}}{30D^{2}} - \frac{s_{f}^{3}}{15D^{3}}\right)}{s_{f} + w_{f}} \ge 0 \qquad \text{for } \frac{s_{f}}{D} \ge 1$$
(19b)

Based on the preliminary sensitivity analysis of the parameters in Eq. (19), for further simplification, a simplified equation was developed as a linear function of s_f / D and w_f / D as follows:

$$K_e = 0.97 + 0.12 \frac{w_f}{D} - 1.25 \frac{s_f}{D} \le 1 \qquad \text{for } s_f / D < 0.5 \tag{20a}$$

$$K_e = 0.75 + 0.12 \frac{w_f}{D} - 0.79 \frac{s_f}{D} \ge 0.04 \qquad \text{for } 0.5 \le s_f \ / \ D \le 1 \tag{20b}$$

$$K_e = 0.04 - 0.02 \left(\frac{s_f}{D} - 1\right) \ge 0$$
 for $s_f / D \ge 1$ (20b)

Fig. 6 demonstrates analytically the variation of the proposed K_e with s_f / D . As can be seen in Fig. 6a, the good agreement between the results obtained from Eq. (19) and the simplified Eq. (20) confirms the reliability of the simplification. In addition, it highlights the relative higher influence of k_e for the final value of K_e compared to k_v . In Fig. 6b, the comparison of K_e obtained from Eq. (1) developed by Mander *et al.* (1988) with Eq. (20) shows that the proposed model predicts K_e values lower than those determined by Eq. (1). It can be attributed to the consideration of the detrimental effect of k_e , in addition to the vertical arching action, in the determination of the proposed K_e . Furthermore, the results confirm that, for the same s_f / D , the increase of w_f / D does not seem to have significant alteration in K_e .

250 Effective lateral confining pressure

In Fig. 7, the confining action in fully and partially FRP confined concrete columns with circular cross section is schematically represented. As shown in Fig. 7a, for a certain axial stress f_c installed in a full FRP confinement configuration, the corresponding FRP tensile stress, f_f , induces a uniform lateral confinement pressure, f_l , acting on the entire concrete area in contact with the FRP. To derive f_l generated by f_f for a full FRP confinement configuration, the equilibrium of forces in the concrete column at the section A-A shown in Fig. 7a must be assured:

$$f_l\left(s_f + w_f\right)D = 4f_f n_f t_f \frac{w_f}{2} \tag{21}$$

where n_f and t_f are the number of FRP layers and thickness of each layer, respectively. Consequently, rearranging Eq. (21) gives:

$$f_{l} = \frac{2n_{f}t_{f}w_{f}}{\left(s_{f} + w_{f}\right)D}f_{f} = \frac{2n_{f}t_{f}w_{f}}{\left(s_{f} + w_{f}\right)D}E_{f}\varepsilon_{h,F} = \frac{2n_{f}t_{f}w_{f}}{\left(s_{f} + w_{f}\right)D}E_{f}\varepsilon_{l,j}$$
(22)

where E_f is the FRP modulus elasticity. Now if p_f defines the ratio of the volume of fibers, V_{FRP} , to the volume of concrete, V_{con} , then:

$$\rho_{f} = \frac{V_{FRP}}{V_{con}} = \frac{2\pi D n_{f} t_{f} \frac{w_{f}}{2}}{\frac{\pi D^{2}}{4} (w_{f} + s_{f})} = \frac{4n_{f} t_{f} w_{f}}{D (w_{f} + s_{f})}$$
(23)

261 Substituting Eq. (23) into Eq. (22), and then rearranging, yields:

$$f_l = \frac{1}{2} \rho_f E_f \varepsilon_{l,j} \tag{24}$$

262 Therefore, in the case of partial confining system, introducing Eq. (24) into Eq. (7) gives:

$$f'_{l} = \frac{1}{2} K_{e} \rho_{f} E_{f} \varepsilon_{l,j}$$
⁽²⁵⁾

263 On the other hand, considering the secant Poisson's ratio, v_s , at the critical section as $\varepsilon_{l,j} / \varepsilon_c$ (Fig. 264 7b), Eq. (25) results in:

$$f'_{l} = \frac{1}{2} K_{e} \rho_{f} E_{f} v_{s} \varepsilon_{c}$$
⁽²⁶⁾

Accordingly, if ε_c is first specified, then by just addressing the corresponding v_s , effective confinement pressure f'_l can be calculated by Eq. (26). Once its relation with ε_c is available, axial stress, f_c , versus ε_c relationship for fully and partially FRP confined concrete can easily be calculated following the active confinement approach, as recommended by existing analysisoriented models (e.g. Lim and Ozbakkaloglu (2014b)).

270 Dilation response

In this section, the determination of a relation between v_s (corresponding to $\varepsilon_{l,j}$) and the applied axial strain level in the concrete column, ε_c , is performed. For a preliminary evaluation of dilation behavior of fully and partially FRP wrapped concrete, the experimental results reported by Zeng *et al.* (2018a) are analyzed, as shown in Fig. 8. For this purpose, the test specimens wrapped by two FRP layers with different s_f/D are selected. Peak axial compressive stress of unconfined concrete, f_{c0} , was reported as 23.4 MPa. Here, ρ_{K} defines the confinement stiffness index, as recommended by Teng *et al.* (2009) for fully FRP confined circular concrete columns. However, in the present study, this non-dimensional parameter index is extended for the case of partial confinement arrangements by adopting the concept of confinement efficiency factor, as:

$$\rho_{K} = \frac{f'_{l} / \varepsilon_{l,j}}{f_{c0} / \varepsilon_{c0}} = \frac{1}{2} K_{e} \frac{\rho_{f} E_{f}}{f_{c0} / \varepsilon_{c0}}$$

$$\tag{27}$$

280 in which

$$\varepsilon_{c0} = 0.0015 + \frac{f_{c0}}{70000}$$
 (Karthik and Mander (2011)) (28)

281 where f_{c0} is in MPa. Moreover, the volumetric strain, ε_{V} , is expressed as:

$$\varepsilon_{V} = \varepsilon_{c} + \varepsilon_{r} + \varepsilon_{h} = \varepsilon_{c} + 2\varepsilon_{h} = \varepsilon_{c} - 2\varepsilon_{l,j}$$
⁽²⁹⁾

where ε_r and ε_h are the lateral (radial) and hoop circumferential strains, respectively. Tensile 282 strain (ε_h) and volumetric expansion are assumed to be negative, while compressive strain (ε_c) 283 and volumetric compaction are considered positive. It should be noted that for comparison, typical 284 axial and dilation responses of unconfined concrete, determined based on Mander et al. (1988) and 285 Osorio *et al.* (2013), are also presented in Fig. 8. Furthermore, $\varepsilon_V < 0$ and $\varepsilon_V > 0$ mean a concrete 286 volumetric expansion and compaction, respectively, during axial compressive loading, and $\varepsilon_v = 0$ 287 corresponds to the secant Poisson's ratio (v_s) equal to 0.5, where concrete volume is not changing. 288 As shown in Fig. 8a, up to roughly f_{c0} and prior the transition zone, the confined concrete tends 289 to behave similar to the unconfined concrete. In transition stage, concrete experiences a significant 290 stiffness degradation along with an increase in the rate of its lateral expansion, leading to the 291 activation of FRP confining pressure. In the case of unconfined concrete, beyond the transition 292

zone, the volumetric change evolution is suddenly reversed due to the degeneration of micro- into 293 meso- and macro-cracks in concrete, leading to a large volumetric expansion (Figs. 8b and c). On 294 the other hand, for FRP confined concrete, after the transition zone, the activated lateral 295 confinement pressure tends to restrain the concrete lateral expansion. In other words, lateral 296 297 pressure applied by the FRP jacket acts in a way to counteract the tendency of concrete for stiffness 298 degradation (Fig. 8b to d). Accordingly, considering the influence of confinement pressure in counteracting the concrete expansion tendency, the volumetric change can be regarded as a 299 function of the confinement stiffness, ρ_{K} . For the high level of this stiffness factor, due to FRP 300 jacket capability to curtail the concrete expansion, its axial strength and deformability can increase 301 significantly. In this way, FRP confined concrete might fail with experiencing a large volume 302 compaction, as shown in Fig. 8c. However, for low level of ρ_K , confined and unconfined concrete 303 have similar dilation response, due to the insufficient confinement pressure in the former one. 304

A closer look of the dilation behavior of the test specimens with $s_f / D = 0.25$ and 0.44 reveals 305 that the effect of s_f on the confinement stiffness was significant enough to alter the tendency of 306 the volumetric response. In fact, the v_s versus ε_c curve of these specimens in Fig. 8d demonstrates 307 that for $s_f / D = 0.25$, the maximum secant Poisson's ratio ($v_{s,max}$) has occurred at $\mathcal{E}_{c,m} = 0.0067$, 308 above which the FRP lateral pressure has restrained concrete dilation, resulting in a remarkable 309 decrease in v_s . However, for $s_f / D = 0.44$, $v_{s,max}$ occurred at the axial strain of $\mathcal{E}_{c,m} = 0.0136$, 310 311 corresponding to the ultimate concrete axial strain. Accordingly, confinement pressure was not 312 capable of changing the concrete expansion evolution during axial loading. In this case, despite of a slight decrease in v_s corresponding to $\varepsilon_c = 0.009$, the lateral pressure provided by FRP was not 313 enough to continue restraining the concrete dilation response for $\varepsilon_c > 0.011$. 314

315 **Proposed relation of** v_s versus ε_c

316 In this section, the determination of v_s versus ε_c relation for fully and partially FRP confined concrete based on experimental results is performed. For this purpose, a large database consisting 317 of 289 test specimens was collected, whose details can be found in Table 2. This data corresponds 318 to the experimental studies reporting the column dilation behavior available in the literature. 319 Among the tested specimens, 153 specimens were fully FRP confined concrete and 136 specimens 320 were confined by partially wrapping concrete with FRP strips. The criteria considered to select the 321 experimental data available in the literature are as follows: (i) Test specimens subjected to axial 322 compressive loading; (ii) Circular concrete columns without steel hoops/ties; (iii) Test specimens 323 fully/partially confined by FRP; (iii) Availability of experimental FRP hoop strain versus axial 324 strain relation (iv) Fibers oriented 90° with respect to the column longitudinal axis. In the test 325 database, f_{c0} is in the range of 15.8–171 MPa with mean and CoV of 40.1 MPa and 0.59, 326 327 respectively. Types of FRP materials consist of: carbon (CFRP), basalt (BFRP), glass (GFRP) and aramid (AFRP) with E_f ranging 13.6–276 GPa with mean and CoV of 184.3 GPa and 0.4, 328 respectively; $n_f \times t_f$ (total thickness of FRP strips) ranging 0.11-3.78 mm with mean and CoV of 329 0.56 mm and 0.79, respectively; ρ_{K} is in the range of 0.002–0.262 with mean and CoV of 0.037 330 and 0.85, respectively. The experimental $v_{s,max}$ is in the range of 0.25–5.31 with mean and CoV of 331 1.1 and 0.65, respectively. To extract the value of the maximum secant Poisson's ratio, $v_{s,max}$, 332 corresponding to the concrete critical section located in the middle of two adjacent FRP strips from 333 the partially confined tests, experimental $\varepsilon_{h,P}$ versus ε_c relations were firstly converted to $\varepsilon_{l,j}$ 334 versus ε_c relations using Eq. (3). By considering that $v_s = \varepsilon_{l,j} / \varepsilon_c$, the previous relation is 335

transformed into a v_s versus ε_c relation, from which $v_{s,max}$ is determined. As shown in Fig. 8d, the parameter $v_{s,max}$ plays a key role in dilation response of FRP confined concrete.

For further examination, Fig. 9 shows the influence of ρ_{K} on the variation of the experimental 338 $v_{s,max}$ in full and partial concrete confinement arrangements. As can be seen, in the case of fully 339 confined concrete, $v_{s,max}$ decreases considerably with the increase of ρ_K , which means that as 340 higher is ρ_{K} as smaller is the concrete dilation. Fig. 9a evidences that for partially confined 341 concrete, the relation between $v_{s,max}$ and ρ_{K} determined by the proposed approach exhibits almost 342 the same trend with that of full confinement. On the other hand, the relation between $v_{s,max}^*$ and 343 ρ_{K}^{*} is shown in Fig. 9b, where ρ_{K}^{*} denotes the confinement stiffness index derived from the 344 original concept of the confinement efficiency factor, developed by Mander et al. (1988) (it can 345 be calculated by Eq. (27) using K_e in Eq. (1)) and $v_{s,max}^*$ is the maximum secant Poisson's ratio, 346 determined based on $k_{\varepsilon} = 1$ because the impact of concrete expansion distribution was ignored by 347 Mander *et al.* (1988). As can be seen in Fig. 9b, at a certain value of ρ_{K}^{*} , $v_{s,max}^{*}$ of the partially 348 confined specimens seems to be lower than that of full confinement counterpart, especially for low 349 level of ρ_{K}^{*} . It presents better dilation behavior for partial systems, compared to fully confined 350 concrete with same ρ_K^* . This can be attributed to the fact that in the Mander *et al.* (1988) approach, 351 the non-uniform distribution of concrete lateral expansion is not considered in the determination 352 of K_e . 353

Based on the best-fit of the dilation results in the test database, the following equation was derived for determining $v_{s,max}$ from ρ_K and f_{c0} :

$$v_{s,\max} = \frac{0.155}{(1.23 - 0.003f_{c0})\sqrt{\rho_K}} \qquad (f_{c0} \text{ in MPa})$$
(30)

To assess the reliability of this relation, Fig. 10 compares the results obtained from Eq. (30) with those extracted from the experimental tests. The values of the mean, coefficient of variation, CoV, and mean absolute percentage error, MAPE, reported in Fig. 10, evidence the good predictive performance of the proposed equation to estimate the value of $v_{s,max}$ in fully and partially FRP confined concrete.

361 Determination of $v_s / v_{s,max}$ versus ε_c relation

In this section, the relation between $v_s / v_{s,max}$ and ε_c corresponding to dilation behavior at the critical section between strips is derived. Based on dilation responses extracted from the experimental results, the diagram represented in Fig. 11 is proposed to predict the dilation behavior of fully and partially FRP confined concrete columns of circular cross section. In this figure, $\varepsilon_{c,m}$ is the axial strain corresponding to $v_{s,max}$; c_1 , c_2 , c_3 and c_4 are the non-dimensional empirical coefficients depending on the axial strain level and ρ_K . According to the best curve fit of the experimental results by using a back analysis, these parameters were determined as:

$$\varepsilon_{c,m} = 0.0085 - 0.05\rho_K \tag{31}$$

369 and

$$c_1 = 0.75 + 3.85\rho_K < 1.00 \tag{32a}$$

$$c_2 = 0.85 + 1.54\rho_K < 0.95 \tag{32b}$$

$$c_3 = 0.65 + 3.08\rho_K < 0.85 \tag{32c}$$

$$0.5 < c_4 = 0.20 + 9.23\rho_K < 0.80 \tag{32d}$$

$$v_{s,0} = 8 \times 10^{-6} f_{c0}^{2} + 2 \times 10^{-4} f_{c0} + 0.138 \quad (f_{c0} \text{ in MPa})$$
(33)

where $v_{s,0}$ is the initial Poisson's ratio of concrete, determined as recommended by Candappa *et* 370 371 al. (2001). As shown in Fig. 11, the expansion of confined concrete is equal to unconfined concrete up to $\varepsilon_c = \varepsilon_{c0}$ (point A) with $v_s = v_{s,0}$. After which, the development of concrete cracking induces 372 an increase in v_s . Subsequently, concrete secant Poisson's ratio tends to increase from $v_{s,0}$ to 373 $c_1 \times v_{s,max}$, corresponding to $\varepsilon_c = 2\varepsilon_{c0}$ (Mander *et al.* 1988). In this phase, FRP confinement 374 pressure is activated by restraining concrete tendency to dilate. The trend afterward $v_{s,max}$ has been 375 reached, at $\varepsilon_c = \varepsilon_{c,m}$ (point C), is followed by a drop in the rate of concrete lateral expansion until 376 ultimate conditions. 377

To examine the reliability of the proposed relation, its prediction, for different levels of ρ_K , is compared with the experimental results in Fig. 12. It should be noted that the analytical relation in each figure is calculated by adopting the average value of the corresponding interval of ρ_K values. As can be seen in the figure, there is a good agreement between the experimental test and analytical results, confirming the reliability of the proposed design-based formulation represented in Fig. 11.

It would be noteworthy that concrete lateral expansion can be regarded as a function of the development of concrete cracking, and subsequently, of the axial strain ε_c . According to the

experimental observations from Guo *et al.* (2018 and 2019), for $\varepsilon_c \leq \varepsilon_{co}$ (where ε_{co} is the axial 385 strain corresponding to peak stress of unconfined concrete f_{c0}), concrete lateral strain at the mid-386 plane of FRP strips and at the critical section would be virtually identical ($k_{\varepsilon} = 1$) due to marginal 387 cracking. However, the ratio between concrete expansion in these regions, k_{ε} , decreases when 388 $\varepsilon_c \ge 2\varepsilon_{co}$ due to the development of major concrete cracking Guo *et al.* (2018 and 2019)). 389 Considering that $\overline{k_{\varepsilon}}$ defines the ratio of concrete expansion at the mid-plane of FRP strips and at 390 the critical section, by assuming it linearly varies in the $\varepsilon_{c0} \le \varepsilon_c \le 2\varepsilon_{c0}$ interval, it can be calculated 391 392 as:

$$\overline{k_{\varepsilon}} = 1 - \left(1 - k_{\varepsilon}\right) \left(\frac{\varepsilon_{c}}{\varepsilon_{c0}} - 1\right)$$
(34)

On the other hand, considering that v_s defines the dilation response at the critical section, the dilation characteristics at the mid-plane of strips (v'_s) can be determined as:

$$v'_{s} = v_{s,0}$$
 for $\varepsilon_{c} \le \varepsilon_{c0}$ (35a)

$$v_{s,0} \le v'_s = \overline{k_{\varepsilon}} v_s \le k_{\varepsilon} c_1 v_{s,\max}$$
 for $\varepsilon_{c0} \le \varepsilon_c \le 2\varepsilon_{c0}$ (35b)

$$v'_{s} = k_{\varepsilon} v_{s}$$
 for $\varepsilon_{c} \ge 2\varepsilon_{c0}$ (35c)

The upper bound in Eq. (35b), demonstrating secant Poisson ratio v'_s when $\varepsilon_c = 2\varepsilon_{c0}$, was taken into account due to fact that concrete lateral strain, either at the critical section or the mid-plane of strips, increasingly enhances during axial compressive loading.

A parametric analysis was performed to highlight the influence of the key parameter, s_f / D , on the dilation response of FRP partially confined concrete elements. For this purpose, a circular cross

section concrete element with diameter of 150 mm and 300 mm height is assumed. The 400 compressive strength of concrete is considered 23.4 MPa. The values of n_f , t_f , E_f and w_f are 401 taken equal to 2, 0.167 mm, 249.1 GPa and 30 mm, respectively. Fig. 13 demonstrates the 402 variations of $\varepsilon_{l,i}$ and $\varepsilon_{l,i}$ with ε_c for five s_f/D arrangements. As expectably, Fig. 13a shows 403 that at a certain ε_c , the $\varepsilon_{l,j}$ increases remarkably with s_f / D . Likewise, at a certain $\varepsilon_{l,j}$, the 404 corresponding axial strain would substantially decrease when s_f/D increases, especially for high 405 level of ε_c . However, as shown in Fig. 13b, $\varepsilon_{l,i}$ increases significantly with the increase of s_f / D 406 from 0 to 0.5, but for $s_f / D > 0.5$, $\varepsilon_{l,i}$ experiences a noticeable decrease due to the relatively high 407 concrete dilation gradient in the critical region (center part between FRP strips) that leads to a 408 strain release in the FRP confined regions. Fig. 13c compares $v_{s,max}$ and $v'_{s,max}$ (maximum secant 409 Poisson's ratio at the critical and mid-plane of strips, respectively) at the various levels of s_f / D . 410 It evidences that $v_{s,max}$ exponentially rises when s_f / D increases, since according to Eq. (30) ρ_K 411 decreases with the increase of s_f / D , which confirms the results presented in Fig. 13a. In case of 412 $v'_{s,max}$, it increases with s_f/D up to a certain level, above which it starts decreasing, by confirming 413 the results presented in Fig. 13b. This tendency can be attributed to the effect of s_f/D on k_{ε} , as 414 represented by Eq. (3) and Fig. 4, as a key parameter to determine dilation behavior at the strip 415 region (Eq. (35)). Accordingly, increasing s_f / D , in one hand, can induce an increase in $v_{s,max}$, 416 and on the other hand, a reduction in k_{ε} . Decreasing in $v'_{s,max}$ for $s_f / D > 0.75$ shows that concrete 417 lateral expansion at the mid-plane of FRP strip is becoming marginal, leading to a significant 418 increase in the difference between $v_{s,max}$ and $v'_{s,max}$, as highlighted by considering the relation 419

between Δv_s and s_f / D in Fig. 13c. Ultimately, since FRP tensile strain $\varepsilon_{h,P}$ is a function of $v'_{s,max}$ and $\varepsilon_{l,i}$, concrete expansion at the strip region is highly expected do not be considerable enough to enhance $\varepsilon_{l,i}$ and subsequently $\varepsilon_{h,P}$ in partial confinement arrangement with large s_f / D . In other word, concrete expansion at this region is not capable of impressively activating FRP confining pressure.

425 Ultimate condition

FRP confined concrete with full and partial confinement can present the following possible failure modes: i) FRP rupture; ii) a combination of FRP rupture and concrete crushing as function of the distance between strips; iii) concrete crushing. Thus, in addition to FRP rupture, the possibility of concrete crushing should be also controlled in the determination of ultimate condition:

$$\varepsilon_{cu} = \min\left(\varepsilon_{cu,r}, \varepsilon_{cu,c}\right) \tag{36}$$

430 where $\varepsilon_{cu,r}$ and $\varepsilon_{cu,c}$ are the ultimate axial strain corresponding to FRP rupture and concrete 431 crushing, respectively.

432 To calculate $\varepsilon_{cu,r}$, based on Eq. (3), the ultimate secant Poisson's ratio $v_{s,u}$ at the critical section 433 corresponding to FRP rupture can be determined as

$$v_{s,u} = \frac{\varepsilon_{l,j,u}}{\varepsilon_{cu,r}}$$
(37)

434 Considering $\varepsilon_{l,i} = k_{\varepsilon} \times \varepsilon_{l,j}$, Eq. (37) can be written as

$$v_{s,u} = \frac{\varepsilon_{l,i,u}/k_{\varepsilon}}{\varepsilon_{cu,r}} = \frac{\varepsilon_{h,rup}}{k_{\varepsilon}\varepsilon_{cu,r}}$$
(38)

435 where $\varepsilon_{h,rup}$ is FRP hoop rupture strain. Therefore, rearranging Eq. (38) gives

$$\varepsilon_{cu,r} = \frac{\varepsilon_{h,rup}}{k_{\varepsilon} v_{s,u}}$$
(39)

436 FRP hoop rupture strain, $\varepsilon_{h,rw}$, in FRP confined concrete columns under axial loading tends to be smaller than FRP ultimate tensile strain, ε_{fu} (from flat coupon tests). In general, to estimate the 437 value of $\mathcal{E}_{h,rup}$, the existing formulations use a strain-reduction factor (Lam and Teng (2003), ACI 438 439 440.2R-08 (2008), Lim and Ozbakkaloglu (2014b). Lam and Teng [38] came up with an average 440 strain-reduction factor of 0.586 ($\varepsilon_{h,rup} = 0.586\varepsilon_{fu}$), which was adopted by ACI 440.2R-08 (2008). Based on a test database of FRP fully confined circular concrete, Lim and Ozbakkaloglu (2014b) 441 proposed a strain-reduction factor as a function of f_{co} and E_f . In this study, according to the test 442 data of FRP fully confined concrete (Table 2), ACI 440.2R-08 (2008) was modified using 443 regression analysis as: 444

$$\frac{\varepsilon_{h,rup}}{\varepsilon_{fu}} = 0.586\beta \tag{40}$$

445 in which

$$\beta = \frac{1}{0.82 + 0.23\varepsilon_{fu}f_{c0}} \tag{41}$$

As shown in Table 3, the proposed equation results in a slight improvement of ACI 440.2R-08 (2008) in the prediction of the test results of $\varepsilon_{h,rup}$, compared to other models. It should be noted that $\varepsilon_{cu,r}$ in Eq. (39) is a function of $v_{s,u}$ as an input parameter, which can be obtained from the proposed relation between v_s and ε_c (Fig. 11). Accordingly, at a certain level of ε_c , the 450 corresponding v_s can be introduced in Eq. (39) based on the assumption of $v_{s,u} = v_s$ and then, $\varepsilon_{cu,r}$ 451 can be calculated. If $\varepsilon_{cu,r} = \varepsilon_c$, the adopted assumption can be verified and ultimate axial strain 452 corresponding to FRP rupture failure mode is determined.

453 On the other hand, to calculate $\varepsilon_{cu,c}$, according to Tamuzs *et al.* (2006), the slope of lateral-to-454 axial strain relation, between two points of the axial strains of $2\varepsilon_{c0}$ and $\varepsilon_{cu,c}$ was defined as the 455 effective tangential Poisson's ratio of $v_{t,eff}$ as (Fig. 14a):

$$v_{t,eff} = \frac{\varepsilon_{l,j,u} - \varepsilon_{l1}}{\varepsilon_{cu,c} - 2\varepsilon_{c0}}$$
(42)

456 where ε_{l1} and $\varepsilon_{l,j,u}$ are the lateral strains at the critical section corresponding to $2\varepsilon_{c0}$ and $\varepsilon_{cu,c}$, 457 respectively, when concrete crushing occurs. Rearranging Eq. (42) gives:

$$\varepsilon_{cu,c} = 2\varepsilon_{c0} + \frac{\varepsilon_{l,j,u} - \varepsilon_{l1}}{v_{l,eff}}$$
(43)

458 Therefore, Eq. (43) can be expressed as:

$$\varepsilon_{cu,c} = \left(2 + \frac{\gamma - \gamma_{\min}}{v_{t,eff}}\right) \varepsilon_{c0}$$
(44)

459 in which

$$\gamma = \frac{\varepsilon_{l,j,u}}{\varepsilon_{c0}} = \frac{\varepsilon_{l,i,u}}{k_{\varepsilon}\varepsilon_{c0}}$$
(45)

$$\gamma_{\min} = \frac{\varepsilon_{I1}}{\varepsilon_{c0}} = \frac{2\varepsilon_{c0}c_1v_{s,\max}}{\varepsilon_{c0}} = 2c_1v_{s,\max}$$
(46)

Since a FRP partially confined concrete with $s_f/D \ge 1$ was assumed behaving almost as an unconfined concrete, in this case, $\varepsilon_{cu,c}$ can be reasonably approximated as $2\varepsilon_{c0}$ (Mander *et al.* (1988)) and according to the proposed $v_s/v_{s,max}$ versus ε_c relation (Fig. 11), $\varepsilon_{l,i,u} = 2k_{\varepsilon}\varepsilon_{c0}c_1v_{s,max}$. Moreover, for $0 < s_f/D \le 1$, it is assumed that $\varepsilon_{l,i,u}$ linearly decreases from $\varepsilon_{h,rup}$ to $2k_{\varepsilon}\varepsilon_{c0}c_1v_{s,max}$ corresponding to $s_f/D = 0$ and $s_f/D \ge 1$, respectively. Therefore, $\varepsilon_{l,i,u}$ can be estimated as (Fig. 14b):

$$\varepsilon_{l,i,u} = \varepsilon_{h,rup} - \left(\varepsilon_{h,rup} - 2k_{\varepsilon}\varepsilon_{c0}c_{1}v_{s,\max}\right) \left(\frac{s_{f}}{D}\right) \quad , \quad 2k_{\varepsilon}\varepsilon_{c0}c_{1}v_{s,\max} \le \varepsilon_{l,i,u} \le \varepsilon_{h,rup}$$
(47)

Simplifying Eq. (47), and then, introducing in Eq. (45), the parameter γ can be determined as:

$$\gamma = \frac{\varepsilon_{l,i,u}}{k_{\varepsilon}\varepsilon_{c0}} = \left(1 - \frac{s_f}{D}\right)\gamma_{\max} + \frac{s_f}{D}\gamma_{\min} \quad , \quad \gamma_{\min} \le \gamma \le \gamma_{\max}$$
(48)

467 in which

$$\gamma_{\max} = \frac{\varepsilon_{h,rup}}{k_{\varepsilon}\varepsilon_{c0}} = \frac{0.586\beta\varepsilon_{fu}}{k_{\varepsilon}\varepsilon_{c0}}$$
(49)

Therefore, to calculate the ultimate axial strain $\varepsilon_{cu,c}$ corresponding to concrete crushing using Eq. (44), the effective tangential Poisson's ratio of $v_{t,eff}$ should be determined. In the present study, according to the best curve fit of the experimental results of the FRP partially confined specimens with $s_f / D \ge 0.5$ (highly likely to experience concrete crushing prior to FRP rupture, as confirmed by Zeng *et al.* (2018a)), based on a back analysis, $v_{t,eff}$ corresponding to $\varepsilon_{cu,c}$ (Eq. (44)) was proposed as follows:

$$v_{t,eff} = \frac{0.049}{\sqrt{\rho_K}} \tag{50}$$

In Fig. 15a, the experimental results corresponding to the effective tangential Poisson's ratio derived from Eq. (42) are compared with the theoretical counterparts. As can be seen, there is an acceptable predictive performance for the proposed model. As a result, replacing Eq. (50) into Eq. (44) gives:

$$\varepsilon_{cu,c} = \left(2 + 20.4\left(\gamma - \gamma_{\min}\right)\sqrt{\rho_{K}}\right)\varepsilon_{c0}$$
⁽⁵¹⁾

Using Eq. (51), $\varepsilon_{cu,c}$ corresponding to concrete crushing failure mode can be determined. Fig. 15b demonstrates that Eq. (51) is able to estimate experimental $\varepsilon_{cu,c}$ with acceptable agreement. As a result, based on Eq. (36), when $\varepsilon_c > \varepsilon_{cu}$, the analytical incremental procedure gets terminated by determining failure mode either by FRP rupture or concrete crushing.

482 Verification

In this section, the reliability of the proposed confinement model for predicting dilation response of fully and partially FRP confined concrete elements of circular cross section is assessed. In Fig. 16, a flowchart for calculating the dilation response of FRP fully and partially confined concrete columns is presented. As can be seen, the lateral strain versus axial strain relation can be easily determined by following the proposed incremental procedure.

Zeng *et al.* (2018a) conducted an experimental study on fully and partially FRP confined circular
concrete with different confinement configurations. All specimens had a diameter of 150 mm and
a height of 300 mm. The compressive strength of unconfined cylindrical concrete was 23.4 MPa.

The values of thickness, tensile elastic modulus and rupture strain of FRP strips were reported as 0.167 mm, 249.1 GPa and 1.66%, respectively. An example calculation of the dilation behavior, ultimate condition and axial response of the test specimen of S-1-3-25 ($s_f / D = 0.75$, $w_f / D = 0.17$ and $n_f = 1$) is presented as follows:

495 <u>Dilation response:</u> For this purpose, the value of $v_{s,max}$ as a key parameter in the proposed relation 496 should be computed. Based on Eq. (30), ρ_K should be first determined. It can be calculated by 497 using Eq. (27) as:

$$\rho_{K} = \frac{1}{2} K_{e} \frac{\rho_{f} E_{f}}{f_{c0} / \varepsilon_{c0}} = 0.5 \times 0.178 \times \frac{0.0008 \times 249100}{23.4 / 0.0018} = 0.0014$$

498 in which

$$\begin{split} K_e &= 0.75 + 0.12 \frac{w_f}{D} - 0.79 \frac{s_f}{D} = 0.75 + 0.12 \times 0.17 - 0.79 \times 0.75 = 0.178 \quad \text{(Eq. (20))} \\ \rho_f &= \frac{4n_f t_f w_f}{D\left(w_f + s_f\right)} = \frac{4 \times 1 \times 0.167 \times 25}{150\left(25 + 112.5\right)} = 0.0008 \quad \text{(Eq. (23))} \\ \varepsilon_{c0} &= 0.0015 + \frac{f_{c0}}{70000} = 0.0015 + \frac{23.4}{70000} = 0.0018 \quad \text{(Eq. (28))} \end{split}$$

499 Accordingly, introducing ρ_{K} into Eq. (30), $v_{s,max}$ corresponding to $\varepsilon_{c,m}$ (Eq. (31)) can be 500 calculated as:

$$v_{s,\max} = \frac{0.155}{(1.23 - 0.003f_{c0})\sqrt{\rho_K}} = \frac{0.155}{(1.23 - 0.003 \times 23.4)\sqrt{0.0014}} = 3.57$$
$$\varepsilon_{c,m} = 0.0085 - 0.05\rho_K = 0.0085 - 0.05 \times 0.0014 = 0.0084$$

501 Accordingly, the relation between $v_s / v_{s,max}$ and \mathcal{E}_c can be calculated as shown in Fig. 17a.

502 <u>Ultimate conditions</u>: To estimate ultimate axial strain of the test specimens, $\varepsilon_{cu,c}$ and $\varepsilon_{cu,r}$ 503 corresponding to concrete crushing and FRP rupture should be determined by using Eq. (39) and 504 Eq. (51), respectively:

505
$$\varepsilon_{cu,r} = \frac{\varepsilon_{h,rup}}{k_{\varepsilon}v_{s,u}} = \frac{0.0107}{0.31 \times v_{s,u}} = \frac{0.0345}{v_{s,u}}$$
 (Eq. (39))

506
$$\varepsilon_{cu,c} = (2 + 20.4(\gamma - \gamma_{\min})\sqrt{\rho_K})\varepsilon_{c0} = (2 + 20.4(8.75 - 5.35)\sqrt{0.0014})0.0018 = 0.0084$$
 (Eq. (51))

508
$$\gamma = \left(1 - \frac{s_f}{D}\right) \gamma_{\text{max}} + \frac{s_f}{D} \gamma_{\text{min}} = (1 - 0.75) \times 18.81 + 0.75 \times 5.39 = 8.75$$
 (Eq. (45))

509
$$\gamma_{\min} = 2c_1 v_{s,\max} = 2(0.75 + 3.85\rho_K)v_{s,\max} = 2 \times (0.75 + 3.85 \times 0.0014) \times 3.57 = 5.39$$
 (Eq. (46))

510
$$\gamma_{\max} = \frac{\varepsilon_{h,rup}}{k_{\varepsilon}\varepsilon_{c0}} = \frac{0.0107}{0.31 \times 0.0018} = 18.81$$
 (Eq. (49))

511
$$\varepsilon_{h,rup} = 0.586 \beta \varepsilon_{fu} = \frac{0.586}{0.82 + 0.23 \varepsilon_{fu} f_{c0}} \varepsilon_{fu} = \frac{0.586}{0.82 + 0.23 \times 0.0166 \times 23.4} 0.0166 = 0.0107 \text{ (Eq. (40))}$$

512
$$k_{\varepsilon} = 1 - 0.92 \frac{s_f}{D} = 1 - 0.92 \times 0.75 = 0.31 > 0.08$$
 (Eq. (3))

By drawing the relation between $v_{s,u} / v_{s,max}$ and ε_c , as illustrated in Fig. 17b, $\varepsilon_{cu,r}$ corresponding to FRP rupture is obtained as 0.0101. As a result, based on Eq. (35), comparing $\varepsilon_{cu,c}$ and $\varepsilon_{cu,r}$, ultimate axial strain ε_{cu} is equal to 0.0084 with concrete crushing failure mode. Fig. 18 compares the dilation responses of the test specimens with different configurations reported by Zeng *et al.* (2018a) with those obtained from the proposed model. As can be observed, the good predictive performance of the model confirms the reliability and efficiency of the proposed analytical model to predict lateral strain versus axial strain curves, working for both FRP fully and partially confined circular concrete.

521 Lim and Ozbakkaloglu (2014c) experimentally investigated the effects of concrete compressive strength and the type of FRP materials (CFRP, GFRP and AFRP) on the axial and dilation behavior 522 of FRP fully confined concrete columns of circular cross section. All specimens had a diameter of 523 152 mm with a height of 305 mm. Four different values of f_{c0} were considered equal to 30, 50, 74 524 and 98 MPa. The values of FRP thickness, tensile elastic modulus and rupture strain were reported 525 as 0.2 mm, 128.5 GPa and 1.86%; 0.165 mm, 236 GPa and 1.76%; and 0.2 mm, 95.3 GPa and 526 3.21%; for AFRP, CFRP and GFRP, respectively. The details of the experimental program can be 527 528 found from Lim and Ozbakkaloglu (2014c). In Fig. 19, the dilation responses registered experimentally and obtained from the proposed model are compared. As can be seen, in general, 529 the proposed model is able to sufficiently predict the experimental counterparts in case of full 530 confinement with various the types of FRP material and f_{c0} . 531

To extensively verify the proposed confinement model, dilation responses of test specimens with partial confinement conducted by Barros and Ferreira (2008), Zeng *et al.* (2017 and 2018b) are also compared in Fig. 20 to those obtained with the developed model. Overall, a good predictive performance confirms the reliability and efficiency of the proposed analytical model to predict the lateral strain versus axial strain of FRP partially confined concrete elements of circular cross section.

538 Summary and conclusions

In this study, a new model was developed to predict dilation behavior of fully and partially FRP 539 confined concrete elements of circular cross section. To estimate dilation response, the secant 540 Poisson's ratio versus axial strain relations at the critical section placed at the middle distance 541 between FRP strips and at the mid-plane of the strips were proposed as a function of confinement 542 543 stiffness for full and partial confinement arrangements. To simulate the concrete columns with partial confinement configurations, the confinement stiffness index proposed by Teng et al. (2009) 544 was modified based on the concept of confinement efficiency factor. For this purpose, in addition 545 to vertical arching action, the effect of the non-uniform distribution of the concrete expansion was 546 547 addressed for determining the confinement efficiency factor. A new methodology was also developed to predict the ultimate condition of partially FRP confined concrete taking into account 548 the possibility of concrete crushing and FRP rupture failure modes. To validate the analytical 549 550 model, it was vastly applied to predict the dilation behavior of the relevant experimental specimens available in the literature. The comparison between the model and experimental counterparts 551 revealed that it is capable of providing an estimation of dilation responses with appropriate 552 precision for design purposes. 553

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Data Availability Statement

All data, models, and code generated or used during the study appear in the submitted article.

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Table 1

ID		s_f/D	$f_{cc} \exp / f_{c0}$	$v'_{s,u} exp$	$k_{\varepsilon} e^{xp} a$
	W15S3L1	0.57	1.01	0.82	0.33
Domog on d Formaina (2000)	W15S3L2	0.57	1.01	0.74	0.29
Barros and Ferreira (2008)	W15S3L3	0.57	1.01	1.05	0.42
	W15S3L4	0.57	1.04	0.89	0.36
	S-1-3-25-1	0.75	1.09	0.92	0.37
	S-1-3-25-2	0.75	1.10	0.98	0.39
	S-1-3-30-1	0.70	1.09	0.98	0.39
	S-1-3-30-2	0.70	1.08	1.05	0.42
7_{opg} at al. (2018_{c})	S-1-3-35-1	0.65	1.16	0.85	0.34
Zeng <i>ei ai</i> . (2018a)	S-1-3-35-2	0.65	1.07	1.06	0.42
	S-2-3-25-1	0.75	1.15	0.95	0.38
	S-2-3-25-2	0.75	1.17	0.98	0.39
	S-1-4-25-1	0.44	1.13	1.19	0.47
	S-1-4-25-2	0.44	1.16	1.29	0.52
	S-1-3-25	0.75	1.00	1.31	0.52
Zeng et al. (2018b)	S-1-3-30	0.73	1.00	1.54	0.62
	S-1-4-25	0.44	1.05	1.14	0.45
	S75	0.75	1.23	0.67	0.27
Wang et al. (2018)	S100	1.00	1.18	0.24	0.10
	S150	1.50	1.11	0.24	0.10

Table 1. Details of the test specimens

Note: ^a: $k_{\varepsilon} \exp = v'_{s,u} \exp / 2.5$

Table 2

Table 2. Assembled database for fully and partially FRP confined concrete elements of circular cross section

	Confinement arrangement			f	0.7		
ID	Total number	Full	Partial	- <i>J</i> ²⁰ (MPa)	μ× (%)	Vs,max	
Rochette and Labossie`re (2000)	2	2	-	42.0 - 43.0	3.4 - 5.0	0.61 - 0.97	
Shehata <i>et al.</i> (2001)	2	2	-	25.6 - 29.8	3.8 - 6.7	0.76 - 0.87	
Teng and Lam (2002)	3	3	-	36.6 - 39.0	2.2 - 4.4	0.66 - 0.99	
Xiao and Wu (2003)	39	39	-	34.5 - 57.0	2.1 - 9.3	0.32 - 1.50	
Berthet et al. (2005)	15	15	-	22.2 - 171	2.0-15.1	0.65 - 2.08	
Al-Salloum (2007)	1	1	-	28.8	8.0	0.64	
Barros and Ferreira (2008)	39	8	31	22.9 - 40.0	0.2 - 26.2	0.25 - 2.20	
Wang and Wu (2008)	4	4	-	30.9 - 52.1	2.1 - 6.1	0.62 - 1.98	
Eid et al. (2009)	18	18	-	31.1 - 75.9	1.3 - 6.9	0.45 - 1.29	
Benzaid and Mesbah (2014)	6	6	-	25.9 - 61.8	1.6 - 9.2	0.95 - 3.77	
Lim and Ozbakkaloglu (2014c)	36	36	-	29.6 - 98.0	1.6 - 6.1	0.61 - 1.53	
Vincent and Ozbakkaloglu (2015)	6	6	-	110.3	3.8 - 5.7	0.77 - 1.06	
Zeng et al. (2017)	12	3	9	24.3	0.8 - 8.3	0.62 - 1.84	
Zeng et al. (2018a)	57	6	54	23.4	0.2 - 13	0.39 - 3.16	
Zeng et al. (2018b)	15	-	15	23.5	0.2 - 5.6	0.90 - 5.31	
Wang <i>et al.</i> (2018)	7	1	6	36.0	0.3 - 5.9	0.42 - 3.03	
Guo <i>et al.</i> (2019)	21	-	21	33.6 - 41.7	0.5 - 5.0	0.44 - 1.73	
Suon <i>et al.</i> (2019)	3	3	-	15.8	1.4 - 4.2	1.00 - 1.53	
ALL	289	153	136	15.8-171	0.2-26.2	0.2-5.3	
	-0/	100		10.0 171			

Table 3

ID	Expression	Mean	SD	MAPE
Lam and Teng (2003) ACI 440.2R-08 (2008)	$\frac{\varepsilon_{h,rup}}{\varepsilon_{fu}} = 0.586$	1.03	0.68	0.33
Lim and Ozbakkaloglu (2014b)	$\frac{\varepsilon_{h,rup}}{\varepsilon_{fu}} = 0.9 - 0.0023 f_{c0} - 0.75 E_f \times 10^{-6}$	1.19	0.80	0.38
Proposed model	$\frac{\varepsilon_{h,rup}}{\varepsilon_{fu}} = 0.586\beta$ in which $\beta = \frac{1}{0.82 + 0.23\varepsilon_{fu}f_{c0}}$	1.00	0.63	0.31

Table 3. Comparison of the reliability of the proposed model and other models

Fig. 1



Fig. 1. Dilation behavior of typical FRP confined concrete





Fig. 2. Detailing of concrete column partially confined by FRP strips



Fig. 3. Lateral expansion in FRP confined concrete: a) partial confinement and b) full confinement



Fig. 4. Variation of k_{ε} with s_{f} obtained from Eq. (3) and the experimental results reported by Barros and Ferreira (2008), Wang *et al.* (2018), Zeng *et al.* (2018a and 2018b)





Fig. 5. FRP confined concrete with a) partial confinement b) full confinement Note: FCCC and PCCC denote fully and partially confined concrete columns of circular cross section, respectively

Fig. 6



Fig. 6. Variation of K_e with s_f / D for a partial system





Fig. 7. Confining action in FRP confined concrete columns; a) full confinement mechanism, b) partial confinement mechanism



Fig. 8. Axial and lateral behavior for the test specimens with two FRP layers, conducted by Zeng *et al.* (2018a): a) axial stress vs axial strain curve; b) concrete lateral strain vs axial strain curve; c) axial stress vs volumetric strain; d) secant Poisson's ratio vs axial strain



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(FCCC: Fully confined concrete column of circular cross section; PCCC: Partially confined concrete column of circular cross section)

Fig. 10



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Fig. 11. Normalized secant Poisson's ratio versus axial strain as a function of ρ_K



Fig. 12. Comparison of the proposed analytical relation and experimental results for the different levels of ρ_{K}

Note: Experimental results were reported by Teng and Lam (2002), Berthet *et al.* (2005); Eid *et al.* (2009), Benzaid and Mesbah (2014); Vincent and Ozbakkaloglu (2015), Zeng *et al.* (2018a), Zeng *et al.* (2018b), Guo *et al.* (2019) and Suon *et al.* (2019)



Fig. 13. a) and b) Variations of $\mathcal{E}_{l,j}$ and $\mathcal{E}_{l,i}$ with \mathcal{E}_{c} ; c) influence of s_{f} / D on $v_{s,max}$ and $v'_{s,max}$



Fig. 14. a) Typical lateral versus axial strain curve; b) Typical $\mathcal{E}_{l,i,u}$ versus s_f / D curve



Fig. 15. Comparison between the experimental and theoretical results; a) $v_{t,eff}^{\text{Exp.}}$ vs ρ_K curve b) $\mathcal{E}_{cu,c}^{\text{Theo.}}$ vs $\mathcal{E}_{cu,c}^{\text{Exp.}}$ curve



Fig. 16. A flowchart for calculating the dilation characteristics of FRP fully and partially confined concrete elements



Fig. 17. Determination of the dilation response of the test specimens of S-1-3-25 conducted by Zeng *et*

al. (2018a) using the proposed model





Fig. 18. Analytical analyses versus experimental results for the FRP fully and partially confined specimens tested by Zeng *et al.* (2018a)



Fig. 19. Analytical analyses versus experimental results for the FRP fully confined specimens tested by Lim and Ozbakkaloglu (2014c)



Fig. 20. Analytical analyses versus experimental results for the FRP partially confined specimens tested by Barros and Ferreira (2008), Zeng *et al.* (2017) and Zeng *et al.* (2018b)